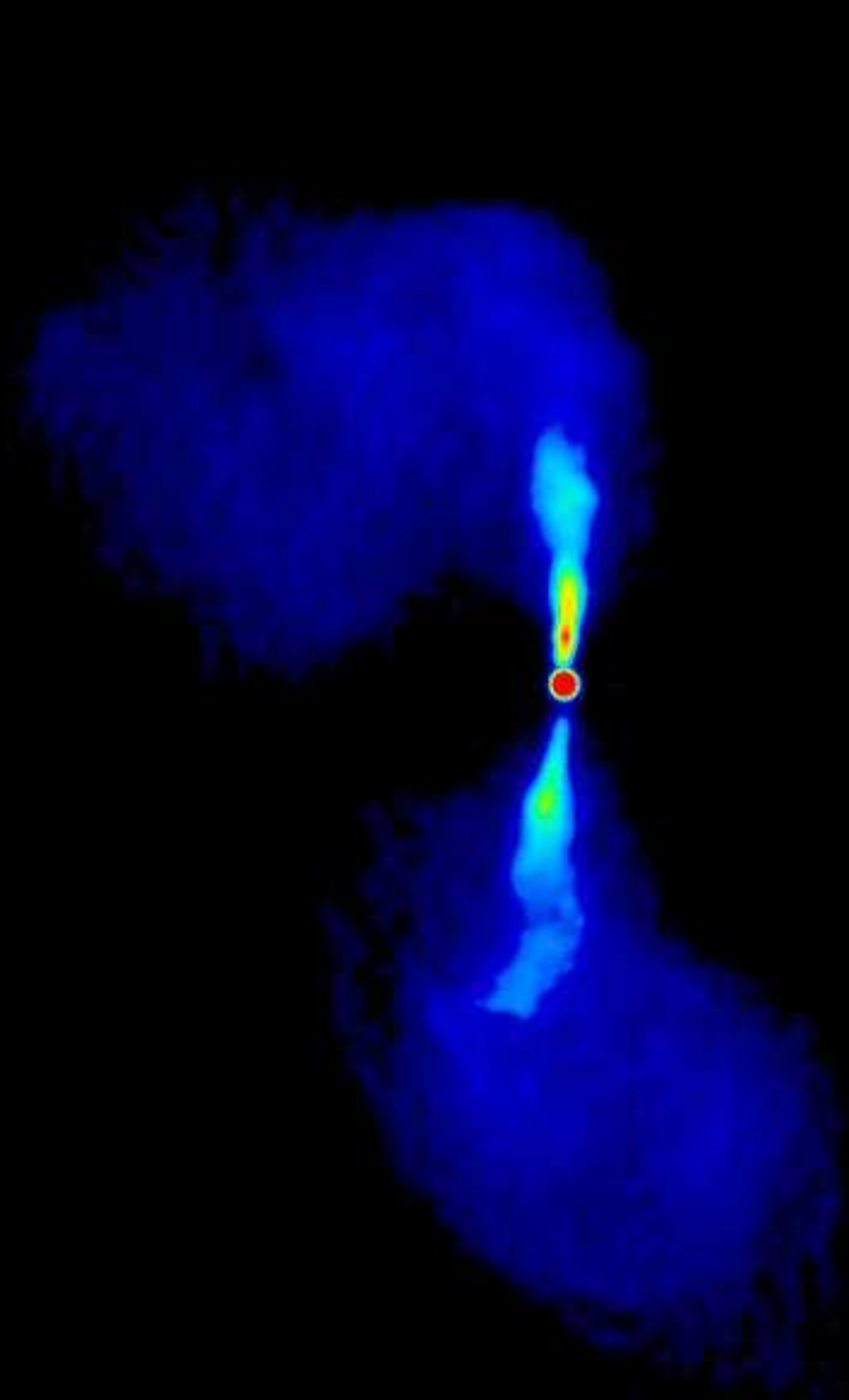


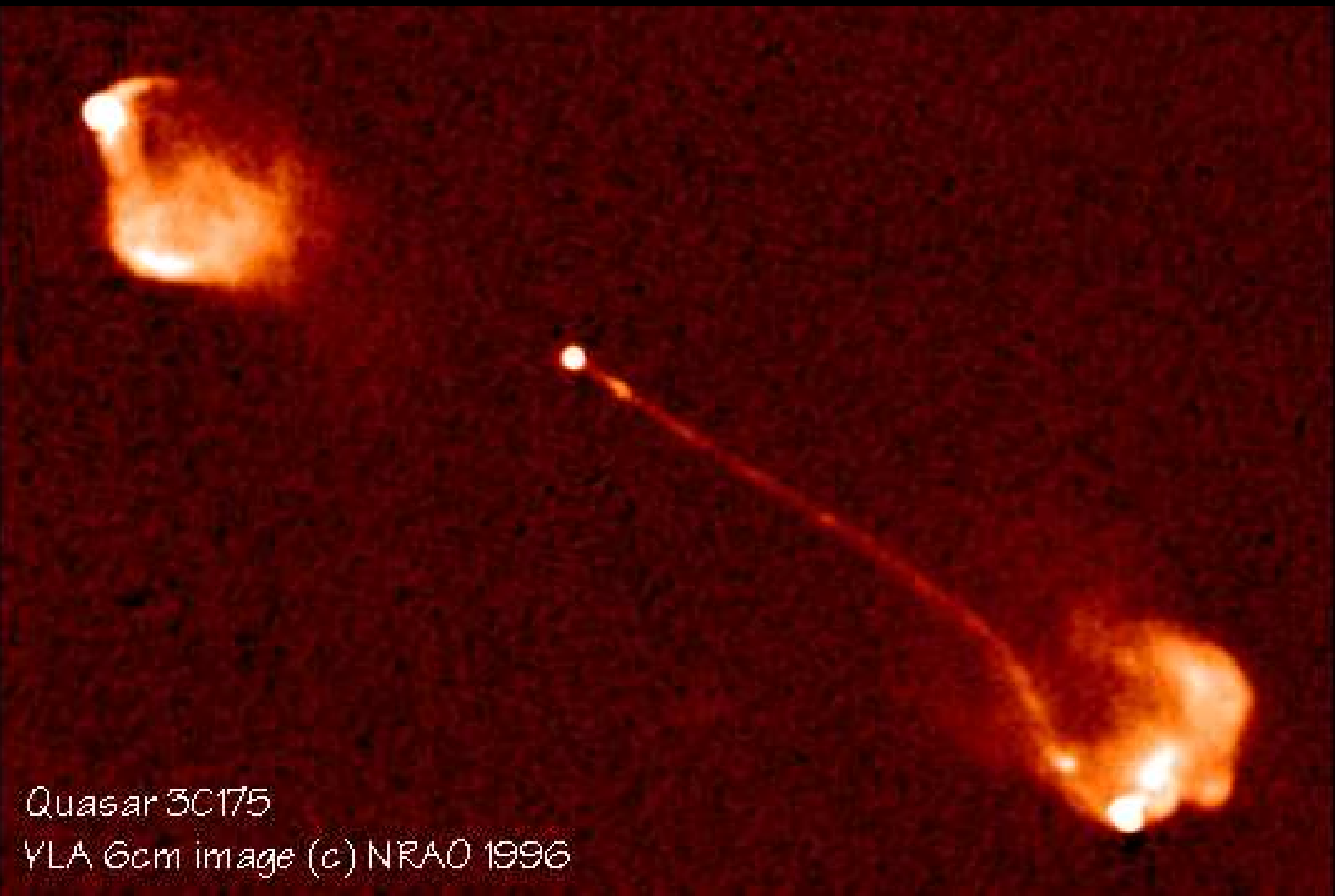


# *Jets and Radio Loud AGN*



Fanaroff-Riley Type 1: strong nucleus, asymmetric jets with wide opening angle ending in plumes

M84 (3C272.1) (Laing & Bridle, 1987): VLA  
4885 MHz,  $134'' \times 170''$ ; see also  
<http://www.jb.man.ac.uk/atlas/other/3C272P1>



Quasar 3C175  
YLA 6cm image (c) NRAO 1996

Radio image of 3C175 ( $z = 0.768$ ; A. Bridle, priv. comm.)

Fanaroff-Riley Type 2: weak (one-sided) jet ending in radio lobes, lobe dominated



## Synchrotron Radiation

Jets are observed to have **strong polarization** and **power law radio spectrum**. These are characteristics of **synchrotron radiation**.

**Synchrotron-Radiation** (=Magnetobremmsstrahlung): Radiation emitted by relativistic electrons in a magnetic field.

*Goal:* Qualitative analysis:

1. Derive the **motion of electrons in magnetic fields**
2. Then use Larmor's formula to obtain the **radiation characteristic from relativistic motion**
3. Use the **Doppler-effect** to convert into the observer's frame of reference.
4. **Integrate over electron distribution** to obtain the final spectrum.

Detailed theory: see Ginzburg & Syrovatskii (1965), Ginzburg & Syrovatskii (1969), Blumenthal & Gould (1970), Reynolds (1982).



## Relativistic Motion

Lorentz-Force ( $\mathbf{E} = 0$ )

$$\frac{d\mathbf{p}}{dt} = \frac{e}{c} \mathbf{v} \times \mathbf{B} \quad \text{where} \quad \mathbf{p} = \frac{m_e \mathbf{v}}{\sqrt{1 - \beta^2}} = \gamma m_e \mathbf{v} \quad (10.1)$$

where  $\beta = v/c$ .

**Assumption:** No radiative losses (i.e., electron does *not* emit synchrotron radiation...):  $\gamma = \text{const.}$

Velocity-vector of the electron:

$$\mathbf{v}_{\parallel} = \frac{\mathbf{v} \cdot \mathbf{B}}{B} \frac{\mathbf{B}}{B} \quad \mathbf{v}_{\perp} = \frac{\mathbf{B} \times (\mathbf{v} \times \mathbf{B})}{B^2} \quad (10.2)$$

$$|\mathbf{v}_{\parallel}| = v \cos \alpha \quad |\mathbf{v}_{\perp}| = v \sin \alpha \quad (10.3)$$

where  $\alpha$  (**pitch-angle**):  $\angle(\mathbf{v}, \mathbf{B})$

No acceleration parallel to the  $\mathbf{B}$ -field  $\implies$  only  $v_{\perp}$  is interesting  $\implies$  circular motion:

$$m_e a_{\perp} = \frac{\gamma m_e v_{\perp}^2}{R} = \frac{e}{c} v_{\perp} B \quad (10.4)$$

$$\frac{v_{\perp}}{R} = \frac{eB}{\gamma m_e c} = \frac{\omega_L}{\gamma} = \omega_B \quad (10.5)$$

where  $\omega_L = 2\pi\nu_L$ : **Larmor frequency** (also Cyclotron frequency, gyrofrequency).



## Numerical values

Numerically, Larmor frequency is

$$\nu_L = 2.8 B_{1G} \text{ MHz} \quad (10.6)$$

The radius of the orbit (**Larmor radius**) is

$$R = \frac{\gamma v_{\perp}}{\omega_L} \approx 10^7 \frac{E_{1\text{GeV}}}{B_{1G}} \text{ cm} \quad (10.7)$$

Typical values:

$$B \approx 10^{-5} \text{ G}, E = 1 \text{ GeV}, \implies R = 3 \times 10^{13} \text{ cm (2 AU)}.$$

i.e., small on cosmic scales



## Radiated Energy, I

Electrodynamics: **Radiation of an accelerated electron:**

$$P_{\text{em}} = \frac{2e^2}{3c^3} \gamma^4 \left( a_{\perp}^2 + \gamma^2 a_{\parallel}^2 \right) \quad (10.8)$$

where  $a$  is the acceleration.

([Messy] derivation by Lorentz-transforming the classical Larmor formula ( $P = (2e^2/3c^3) \cdot a^3$ ), see, e.g., Shu)

For **circular motion**,  $a_{\perp} = \omega_B v_{\perp}$  and  $a_{\parallel} = 0$ . Hence

$$P_{\text{em}} = \frac{2e^2}{3c^3} \gamma^4 \frac{v_{\perp}^2 e^2 B^2}{\gamma^2 m_e^2 c^2} \quad (10.9)$$

$$= 2\beta^2 \gamma^2 c \cdot \sigma_{\text{T}} \cdot U_{\text{B}} \cdot \sin^2 \alpha \quad (10.10)$$

where  $U_{\text{B}} = B^2/8\pi$  (**Energy density of the  $B$ -field**),  $\sigma_{\text{T}} = \frac{8\pi e^4}{3m_e^2 c^4}$  (**Thomson-cross section**).

Presence of  $\sigma_{\text{T}}$  due to quantum electrodynamics: Derivation of synchrotron-radiation in frame of reference of electron via interaction of electron with a virtual photon of the magnetic field (i.e., **Compton scattering with virtual photon**).



## Radiated Energy, II

Total energy radiated: Integration over all electrons.

*Assumption:* Isotropic velocity distribution.

Average pitch angle

$$\langle \sin^2 \alpha \rangle = \frac{1}{4\pi} \int_0^{4\pi} \sin^2 \alpha d\Omega = \frac{1}{4\pi} \int_0^{2\pi} d\varphi \int_0^\pi \sin^2 \alpha \sin \alpha d\alpha = \frac{2}{3} \quad (10.11)$$

therefore

$$\langle P_{\text{em}} \rangle = \frac{4}{3} \beta^2 \gamma^2 c \sigma_{\text{T}} U_{\text{B}} \quad (10.12)$$

for  $\beta \rightarrow 1$ .

*Note:* Since  $E = \gamma m_e c^2 \implies P \propto E^2 U_{\text{B}}$ .

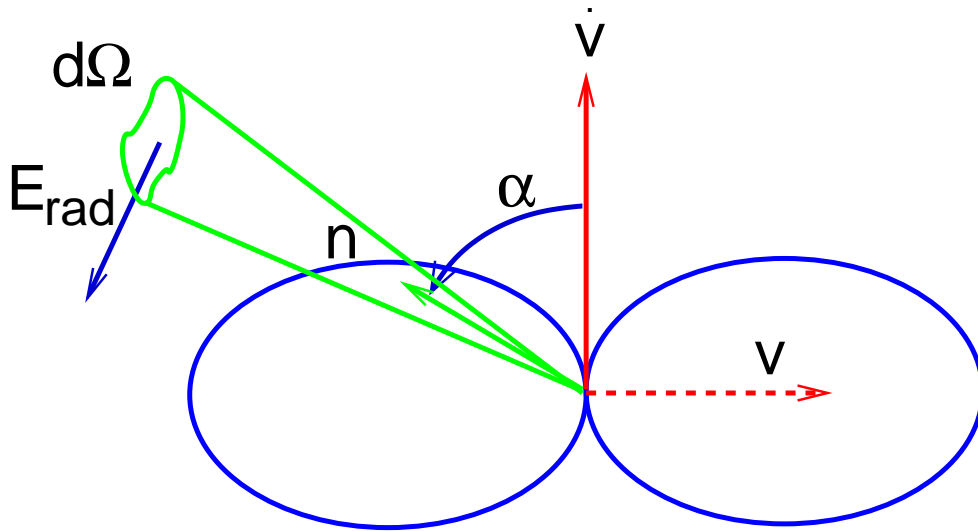
*Note:*  $P_{\text{em}} \propto \sigma_{\text{T}} \propto m_e^{-2} \implies$  Synchrotron radiation from charged particles with larger mass (protons,...) is negligible.

*Note:* Life-time of particle of energy  $E$  is

$$t_{1/2} \sim \frac{E}{P} \propto 1/(B^2 E) = 5 \text{ s} \left( \frac{B}{1 \text{ T}} \right)^{-2} \gamma^{-1} = 1.6 \times 10^7 \text{ years} \left( \frac{B}{10^{-7} \text{ T}} \right)^{-2} \gamma^{-1} \quad (10.13)$$

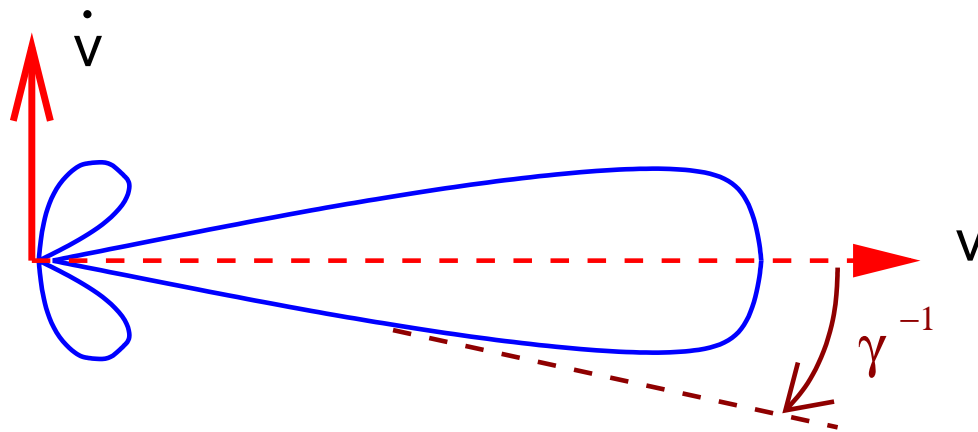


# Single Electron spectrum, I



Frame of reference of electron:  
Emitted radiation has **dipole characteristic** (see, e.g., Eq. 6.2).

after Rybicki & Lightman, Fig. 3.5

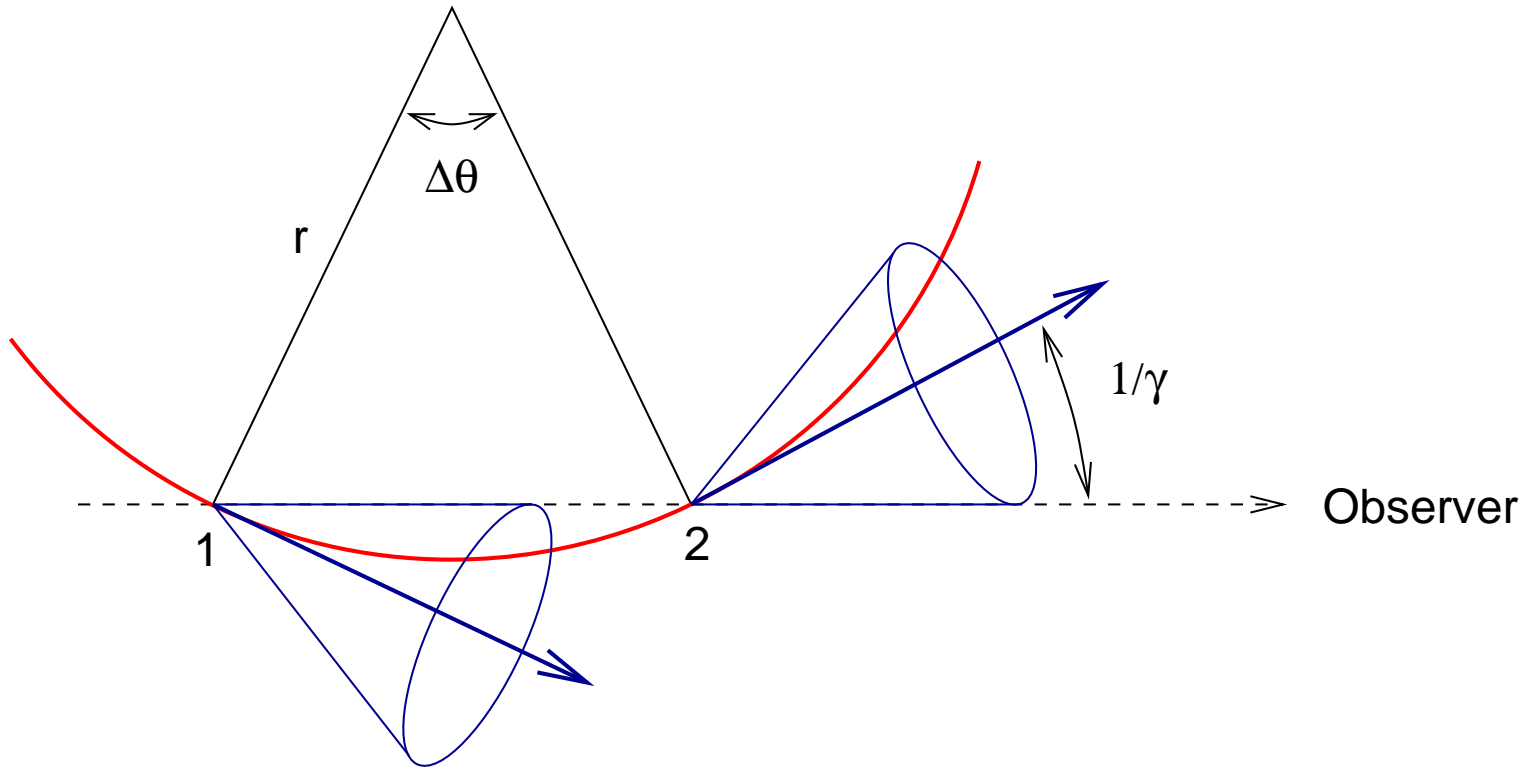


Lorentz-Transform into laboratory system: **Forward Beaming**. **Opening angle** is  $\Delta\theta \approx \gamma^{-1}$ .

after Rybicki & Lightman, Fig. 4.11d



## Single Electron spectrum, II



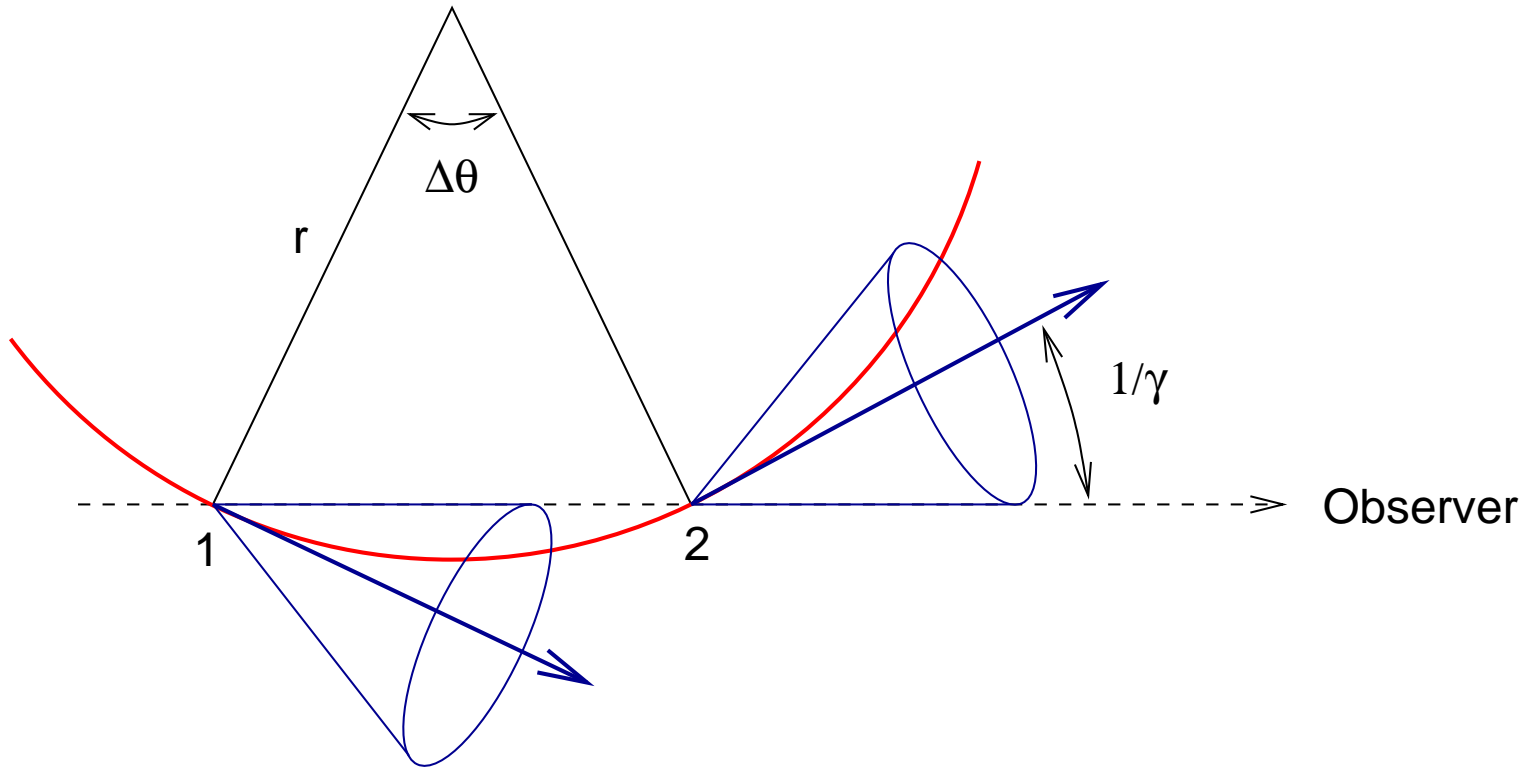
(Rybicki & Lightman, 1979, after Fig. 6.2)

**Electron frame of rest:** beam passes observer during time

$$\Delta t = \frac{\Delta\theta}{\omega_B} = \frac{m_e c \gamma}{eB} \frac{2}{\gamma} = \frac{2}{\omega_L} \quad (10.14)$$



## Single Electron spectrum, III



(Rybicki & Lightman, 1979, after Fig. 6.2)

**Observer frame:** Doppler! (electron is closer at end of beam)

⇒ observed pulse duration:

$$\tau = \left(1 - \frac{v}{c}\right) \Delta t = (1 - \beta) \Delta t \quad (10.15)$$



## Single Electron spectrum, IV

For  $\gamma \gg 1$ , i.e.,  $\beta = v/c \sim 1$

$$\frac{1}{\gamma^2} = 1 - \frac{v^2}{c^2} = (1 + \beta)(1 - \beta) \approx 2(1 - \beta) \quad (10.16)$$

such that

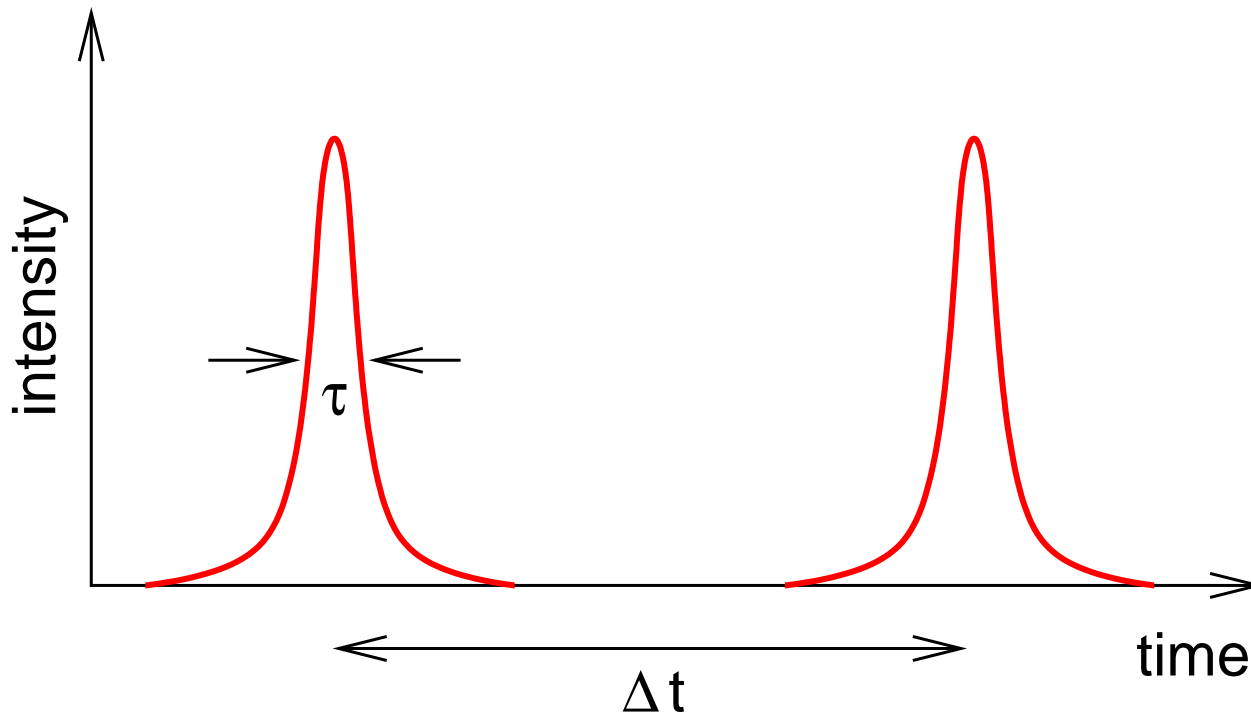
$$\tau = (1 - \beta)\Delta t = \frac{1}{2} \left(1 - \frac{v^2}{c^2}\right) \Delta t = \frac{1}{\gamma^2 \omega_L} \quad (10.17)$$

Thus the **characteristic frequency** of the radiation is given by

$$\omega_c = \gamma^2 \omega_L = \frac{eB}{m_e c} \left( \frac{E}{m_e c^2} \right)^2 \quad (10.18)$$



## Resulting Field



after Shu, Fig. 18.2

The observed time-dependent  $E$ -Field,  $E(t)$ , from one electron is a sequence of pulses of width  $\tau$ , separated in time by  $\Delta t$ .

To a good precision, we can approximate these single peaks with  $\delta$ -functions.

In reality: derive spectrum by **Fourier-transforming**  $E(t)$ . Basic result is the same.



## Nonthermal Synchrotron Radiation, I

**Spectral energy distribution**  $P_\nu$  of one electron with total energy  $E = \gamma m_e c^2$  is

$$P_\nu(\gamma) = \frac{4}{3} \beta^2 \gamma^2 c \sigma_T U_B \delta(\nu - \gamma^2 \nu_L) \quad (10.19)$$

where  $\delta(x)$  is a  $\delta$ -function, i.e.,

$$\delta(x) = 0 \quad \text{for } x \neq 0 \quad \text{and} \quad \int_{-\infty}^{+\infty} \delta(x) dx = 1 \quad (10.20)$$

i.e., electron with energy  $\gamma m_e c^2$  “blinks” at frequency  $\nu = \gamma^2 \nu_L = 1/\tau$ .

For an electron distribution,  $n(\gamma)$ , the **emitted spectrum** is found by properly weighting contributions of electrons with different energies:

$$P_\nu = \int_1^\infty P_\nu(\gamma) n(\gamma) d\gamma \quad (10.21)$$

Most important case: **nonthermal synchrotron radiation**, where electrons have a **power-law distribution**

$$n(\gamma) d\gamma = n_0 \gamma^{-p} d\gamma \quad (10.22)$$



## Nonthermal Synchrotron Radiation, II

Insert distribution into Eq. (10.21) and perform the integration:

$$P_\nu = \int_1^\infty \frac{4}{3} \beta^2 \gamma^2 c \sigma_T U_B \delta(\nu - \gamma^2 \nu_L) n_0 \gamma^{-p} d\gamma \quad (10.23)$$

since  $\gamma \gg 1$ :  $\beta \approx 1$

$$= A \int_1^\infty \gamma^{2-p} \delta(\nu - \gamma^2 \nu_L) d\gamma \quad (10.24)$$

substituting  $\nu' = \gamma^2 \nu_L$ , i.e.,  $d\nu' = \nu_L 2\gamma d\gamma$

$$= B \int_{\nu_L}^\infty \gamma^{1-p} \delta(\nu - \nu') d\nu' \quad (10.25)$$

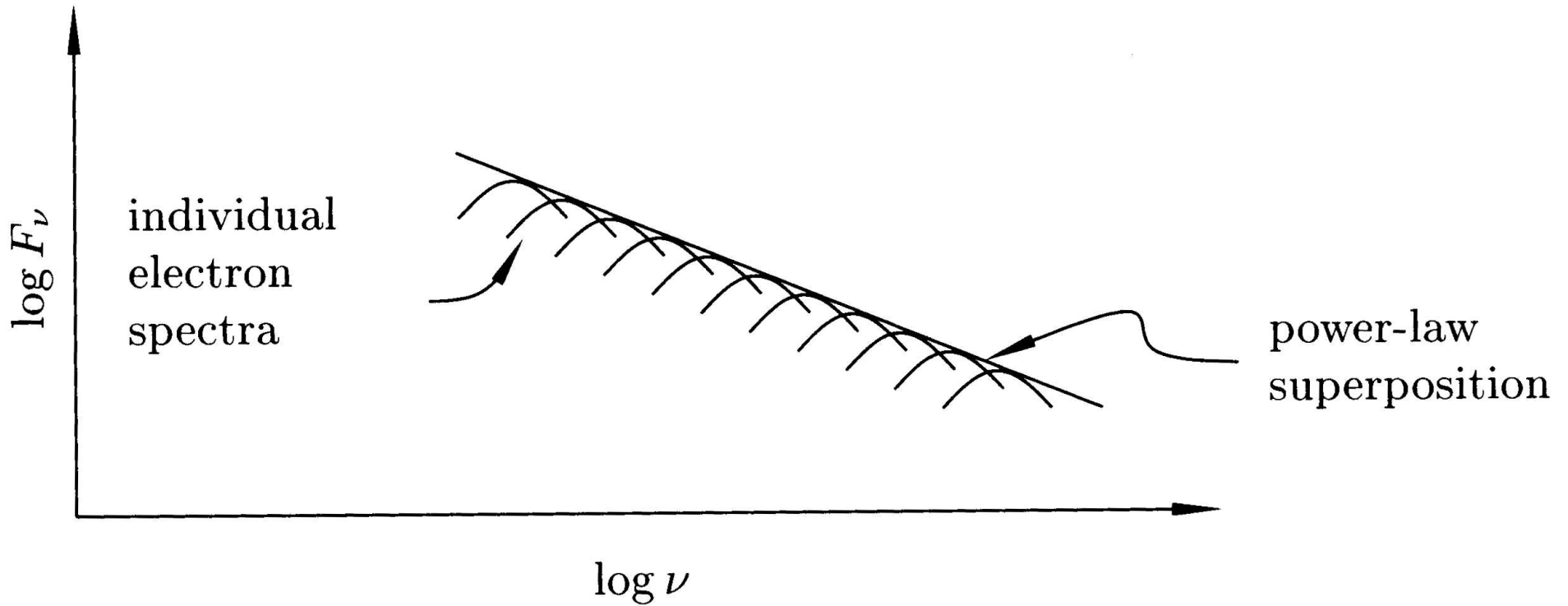
since  $\gamma = (\nu' / \nu_L)^{1/2}$ , one finally finds

$$P_\nu = \frac{2}{3} c \sigma_T n_0 \frac{U_B}{\nu_L} \left( \frac{\nu}{\nu_L} \right)^{-\frac{p-1}{2}} \quad (10.26)$$

The spectrum of an electron power-law distribution is a power-law!



# Nonthermal Synchrotron Radiation, III



Shu, Fig. 18.4





## Summary

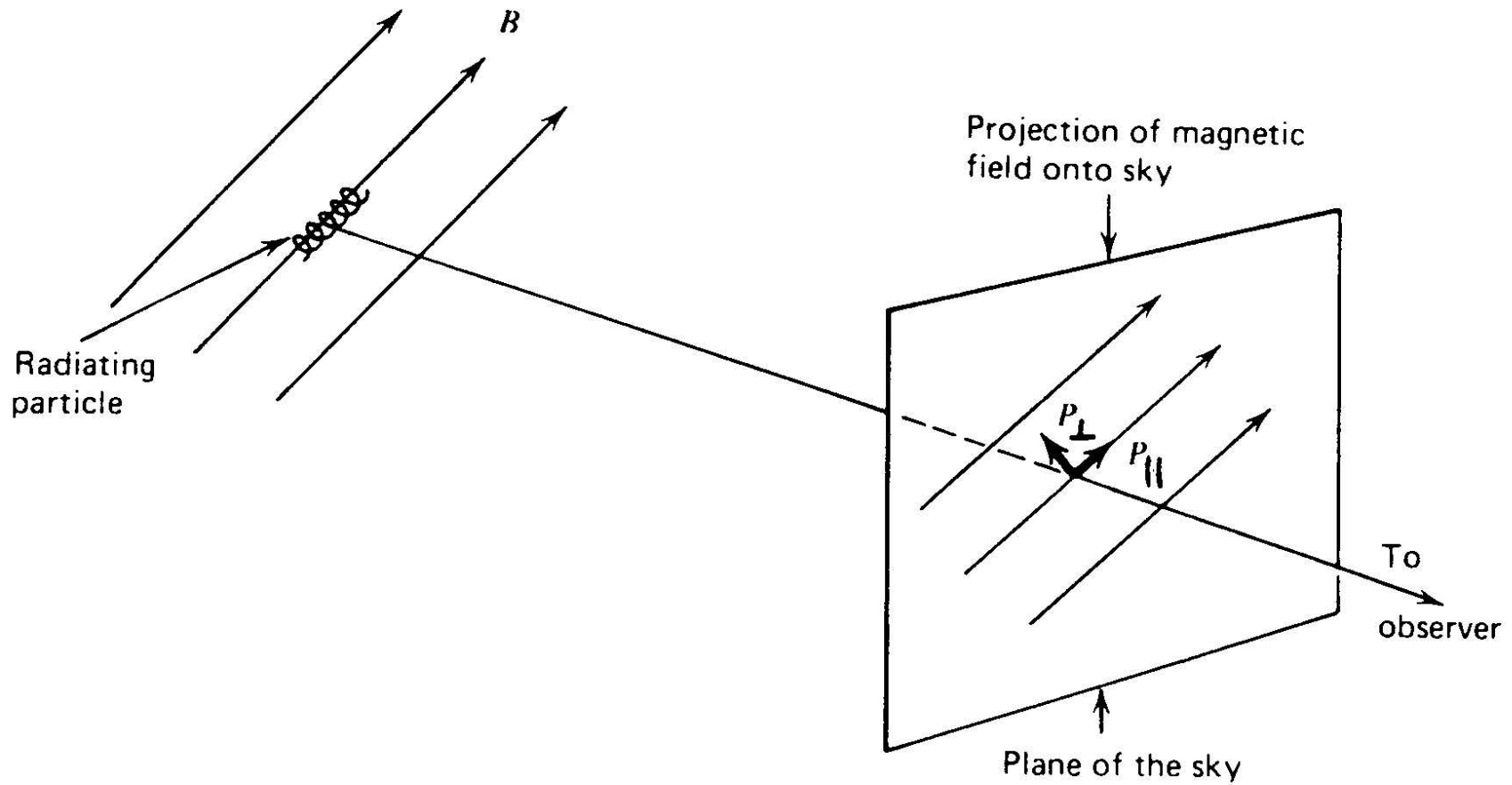
What we have done so far:

1. Motion of the electron
2. Radiation characteristic from relativistic motion
3. Doppler-effect
4. Integration over electron distribution

It is possible to do the same analytically without any approximations. This is too complicated to be done here. See the references for details.



# Exact Results, I



(Rybicki & Lightman, 1979, Fig. 6.7)

Exact calculation needs to take into account **polarization** of synchrotron radiation.



## Exact Results, II

Result of exact calculation for **both polarization directions**:

$$\begin{pmatrix} P_{\parallel} \\ P_{\perp} \end{pmatrix} = \frac{\sqrt{3} e^3 B}{2 m c^2} \begin{pmatrix} F(\nu/\nu_c) - G(\nu/\nu_c) \\ F(\nu/\nu_c) + G(\nu/\nu_c) \end{pmatrix} \quad (10.27)$$

where

$$F(x) = x \int_x^{\infty} K_{5/3}(y) dy \quad (10.28)$$

$$G(x) = x K_{2/3}(x) \quad (10.29)$$

and  $K_i$  are modified Bessel-functions of  $i$ -th order

Polarization allows to measure the magnetic field direction

$$F(x) = x \int_x^\infty K_{3/2}(\eta) d\eta \quad \text{and} \quad \mathfrak{E}(x) = xK_{2/2}(x)$$

$x$	$F(x)$	$\mathfrak{E}(x)$	$x$	$F(x)$	$\mathfrak{E}(x)$
0	0	0	0.90	0.694	0.521
0.001	0.213	0.107	1.0	0.655	0.494
0.005	0.358	0.184	1.2	0.566	0.439
0.01	0.445	0.231	1.4	0.486	0.386
0.025	0.583	0.312	1.6	0.414	0.336
0.050	0.702	0.388	1.8	0.354	0.290
0.075	0.772	0.438	2.0	0.301	0.250
0.10	0.818	0.475	2.5	0.200	0.168
0.15	0.874	0.527	3.0	0.130	0.111
0.20	0.904	0.560	3.5	0.0845	0.0726
0.25	0.917	0.582	4.0	0.0541	0.0470
0.29	0.918	0.592	4.5	0.0339	0.0298
0.30	0.918	0.596	5.0	0.0214	0.0192
0.40	0.901	0.607	6.0	0.0085	0.0077
0.50	0.872	0.603	7.0	0.0033	0.0031
0.60	0.832	0.590	8.0	0.0013	0.0012
0.70	0.788	0.570	9.0	0.00050	0.00047
0.80	0.742	0.547	10.0	0.00019	0.00018



## Total Emitted Spectrum

The **total emitted power** for monoenergetic electrons is

$$P(\nu) = P_{\parallel}(\nu) + P_{\perp}(\nu) \propto F(\nu) \quad (10.30)$$

As before, the total emitted spectrum is found by integrating over the electron energy distribution. For a power-law:

$$\begin{pmatrix} P_{\parallel}(\nu) \\ P_{\perp}(\nu) \end{pmatrix} = \left( \frac{\sqrt{3}}{2} \right) n_0 \frac{e^3 B}{m_e c^2} \begin{pmatrix} J_F - J_G \\ J_F + J_G \end{pmatrix} \left( \frac{2\nu}{3\nu_L} \right)^{-(p-1)/2} \quad (10.31)$$

where

$$J_F = \frac{2^{(p+1)/2}}{p+1} \Gamma\left(\frac{p}{4} + \frac{19}{12}\right) \Gamma\left(\frac{p}{4} - \frac{19}{12}\right) \quad (10.32)$$

$$J_G = 2^{(p-3)/2} \Gamma\left(\frac{p}{4} + \frac{7}{12}\right) \Gamma\left(\frac{p}{4} - \frac{1}{12}\right) \quad (10.33)$$

$\Gamma(x) = \int_0^{\infty} t^{-x} e^{-t} dt$  is the **Gamma-function**.



## Degree of Polarization

The **degree of polarization** is defined by

$$\text{degree of polarization} := \frac{P_{\perp} - P_{\parallel}}{P_{\perp} + P_{\parallel}} \quad (10.34)$$

For a **power law electron distribution**:

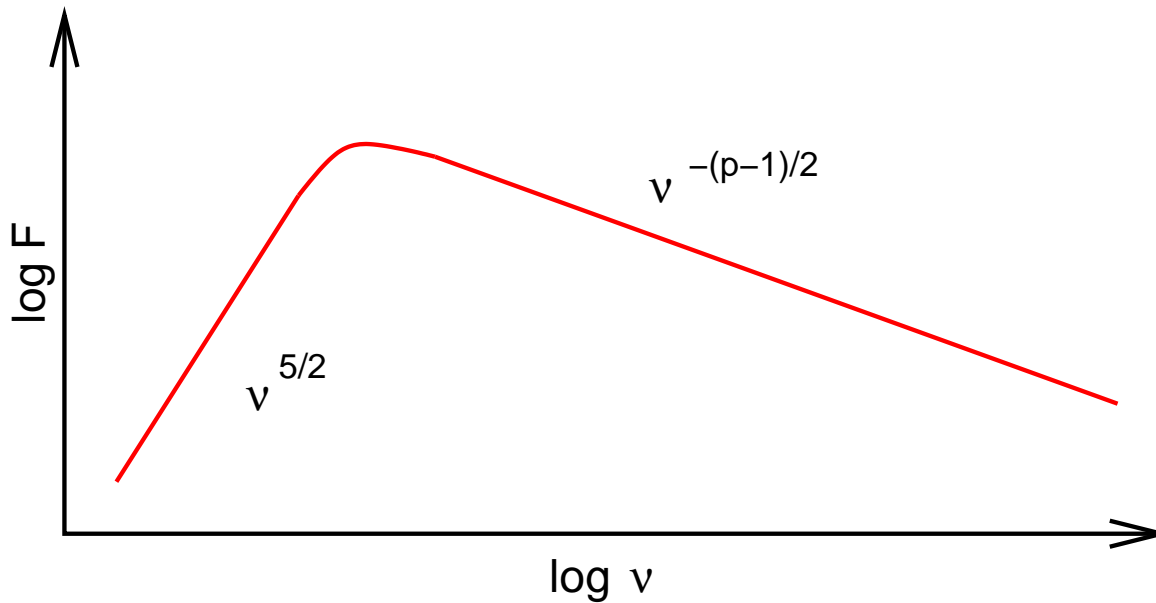
$$\frac{P_{\perp} - P_{\parallel}}{P_{\perp} + P_{\parallel}} = \frac{J_G}{J_F} = \frac{p + 1}{p + 7/3} \quad (10.35)$$

For  $p = 2.5$  the degree of polarization is  $\sim 70\%$ . This is **very large!!**

**Caveat:** Faraday-rotation and B-field inhomogeneities can decrease the degree of polarization.



## Synchrotron Self-Absorption



after Shu, Fig. 18.6

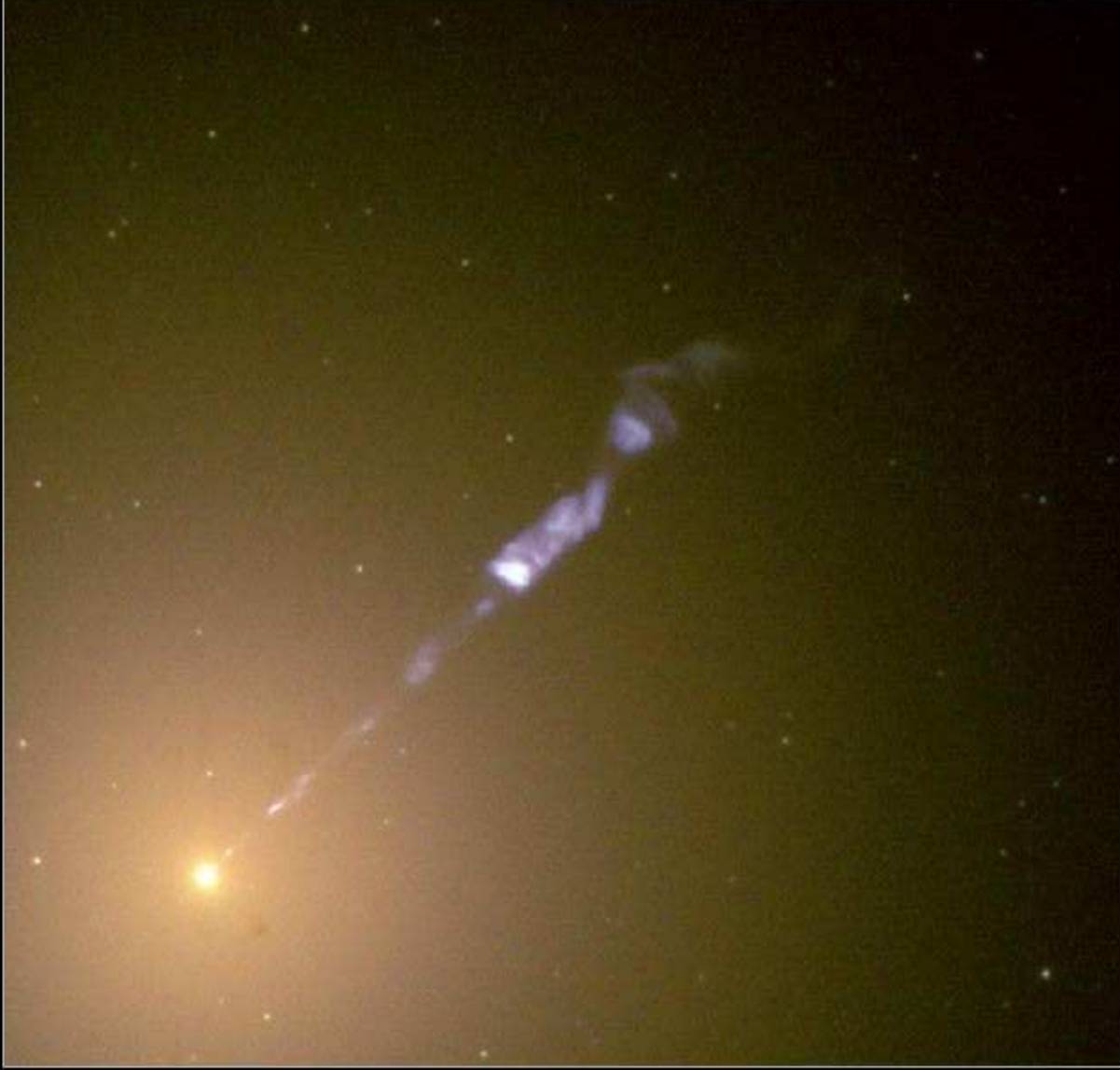
For a power law electron distribution  $\propto E^{-p}$ , total spectral shape is:

For low frequencies:  $P_\nu \propto B^{-1/2} \nu^{5/2}$  (independent of  $p$ )  
For large frequencies:  $P_\nu \propto \nu^{-(p-1)/2}$

At low  $\nu$ : synchrotron emitting electrons can absorb synchrotron photons: **synchrotron self-absorption**.

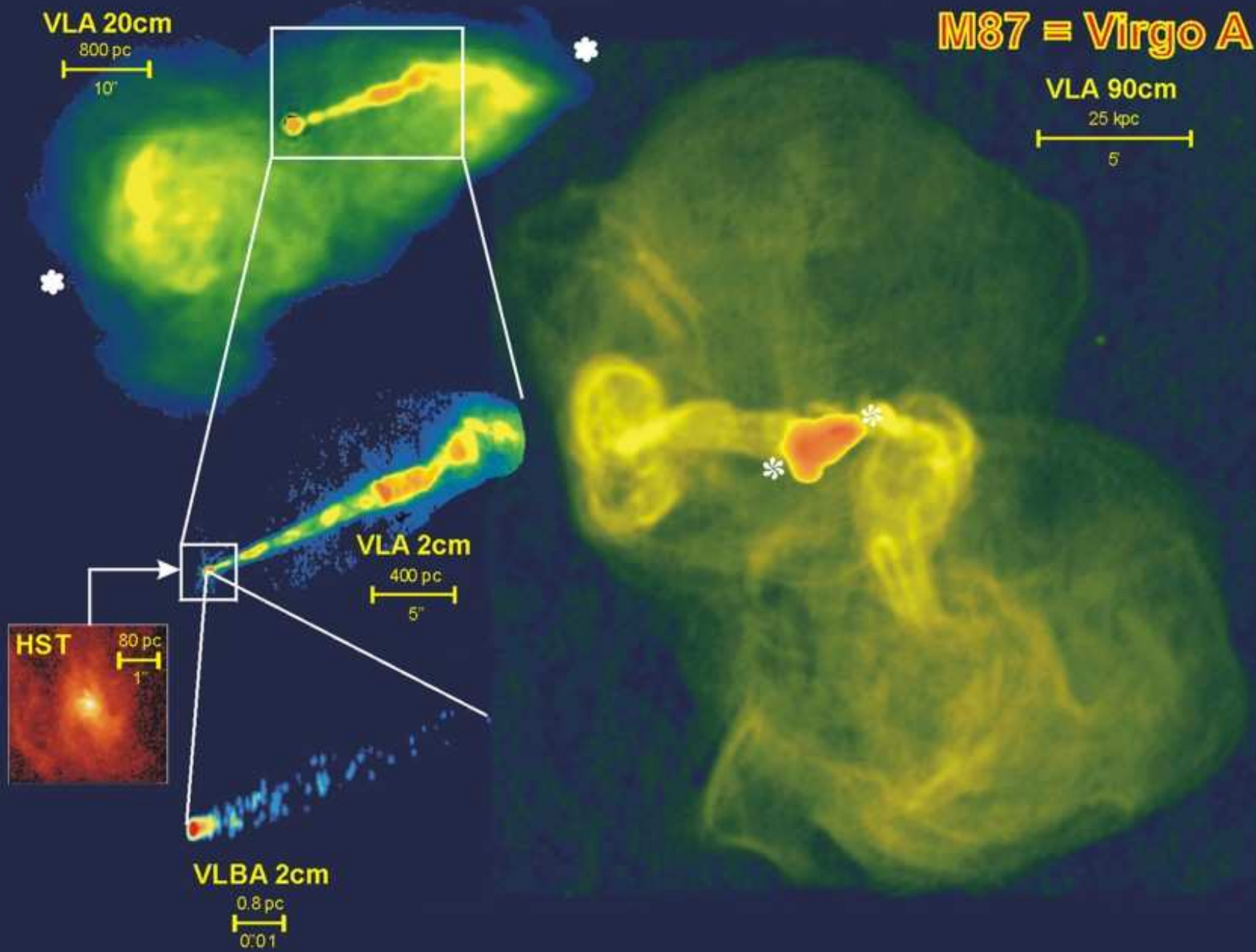
At very high frequencies, additional break due to electron energy losses. The **transition frequency** can be used to measure the strength of the  $B$ -Field. See text-books on radio astronomy.

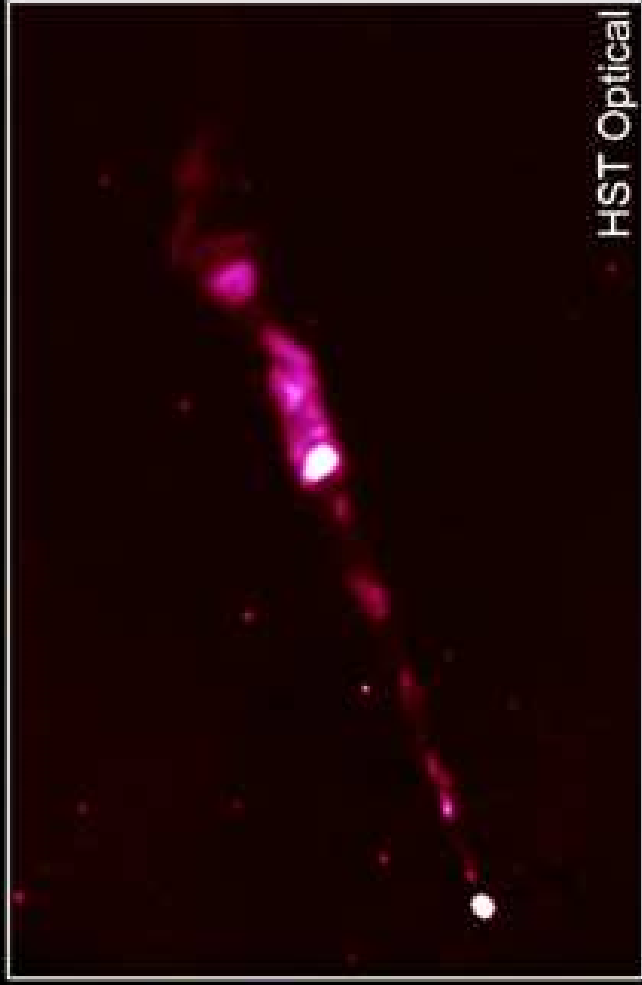
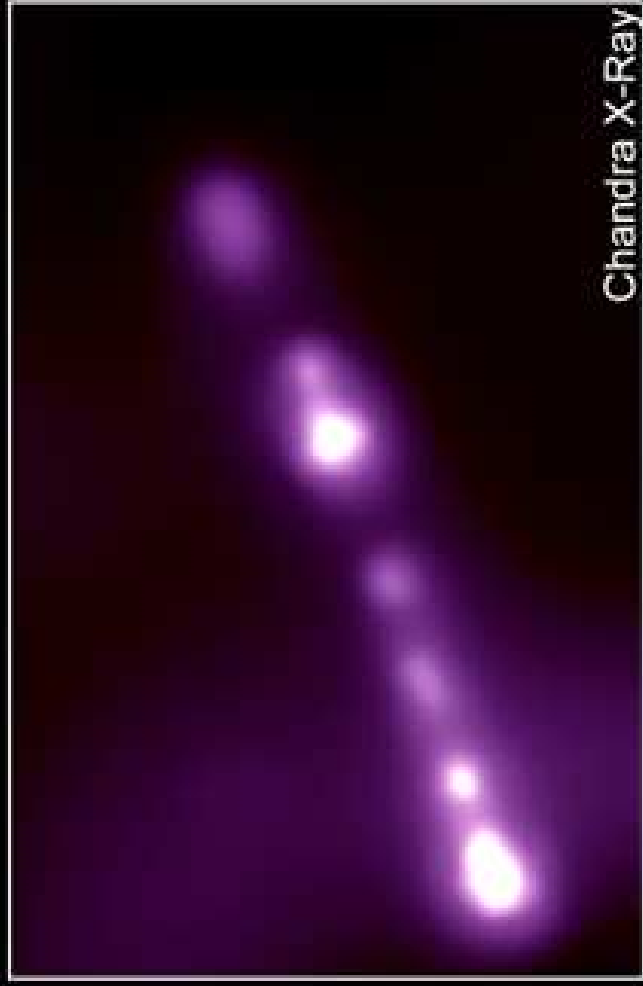
The M87 Jet



Hubble  
Heritage

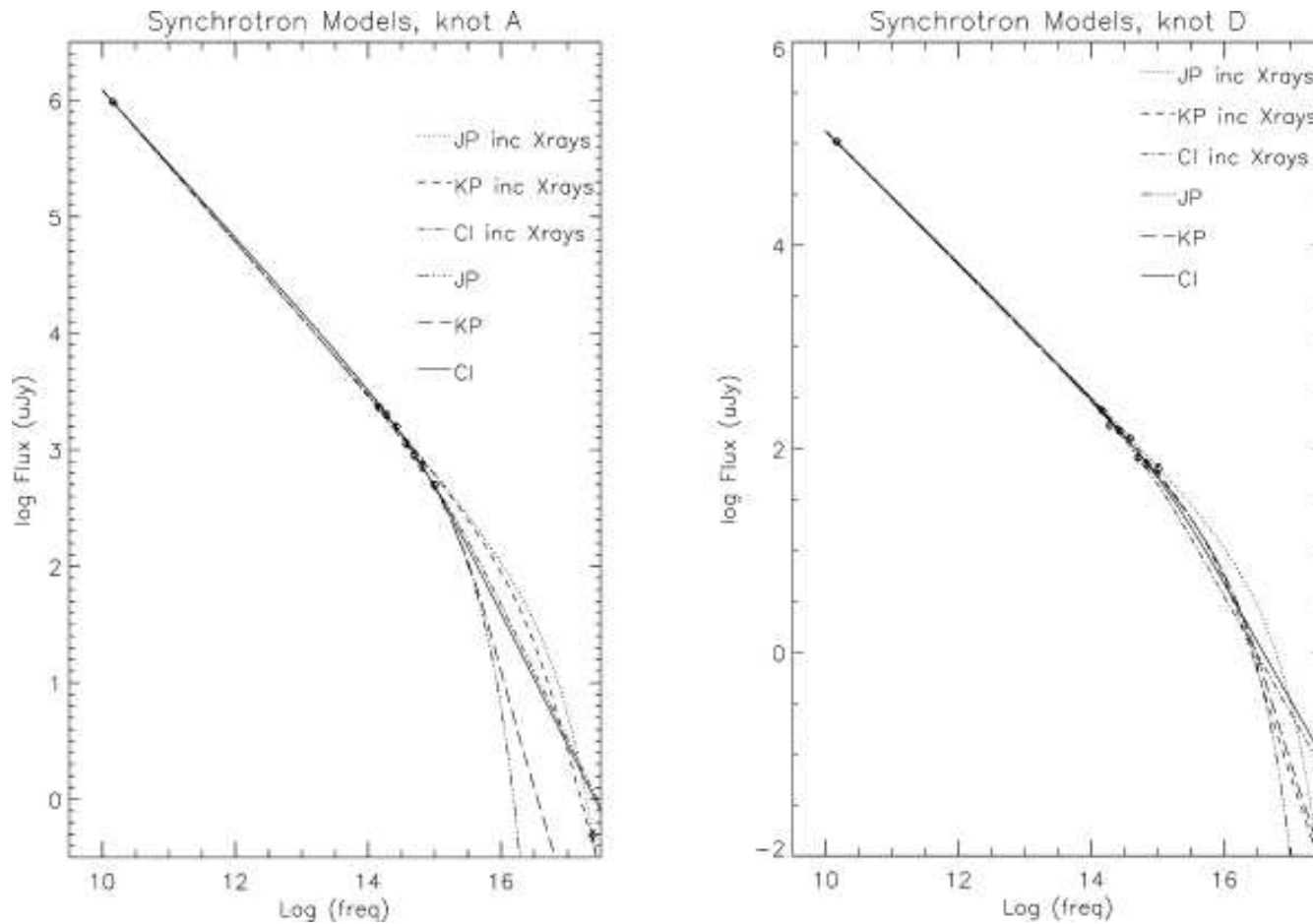








# Jet Spectrum



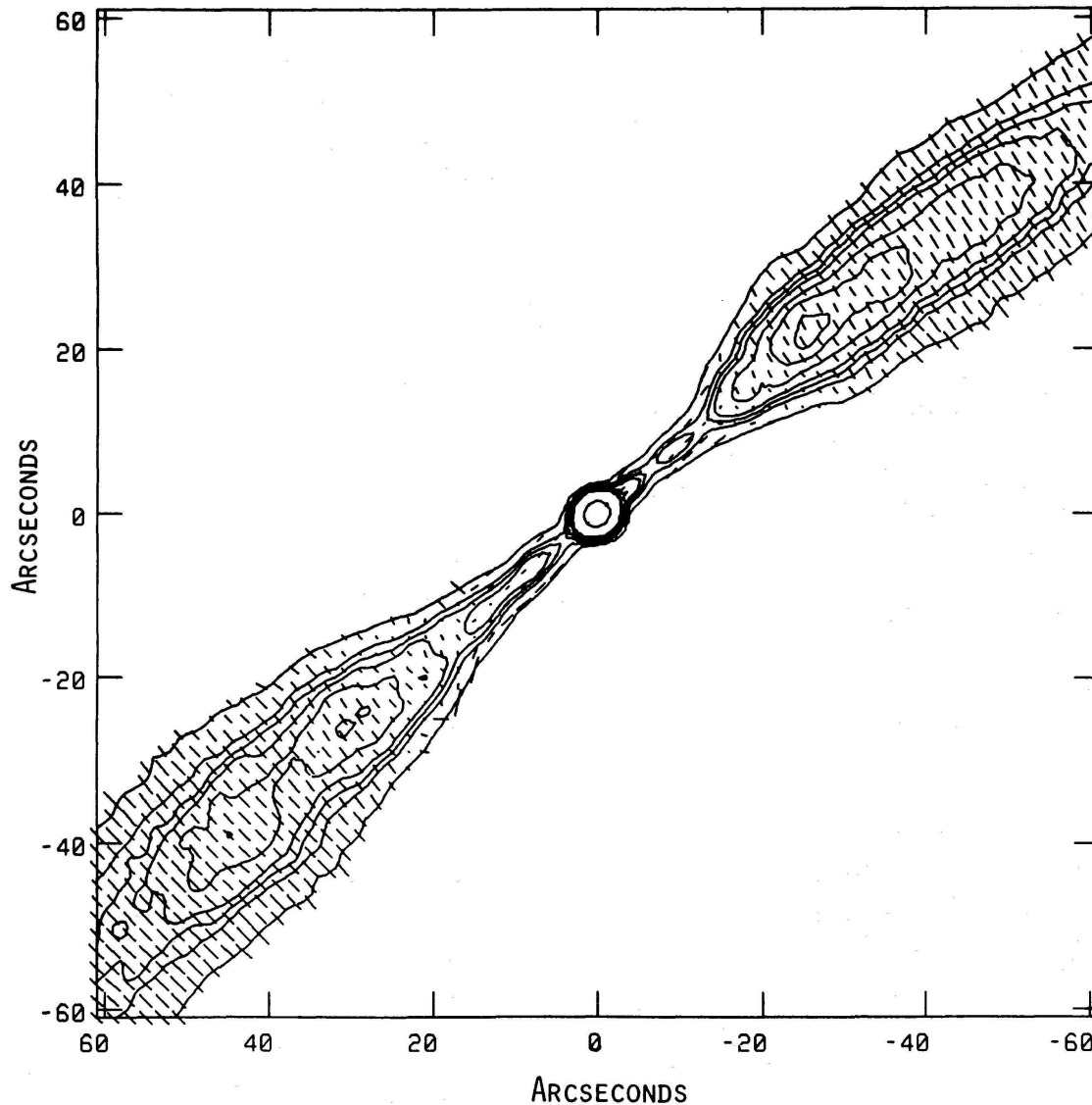
(M87; Perlman et al., 2002)

Spectral shape of jet emission is a power law  $\implies$  **synchrotron radiation**

Typical power law index:  $\alpha \sim 0.65$  between radio and optical.



## Jet Polarization



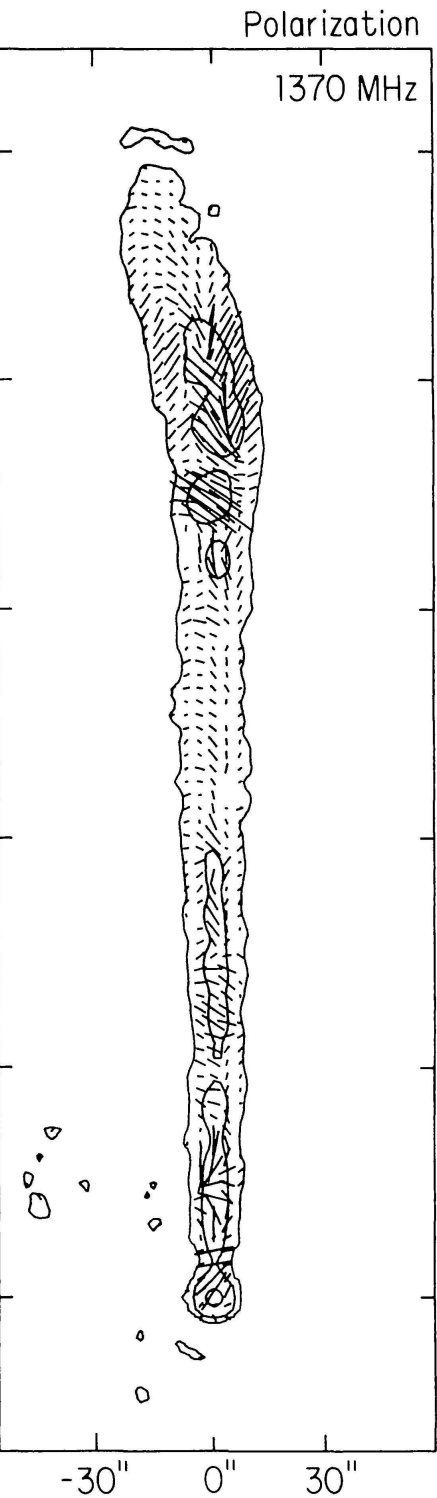
polarization in two-sided jet sources (FR 1): up to 40%

$B$ -field orientation:

- close to core:  $B \parallel$  jet axis
- away from core ( $\sim 10\%$  jet length):  $B \perp$  jet axis

$B$ -field can change orientation again in knots

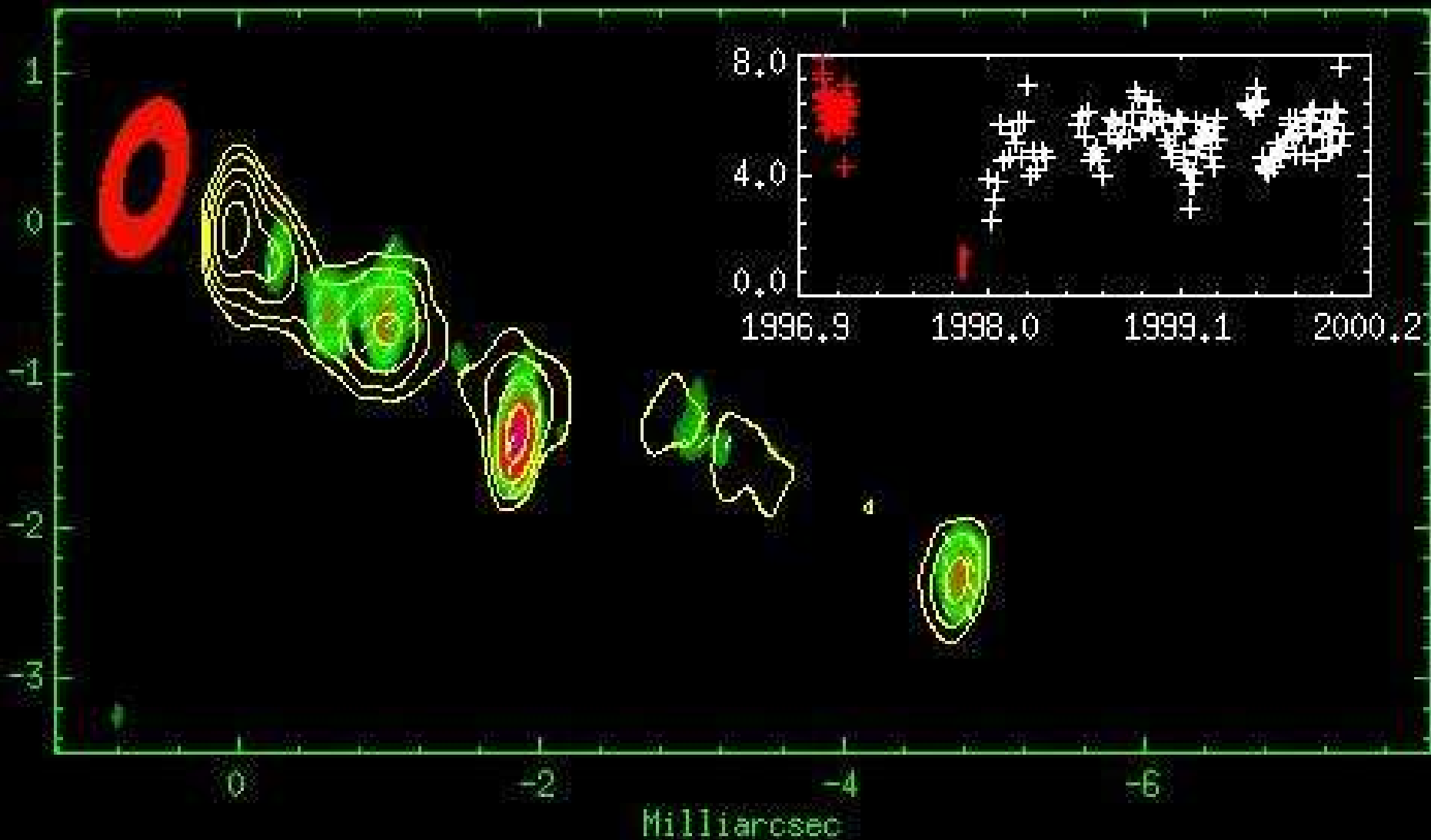
( $B$ -field configuration in IC 4296; Killeen, Bicknell & Ekers, 1986, Fig. 25b)



polarization in one-sided jet sources (FR 2): similar to FR 1, i.e., 40% and higher

*B*-field orientation in FR 2: parallel to jet axis throughout the jet

(*E*-field configuration in NGC 6251, note: *B*-field is perpendicular to *E*-field!; Perley, Bridle & Willis, 1984, Fig. 17)



Jet motion in 3C120 (Marscher et al., 2002)

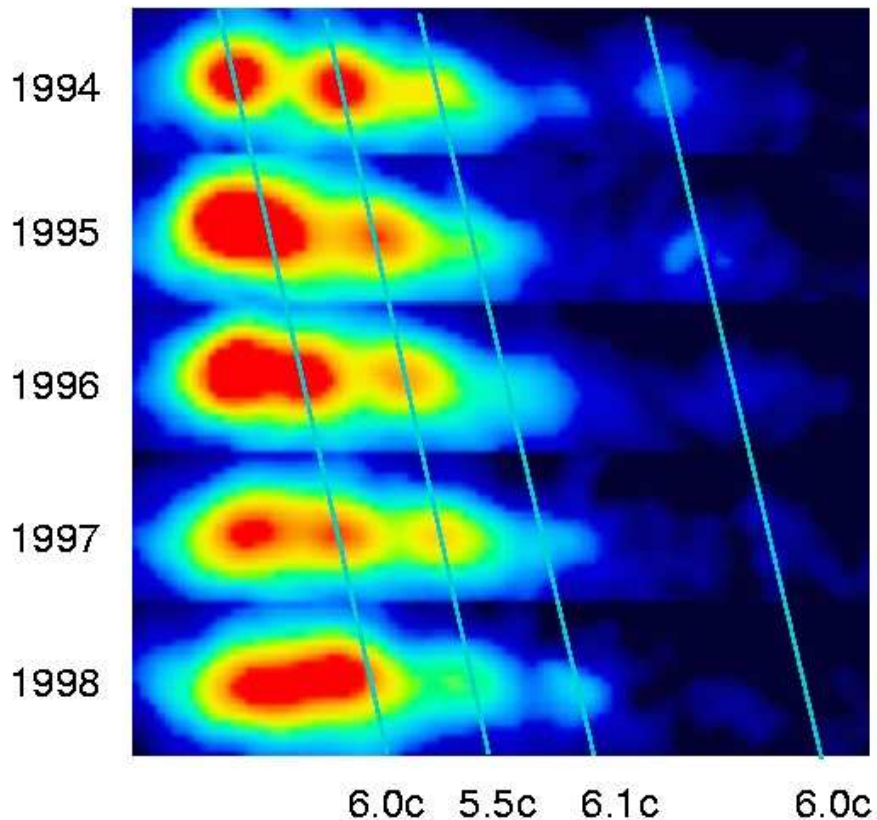
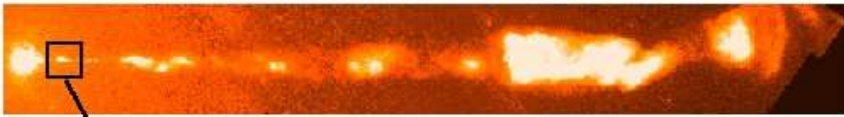
3C120: Sy 1,  $M_{\text{BH}} = 3 \times 10^7 M_{\odot}$  from reverberation mapping

MOVIE TIME: [jetmovies/3c120rx.avi](#)



## Superluminal Motion, II

Superluminal Motion in the M87 Jet



3C120: Apparent speed of jet:  $\sim 5c$

M87: Apparent speed of jet:  $\sim 6c$

**Superluminal motion:** The apparent velocities measured in many AGN jets are  $v > c$ .

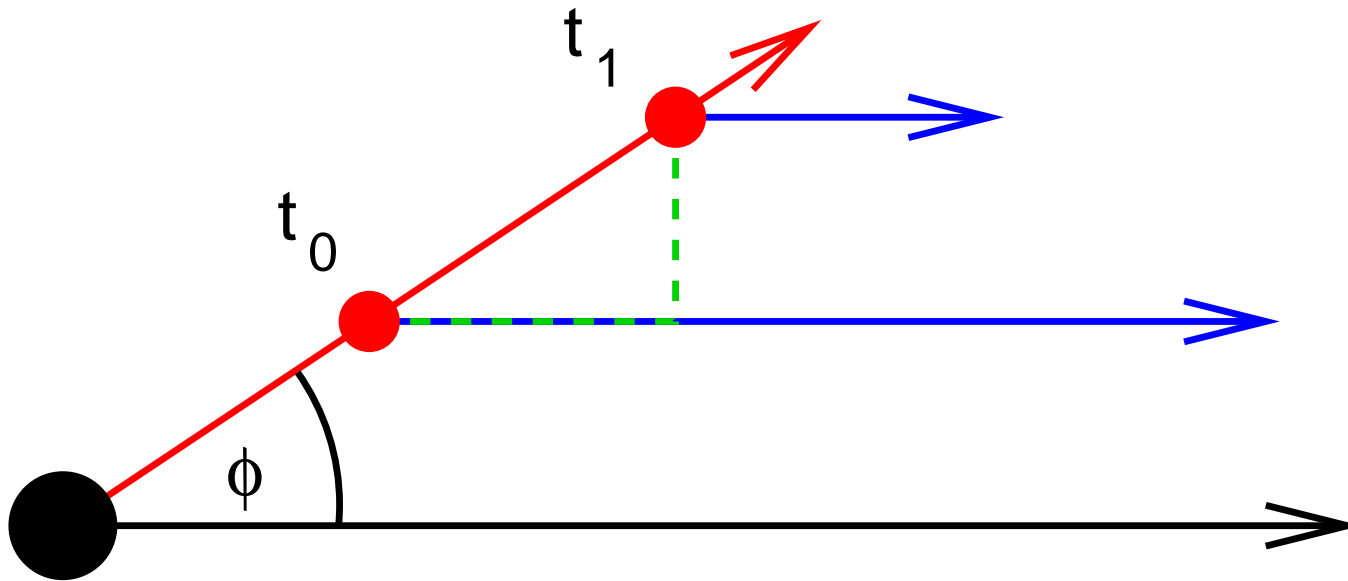
First discovered in 1971 in 3C273.

Biretta/STScI





## Superluminal Motion, III



Consider blob moving towards us with speed  $v$  and angle  $\phi$  with respect to line of sight, emitting light signals at  $t_0$  and  $t_1 = t_0 + \Delta t_e$

**Light travel time:** Observer sees signals separated by

$$\Delta t_o = \Delta t_e - \Delta t_e \frac{v}{c} \cos \phi = \left(1 - \frac{v}{c} \cos \phi\right) \Delta t_e \quad (10.36)$$

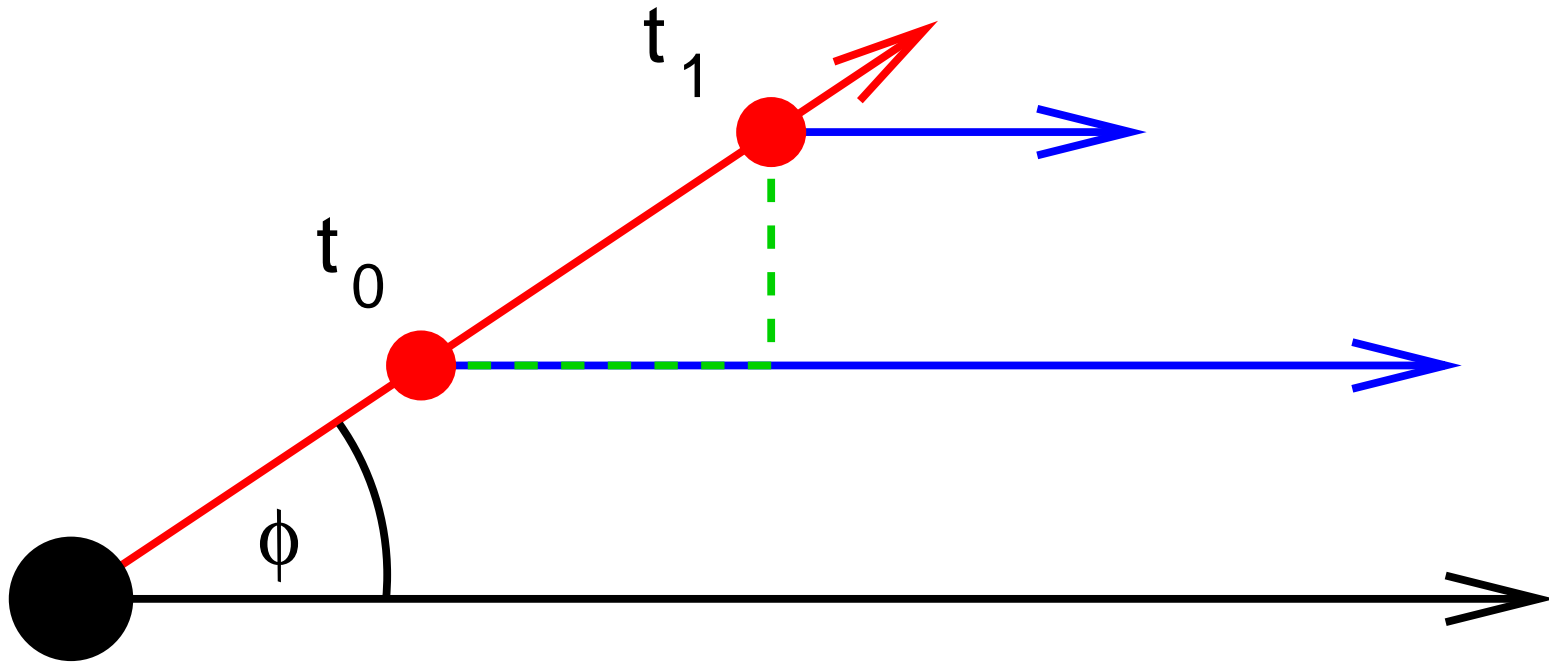
**Observed distance** traveled in plane of sky:

$$\Delta \ell_{\perp} = v \Delta t_e \sin \phi \quad (10.37)$$





## Superluminal Motion, IV



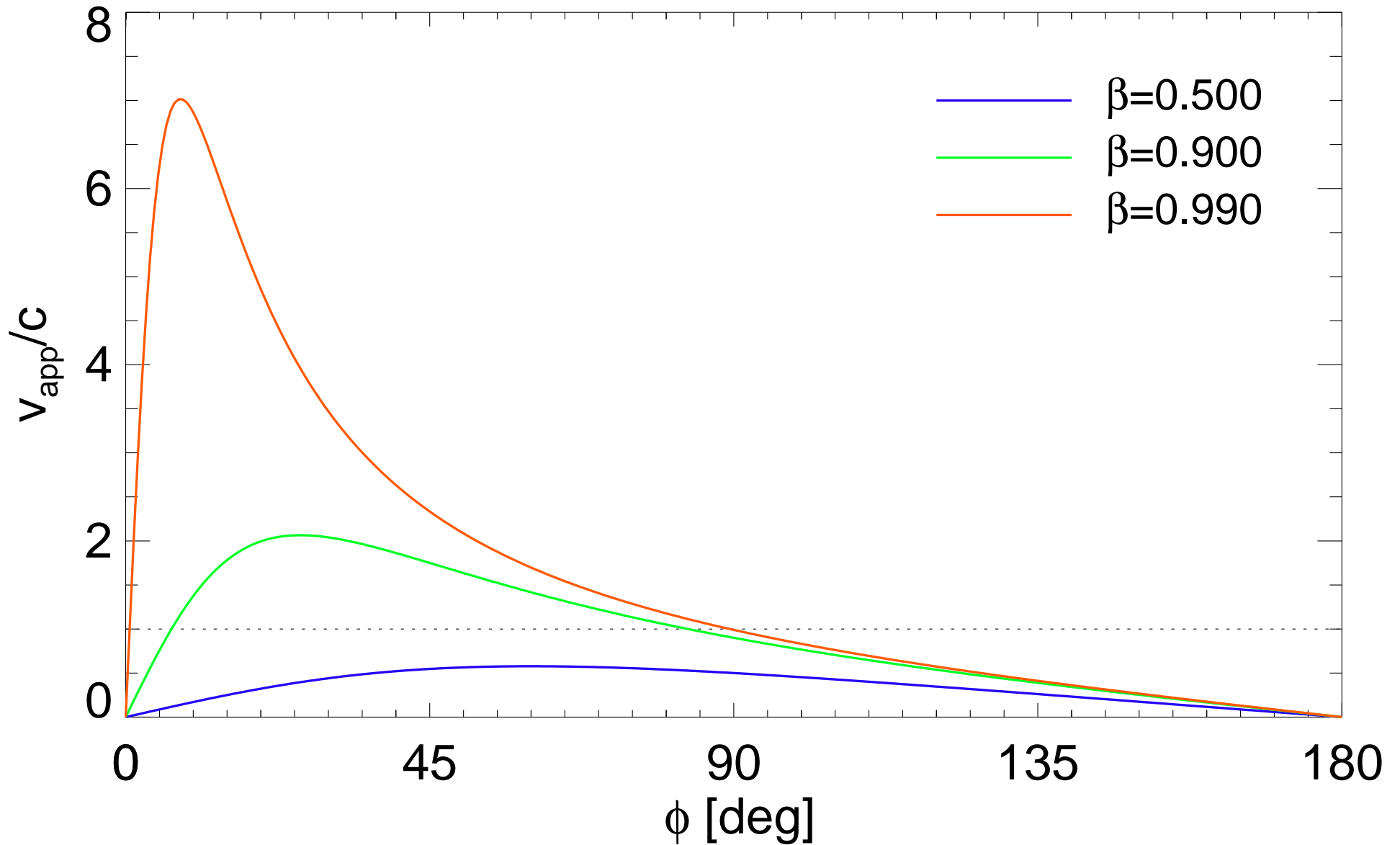
Apparent velocity deduced from observations:

$$v_{\text{app}} = \frac{\Delta l_{\perp}}{\Delta t_o} = \frac{v \Delta t_e \sin \phi}{\left(1 - \frac{v}{c} \cos \phi\right) \Delta t_e} = \frac{v \sin \phi}{\left(1 - \frac{v}{c} \cos \phi\right)} \quad (10.38)$$

$\Rightarrow$  For  $v/c$  large and  $\phi$  small:  $v_{\text{app}} > c$



## Superluminal Motion, V





## A relativistic invariant, I

So, if  $\phi$  is known, we can determine real speed.

In order to determine  $\phi$ , we have to make use of **an useful relativistic invariant**:

$$\frac{I_{\text{nu}}}{\nu^3} = \text{const.} \quad (10.39)$$

in all frames of reference.

*Proof:* The **number of photons with momentum in interval  $\mathbf{p}, \mathbf{p} + d^3$**  is given by

$$dN = 2n \left( \frac{V d^3p}{h^3} \right) \quad (10.40)$$

where  $n$ : photon number,  $V d^3p$ : phase volume,  $h^3$ : volume of phase space cell.

$\implies$  **Energy flowing through volume element  $d^3x = dA(c dt)$ :**

$$dE = h\nu dN = 2nh\nu dA(c dt) \left( \frac{d^3p}{h^3} \right) \quad (10.41)$$



## A relativistic invariant, II

Since  $p = h\nu/c$ :

$$d^3p = p^2 dp d\Omega = \left(\frac{h\nu}{c}\right)^2 h \frac{d\nu}{c} d\Omega = \left(\frac{h}{c}\right)^3 \nu^2 d\nu d\Omega \quad (10.42)$$

Therefore

$$dE = 2nh\nu c dA dt \left(\frac{d^3p}{h^3}\right) = \frac{2h\nu^3}{c^2} n dA dt d\Omega d\nu \quad (10.43)$$

or

$$\frac{dE}{dA dt d\Omega d\nu} = I = \frac{2h\nu^3}{c^2} n \quad (10.44)$$

Therefore

$$\frac{I}{\nu^3} = \frac{2h}{c^2} n \quad (10.45)$$

and since  $n$  is just a number,  $I/\nu^3$  is Lorentz-invariant.



## Relativistic Aberration

Relativistic invariance:  $I_\nu/\nu^3 = \text{const.}$  where  $I_\nu$  is the intensity.

Therefore, **observed intensity of a moving blob**:

$$\frac{I(\nu_{\text{obs}})}{\nu_{\text{obs}}^3} = \frac{I(\nu_{\text{em}})}{\nu_{\text{em}}^3} \quad (10.46)$$

Because of the **relativistic Doppler effect**:

$$\nu_{\text{obs}} = \frac{\nu_{\text{em}}}{\gamma(1 - \beta \cos \phi)} \quad (10.47)$$

( $\beta = v/c$ ) and thus

$$I(\nu_{\text{obs}}) = \nu_{\text{obs}}^3 \frac{I(\nu_{\text{em}})}{\nu_{\text{em}}^3} = \frac{I(\nu_{\text{em}})}{(\gamma(1 - \beta \cos \phi))^3} \quad (10.48)$$

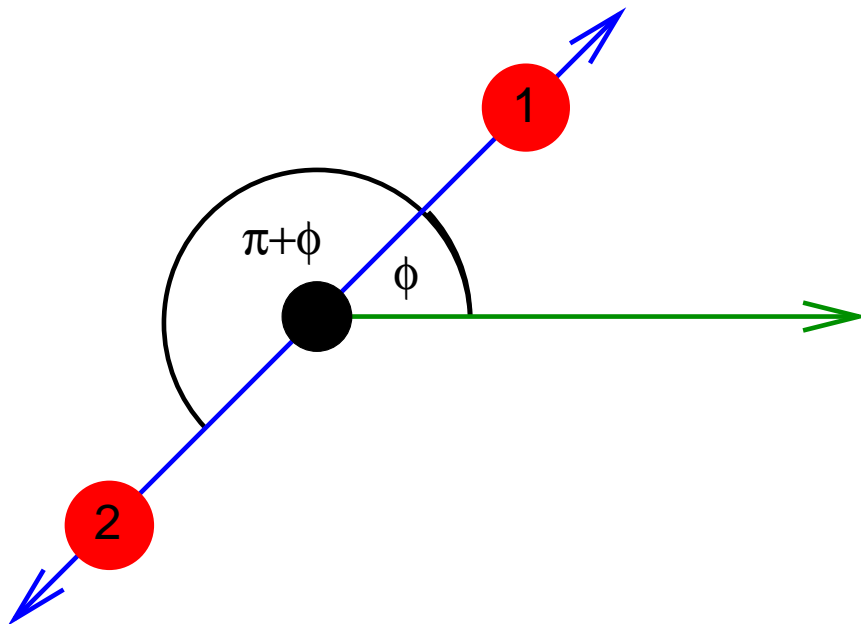
Specifically, for a **blob with a power law spectrum**:

$$I(\nu_{\text{obs}}) = \frac{A\nu_{\text{em}}^{-\alpha}}{(\gamma(1 - \beta \cos \phi))^3} = \frac{A(\gamma(1 - \beta \cos \phi))^{-\alpha} \nu_{\text{obs}}^{-\alpha}}{(\gamma(1 - \beta \cos \phi))^3} = \frac{A\nu_{\text{obs}}^{-\alpha}}{(\gamma(1 - \beta \cos \phi))^{3+\alpha}} \quad (10.49)$$

(where  $A$  is the normalization constant of the power law).



## Relativistic Aberration



Now take a source emitting blobs symmetrically in two directions.

From Eq. (10.49) the ratio of fluxes from the blobs is

$$\frac{F_1}{F_2} = \left( \frac{1 + \beta \cos \phi}{1 - \beta \cos \phi} \right)^{3+\alpha} \quad (10.50)$$

Radiation from a blob moving towards observer is strongly boosted.

Jet can be expressed as a series of blobs. But the number of blobs observed scales as  $(\gamma(1 - v \cos \phi))^{-1}$ , such that for jets:

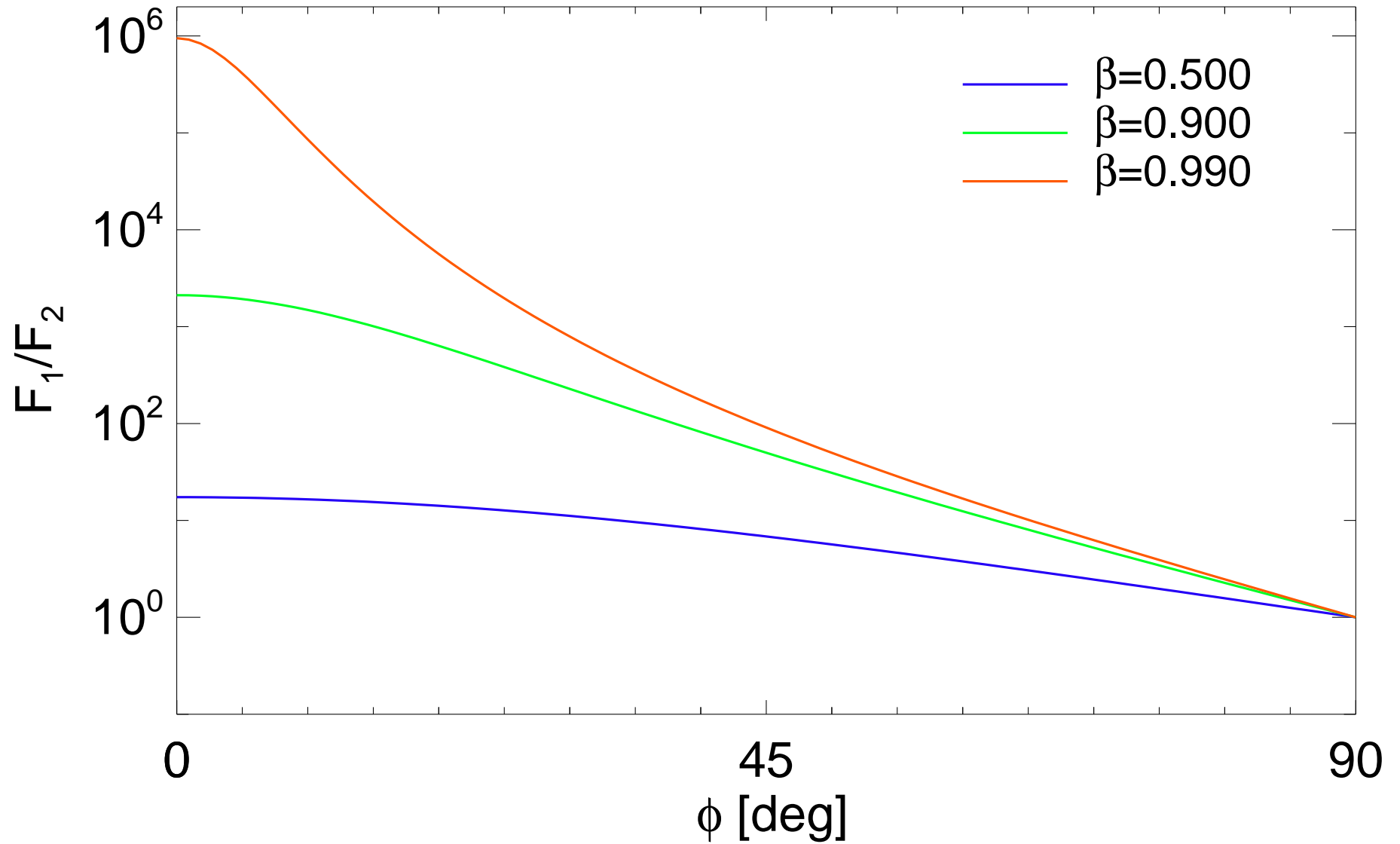
$$\frac{F_1}{F_2} = \left( \frac{1 + \beta \cos \phi}{1 - \beta \cos \phi} \right)^{2+\alpha} \quad (10.51)$$

One sidedness of jets is a relativistic effect.

From measuring  $F_1/F_2$ , we can in principle determine  $\phi$ .



# Relativistic Aberration



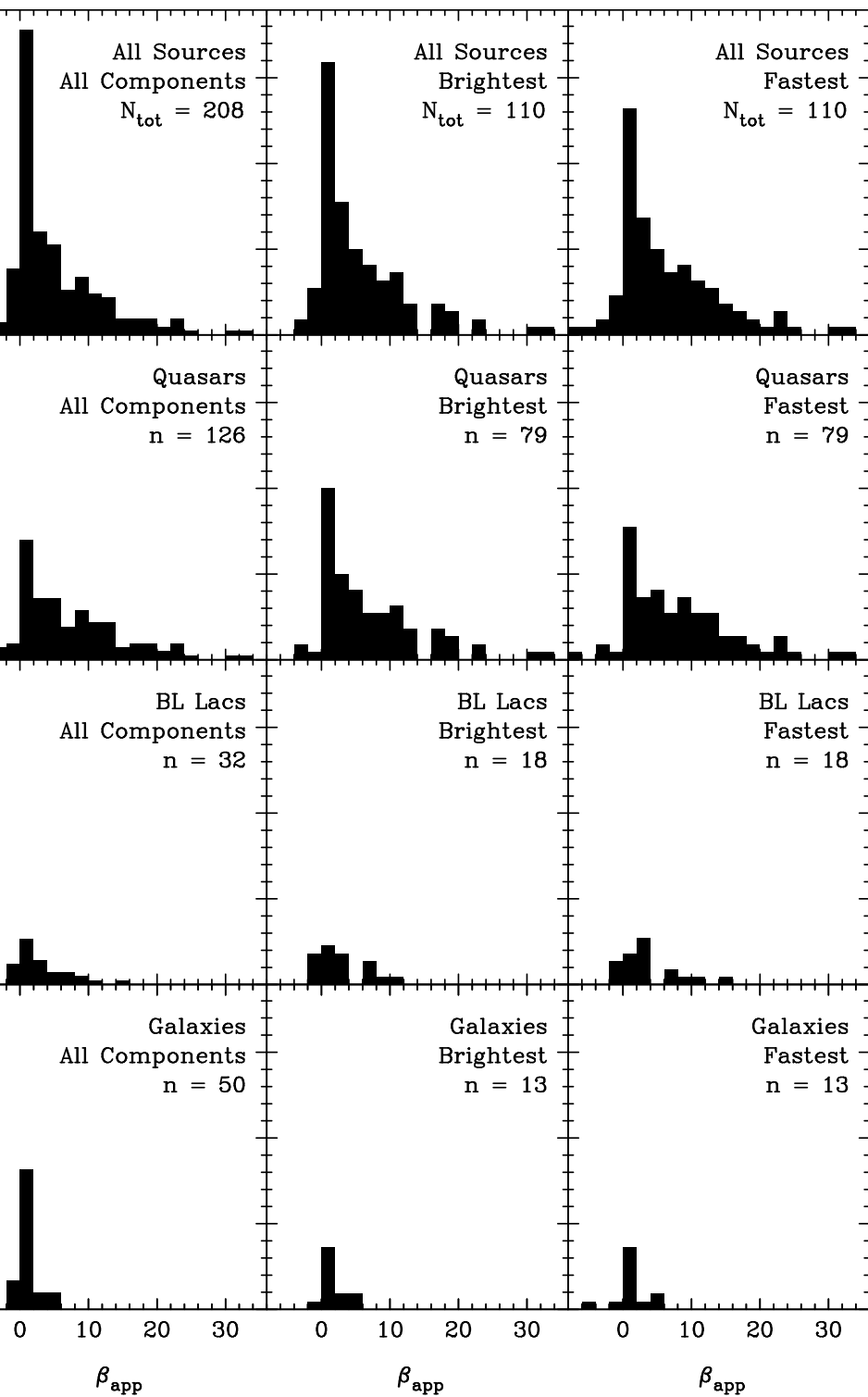


## Jet Statistics, I

Kellermann et al. (2004): **Largest survey of jets performed so far.**

- Wavelength 2 cm (15 GHz)
- All AGN with flat spectra ( $\alpha < 0.5$  for  $S_\nu \propto \nu^{-\alpha}$ ) and fluxes above 1.5 Jy at 15 GHz
- Survey started in 1994, ended in 2001, typically 7 observations per source
- 208 features in 110 AGN (Seyfert, BL Lac, Quasars).
- movies and images at <http://www.nrao.edu/2cmsurvey> (recommended!)





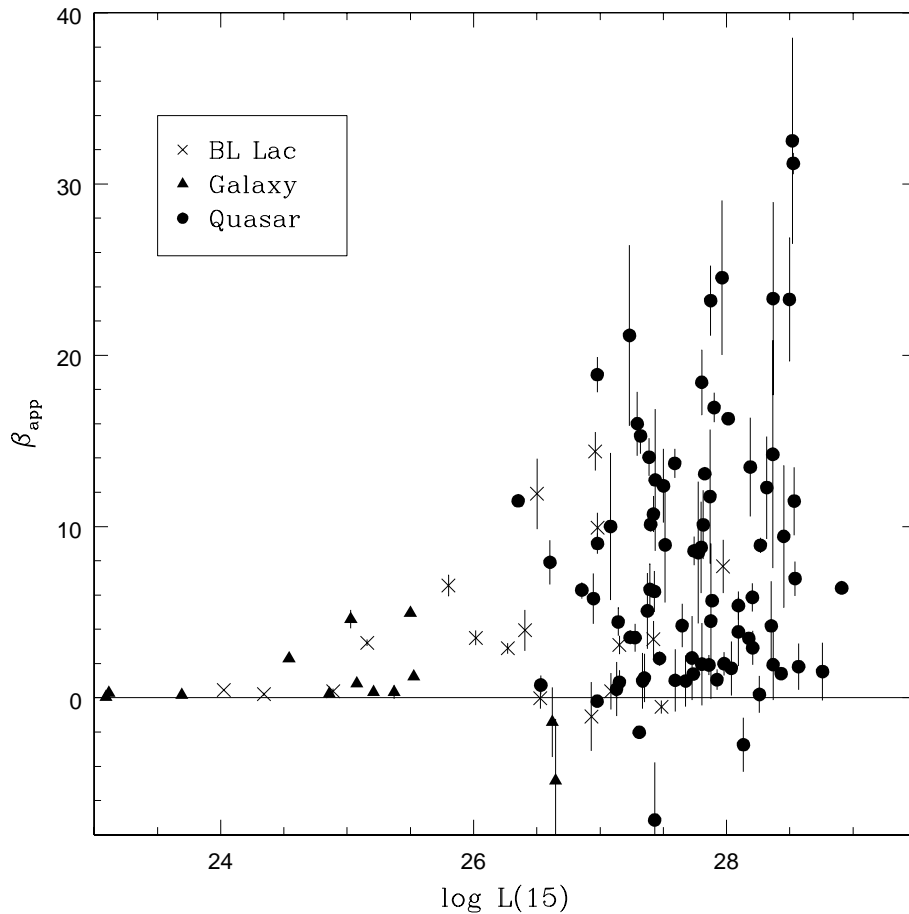
### Distribution of observed velocities:

- **apparent velocity range:**  $\beta \leq 15$
- **Quasars:** tail up to  $\beta \sim 34$
- **others:** mainly  $\beta \lesssim 6$

(Kellermann et al., 2004, Fig. 4)



## Jet Statistics, III



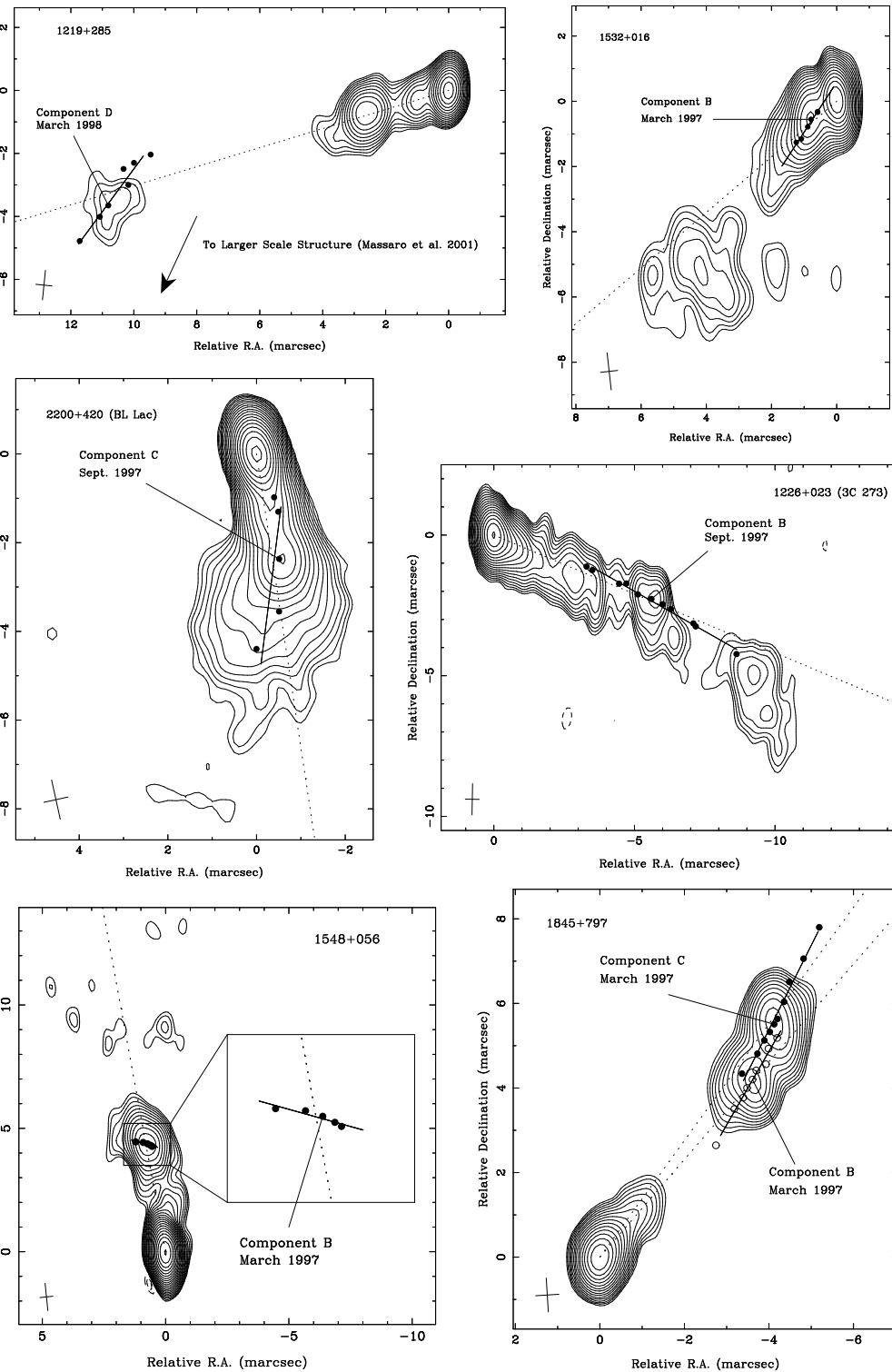
(Kellermann et al., 2004, Fig. 6)

Relation between  $\beta$  and luminosity:  
larger scatter at higher  $L$

This does *not* mean that lower  $L$  sources have lower speeds, since observational effects also play a role:

sample is flux limited

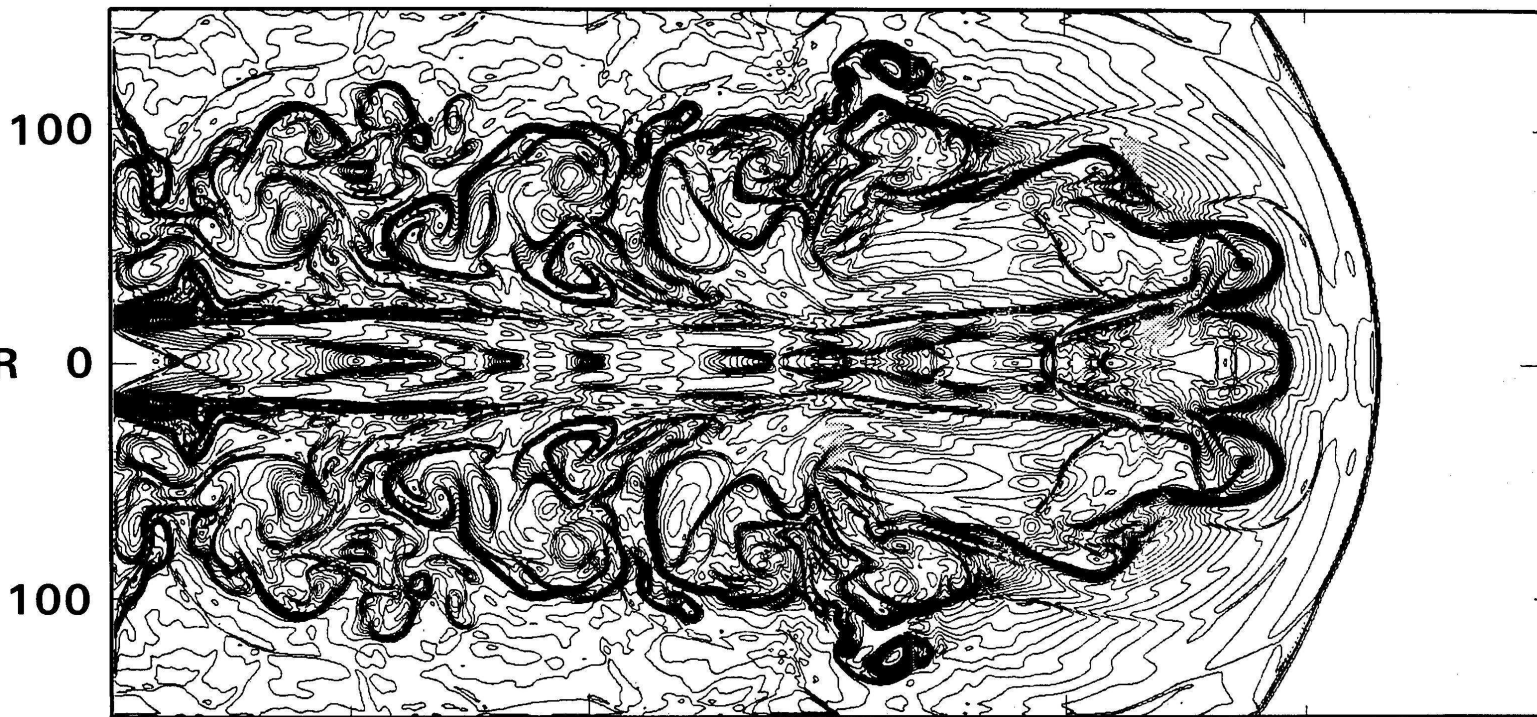
- ⇒ faintest sources are close, and probably represent the most normal sources
- ⇒ probability that high Lorentz factor jets point in our direction grows with sampled volume, so perhaps the distribution is a selection effect.



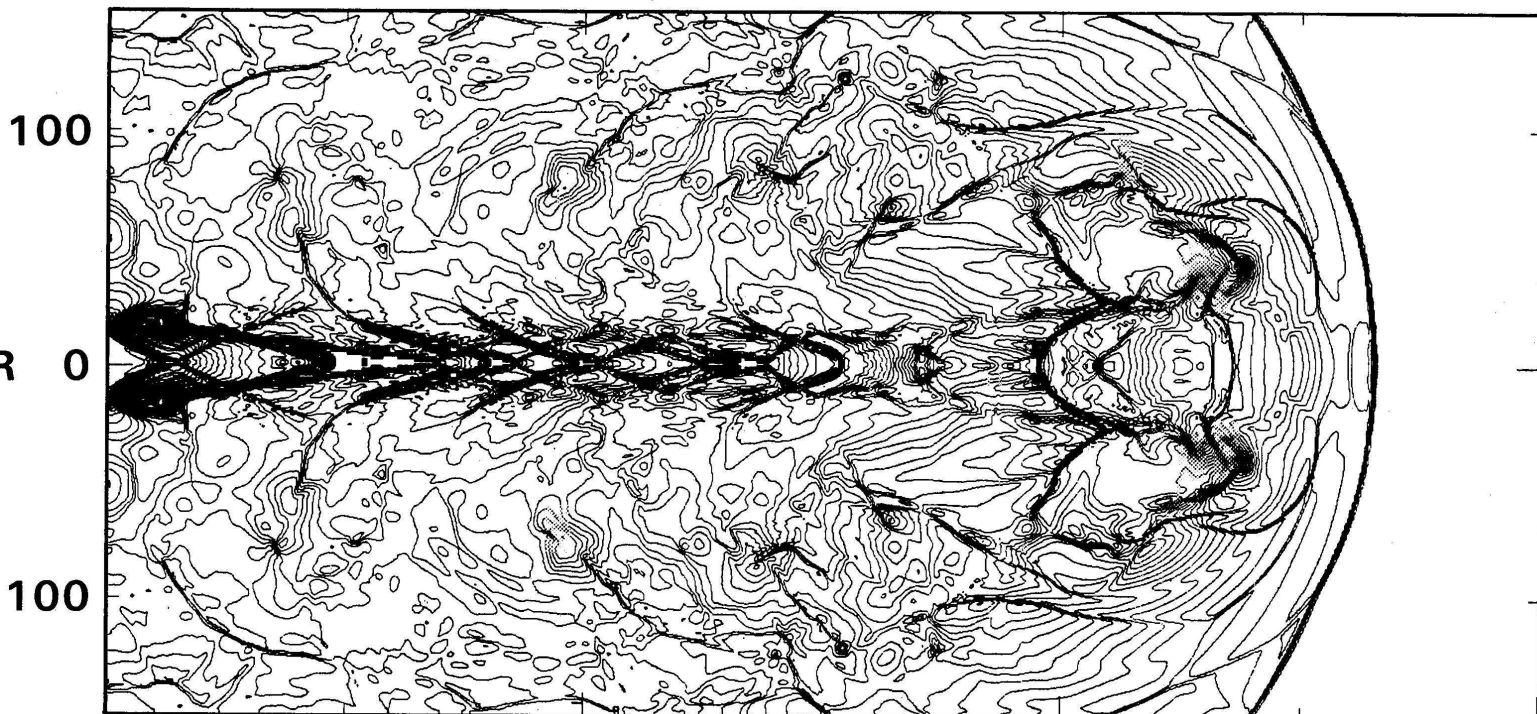
In many sources, **bent trajectories** are observed, which **do not follow jet axis**

- ⇒ **do blobs follow pre-existing channel?**
- ⇒ **nonballistic motion?**
- ⇒ **difference between bulk motion and pattern motion?**

(Kellermann et al., 2004, Fig. 7)



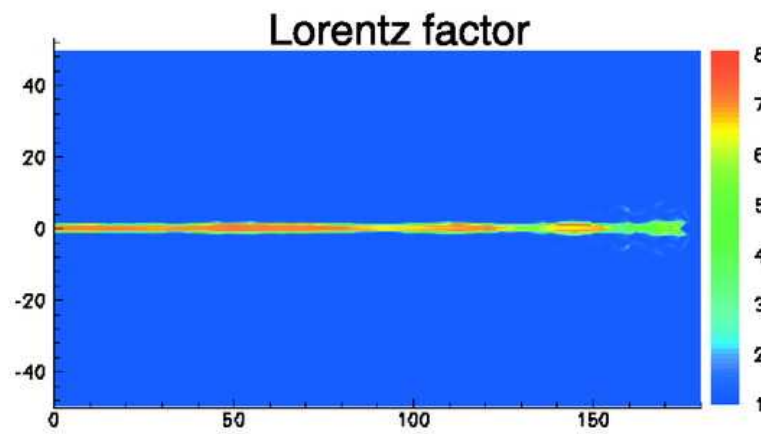
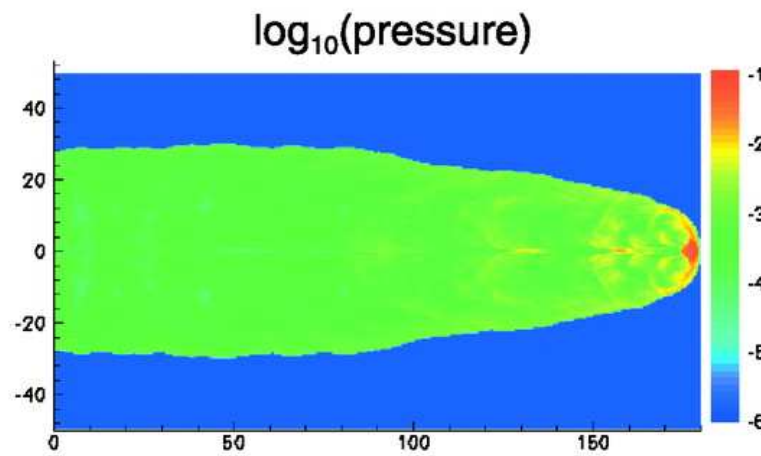
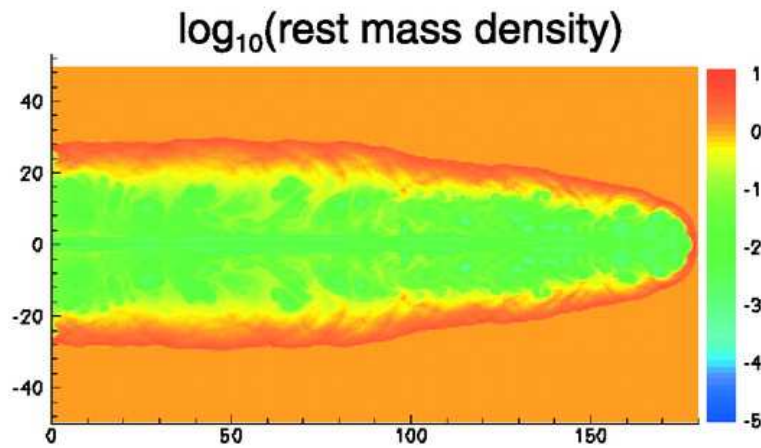
Jet propagation is  
very difficult  
hydrodynamics:  
generally solved  
numerically



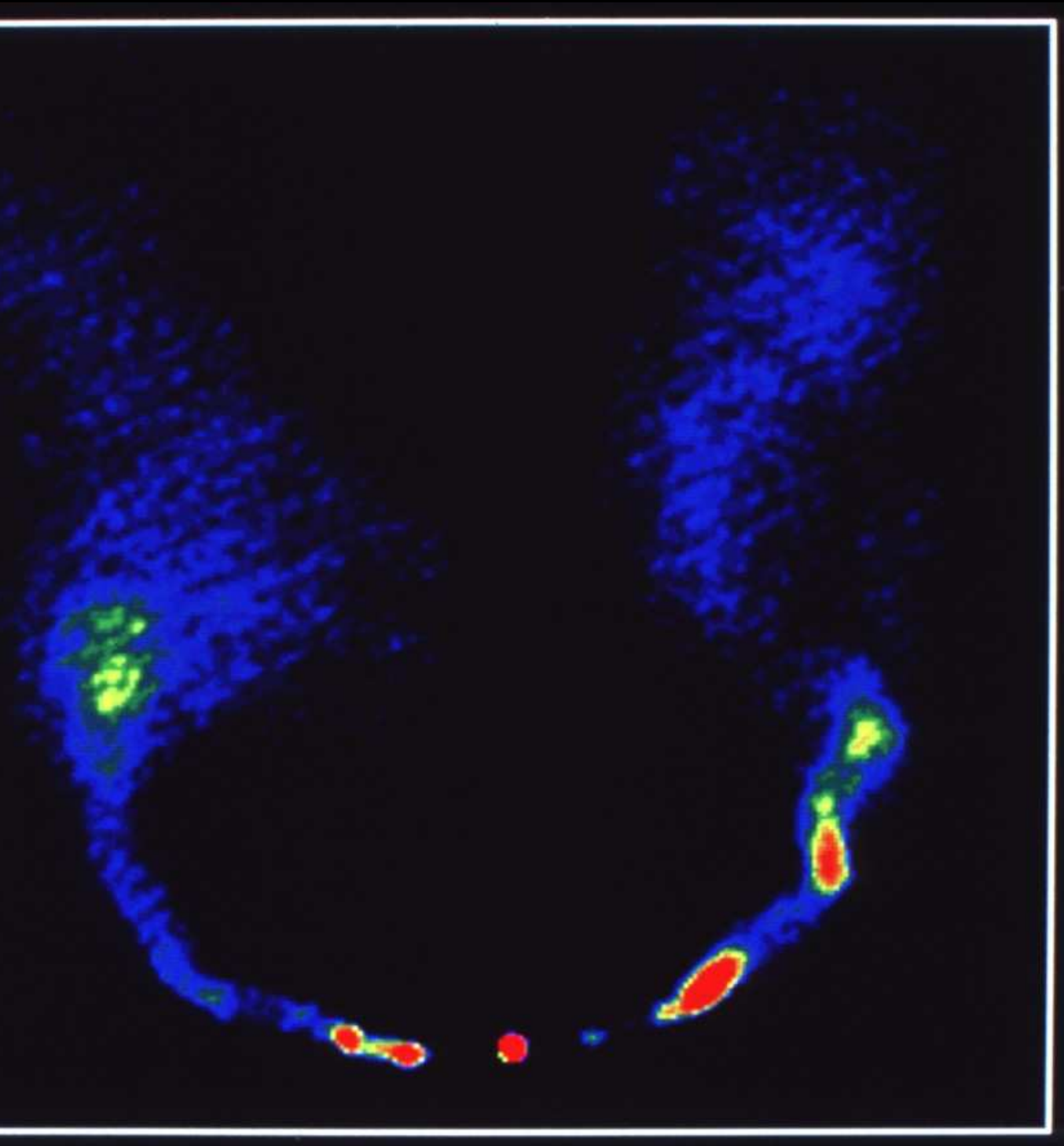
Numerical simulation  
of a Mach=6 jet (Top:  
density, bottom:  
pressure Lind et al.,  
1989).

Turbulent structure  
due to  
Kelvin-Helmholtz  
instability  
(hydrodynamical  
instability in shear  
flows)





(Mizuta, Yamada & Takabe, 2004)



NGC 1265: radio galaxy  
in Perseus cluster,  
moving with  
 $2000 \text{ km s}^{-1}$  through  
intergalactic medium.

(NRAO/AUI; O'dea & Owen,  
1986)

Declination (1950.0)

NGC 1265

1418 MHz

30"

41° 41' 00"

30"

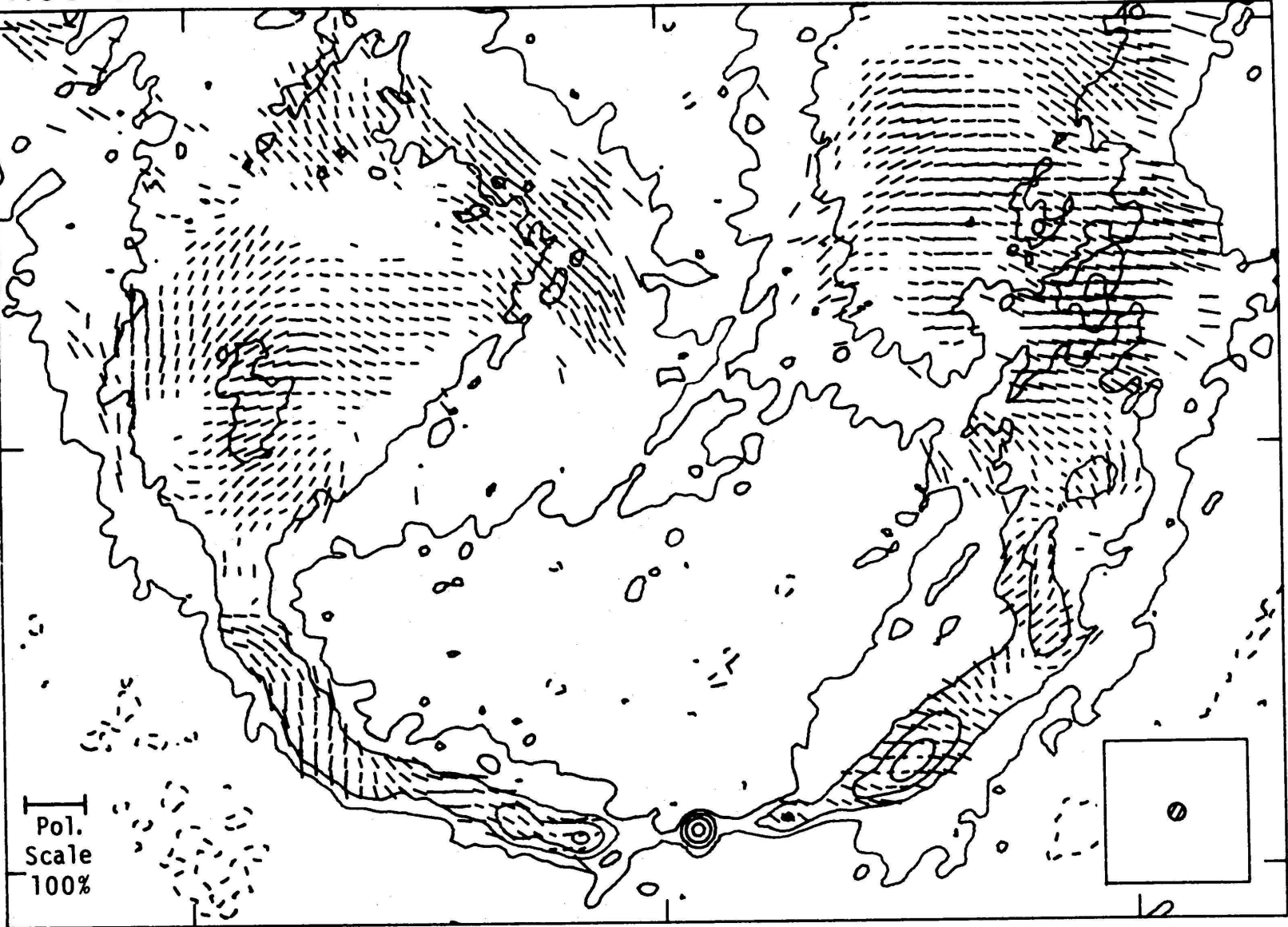
Pol.  
Scale  
100%

03<sup>h</sup> 15<sup>m</sup> 00<sup>s</sup>

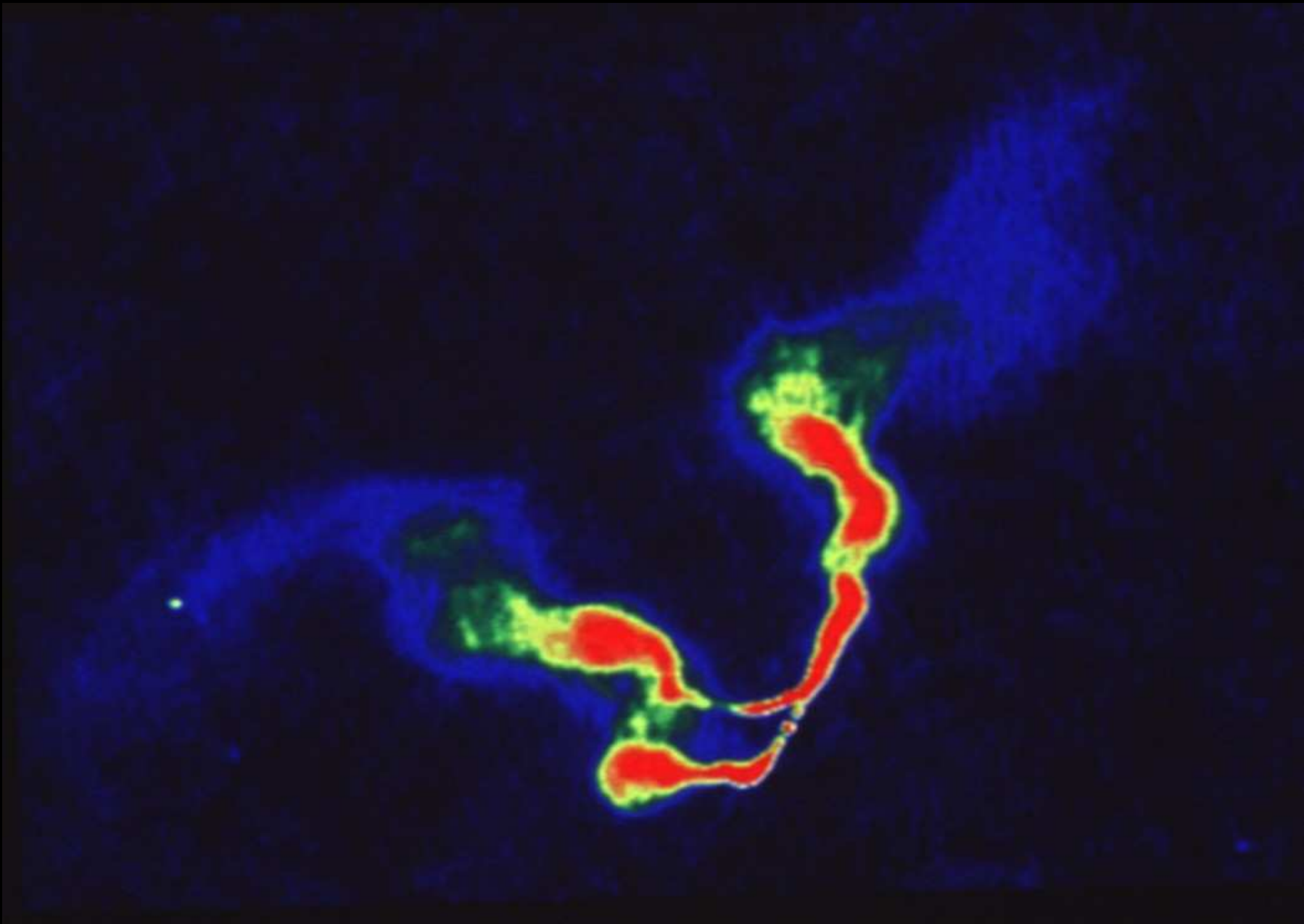
57<sup>s</sup>

54<sup>s</sup>

Right Ascension (1950.0)



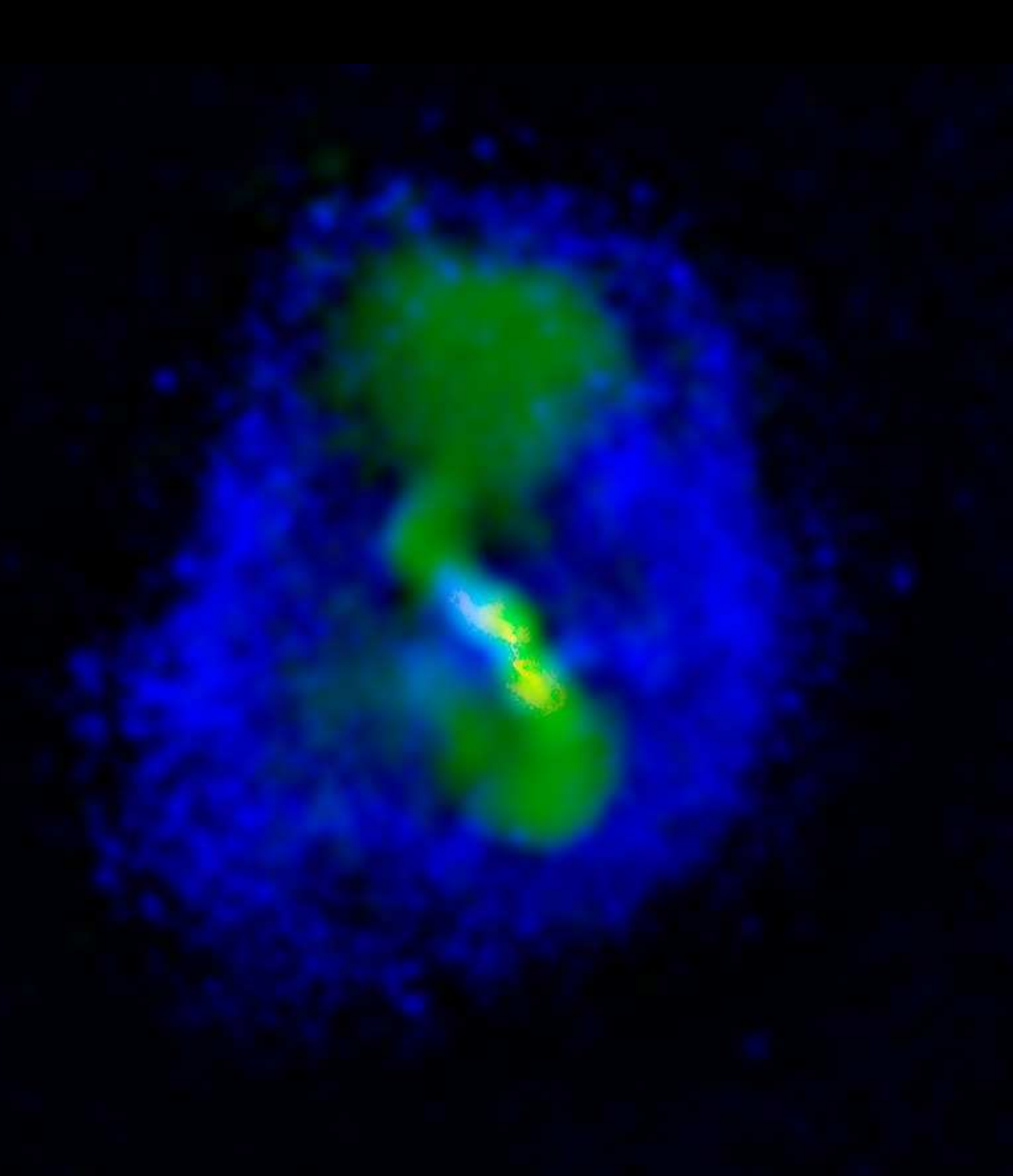
*E*-field structure of NGC 1265 (O'dea & Owen, 1986)



(NRAO/AUI/Owen et al.)

3C75 in Abell 400 at  $\lambda = 20$  cm: twin radio jets from double core.





Hydra A: Multiple  
cavities drifting  
outwards through the  
intergalactic medium.  
Cavity system created  
in the past

200–500 Myears

green: radio, blue: X-rays, after  
subtracting elliptical  $\beta$ -model  
for gas distribution.

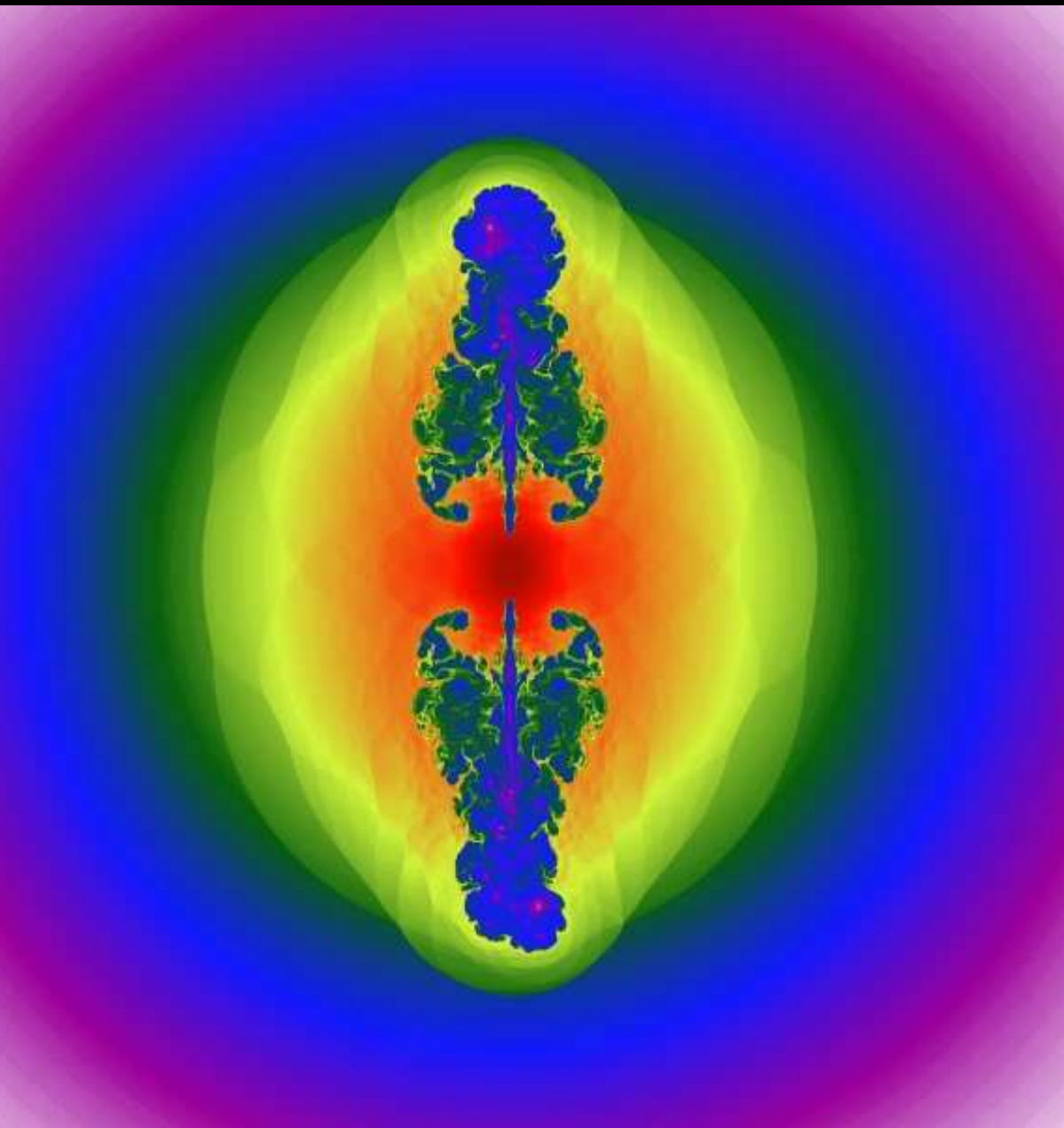
Size scale: outer cavities have  
diameters of 200 and 120 kpc.

(courtesy Mike Wise, UvA,  
astro-ph/0612100)



Formation of jet substructure / cavities  
in MHD simulations of a jet penetrating  
into a cluster gas

courtesy M. Brüggen (IUB) and UKAFF



Global view of  
jet-IGM-interaction and cavity  
formation

courtesy M. Brüggen (IUB) and UKAFF

Movie: [jetmovies/brueggen\\_moviebig2.avi](#)

see Heinz et al., 2006, MNRAS



## Jets and IGM, VII

Radio lobe physics:

**Total energy content** of lobe for a power law distribution of electrons,  $n(E) = n_0 E^{-p}$ :

$$U_e = V \int_{E_1}^{E_2} n(E) E dE = \frac{V n_0}{2-p} \left( E_2^{2-p} - E_1^{2-p} \right) \quad (10.52)$$

Integrating over the synchrotron spectrum (Eq. (10.26)) gives the **total synchrotron luminosity** produced by this electron population:

$$L = \frac{4\sigma_T U_B V n_0}{3m_e^2 c^4} \left( \frac{E_2^{3-p} - E_1^{3-p}}{3-p} \right) \quad (10.53)$$

Using the characteristic frequency

$$\omega_c = \gamma^2 \omega_L = \frac{eB}{m_e c} \left( \frac{E}{m_e c^2} \right)^2 \quad (10.18)$$

$E_1$  and  $E_2$  can be expressed in terms of the frequency band over which the power law is observed,  $\nu_1, \nu_2$ . After some messy calculation one obtains:

$$\frac{U_e}{L} = \frac{A}{B^{3/2}} \quad (10.54)$$

where  $A$  is some constant.



## Jets and IGM, VIII

The **total kinetic energy in particles** is

$$U_{\text{particles}} = aU_e = aAB^{-3/2}L \quad (10.55)$$

where  $a > 1$  (since there are other particles than electrons in the lobe).

Therefore the **total energy of the radio lobe** is

$$U_{\text{tot}} = U_{\text{particles}} + U_B = \frac{aAL}{B^{3/2}} + \frac{VB^2}{8\pi} \quad (10.56)$$

The **minimum of  $U_{\text{tot}}$**  is reached for

$$B_{\text{min}} = \left( \frac{6\pi aAL}{V} \right)^{2/7} \quad (10.57)$$

while the **equipartition  $B$ -field**, for which  $U_{\text{particles}} = U_B$  is

$$B_{\text{eq}} = \left( \frac{8\pi aAL}{V} \right)^{2/7} \quad (10.58)$$

Since the total energy for equipartition is  $1.01U_{\text{min}}$ , one often assumes synchrotron sources are in equipartition.

First noticed by Burbidge (1959).



## Jets and IGM, IX

### Radio lobes:

- Typical luminosity is a few times  $L = 10^{44} \text{ erg s}^{-1}$
- Typical  $B$ -fields are  $\sim 10^{-4} \text{ G}$

Assuming equipartition: typical energy content of a radio lobe:  $E \sim 10^{60} \text{ erg}$

corresponding to  $10^7$  supernovae

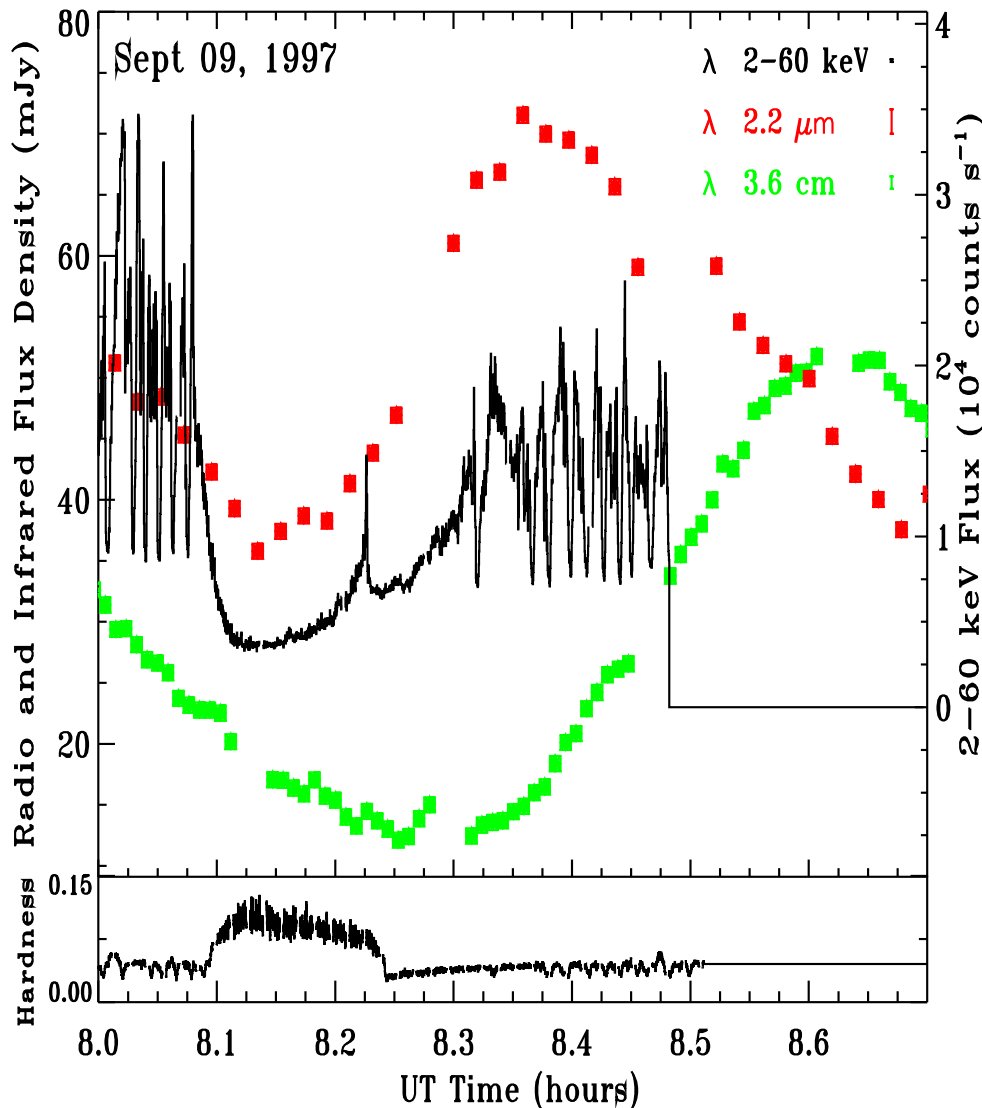
$\implies$  lobe lifetime  $t \sim E/L \sim 10^8 \text{ yr}$

$\implies$  jets and lobes are rather long lived phenomena

Equipartition holds only approximately true for jets and lobes (see, e.g., Heinz & Begelman 1997).



## Jet Formation



(GRS 1915+105; Mirabel et al., 1998)

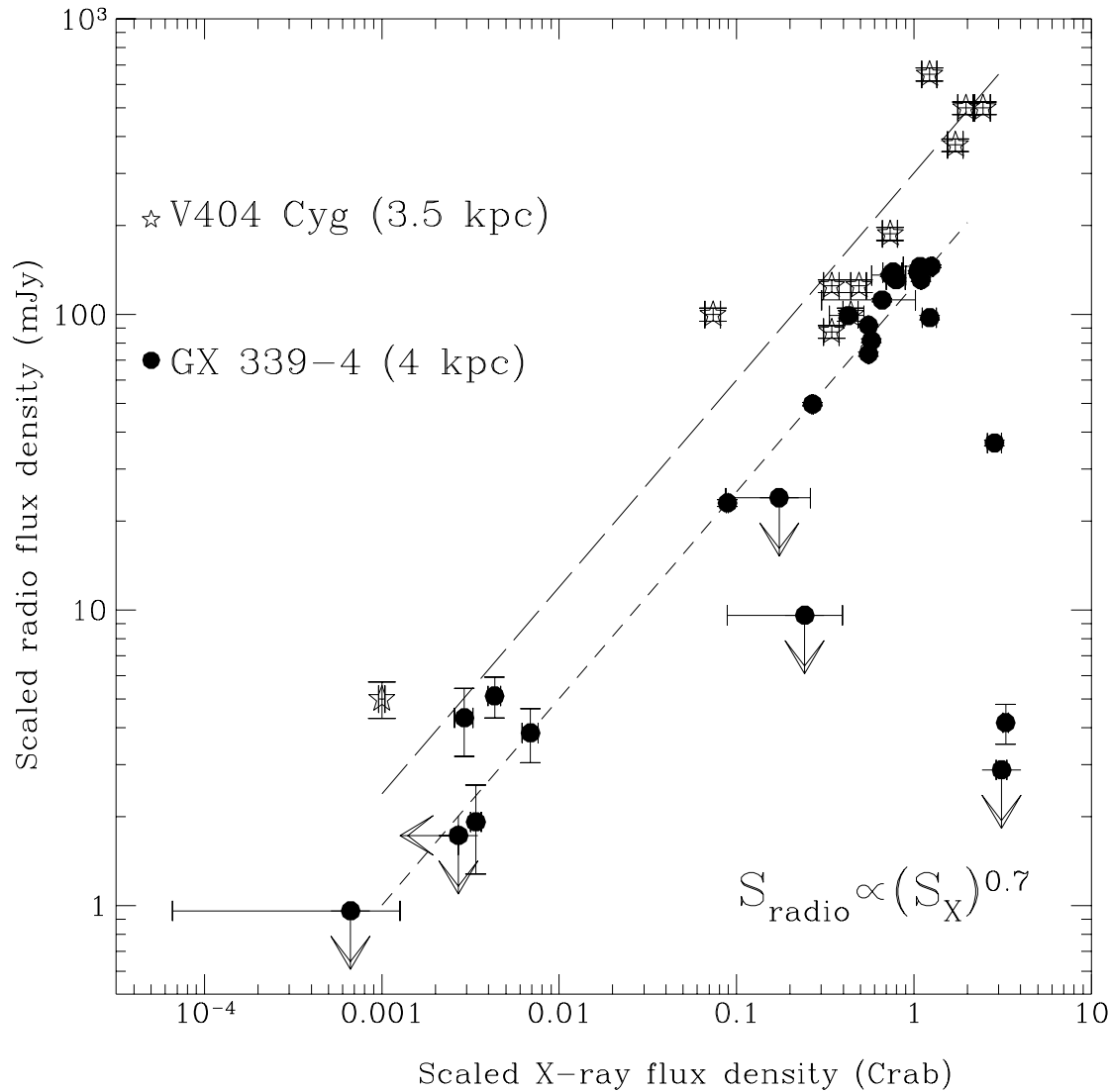
Dynamics of jet formation are better studied in Galactic black holes with jets (“**microquasars**”) because of shorter timescales.

Find clear **X-ray–radio correlation** (similar also seen in some AGN such as 3C120)

$\Rightarrow$  “**universal disk-jet-connection**”



# Jet Formation



X-ray binaries:  $S_{\text{radio}} \propto S_X^{0.7}$

⇒ Radio and X-ray fluxes  
are correlated:  
evidence for interaction  
between disk and jet!

(Gallo, Fender & Pooley, 2003)



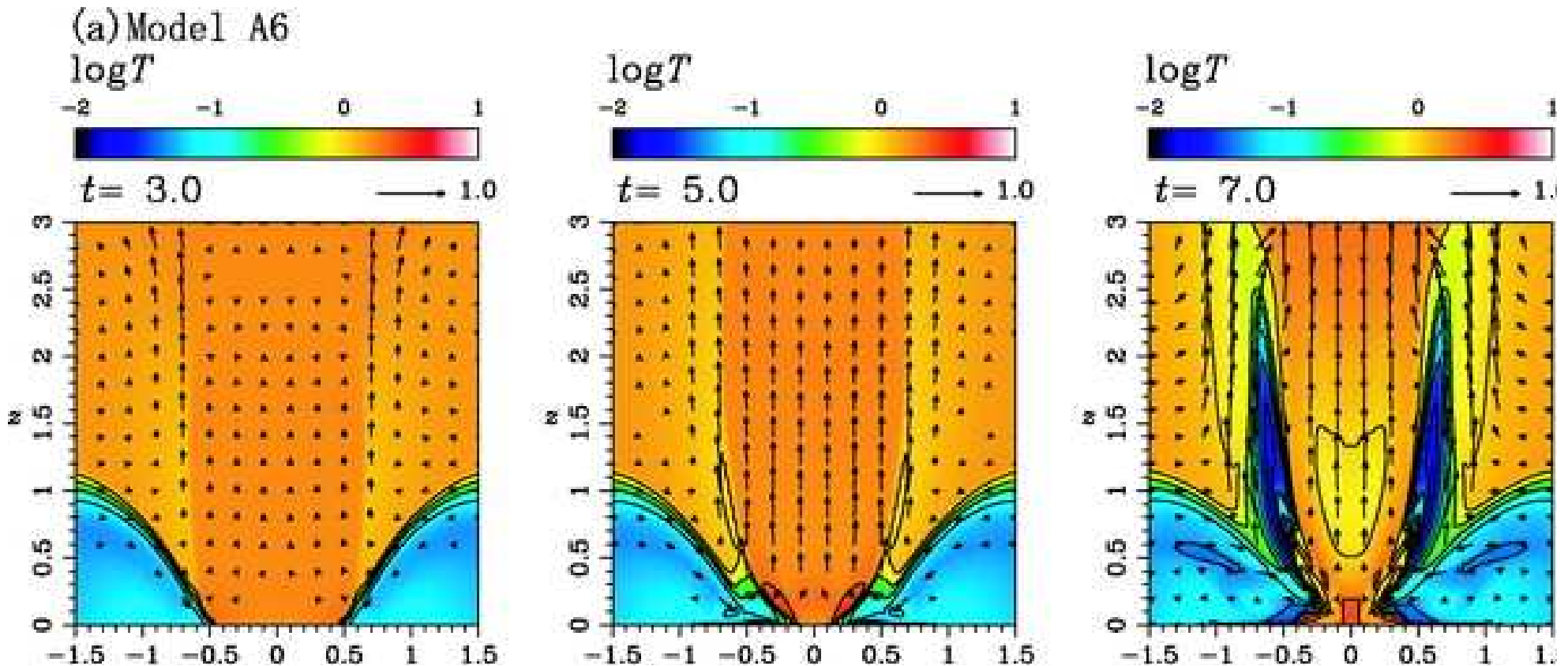


movie time: [jetmovies/agn\\_xray\\_020505\\_11\\_640x480\\_95pc](#)

Marscher et al. (2002): 3C120: X-ray dips followed by radio ejection events  
⇒ jets and accretion disk are related.

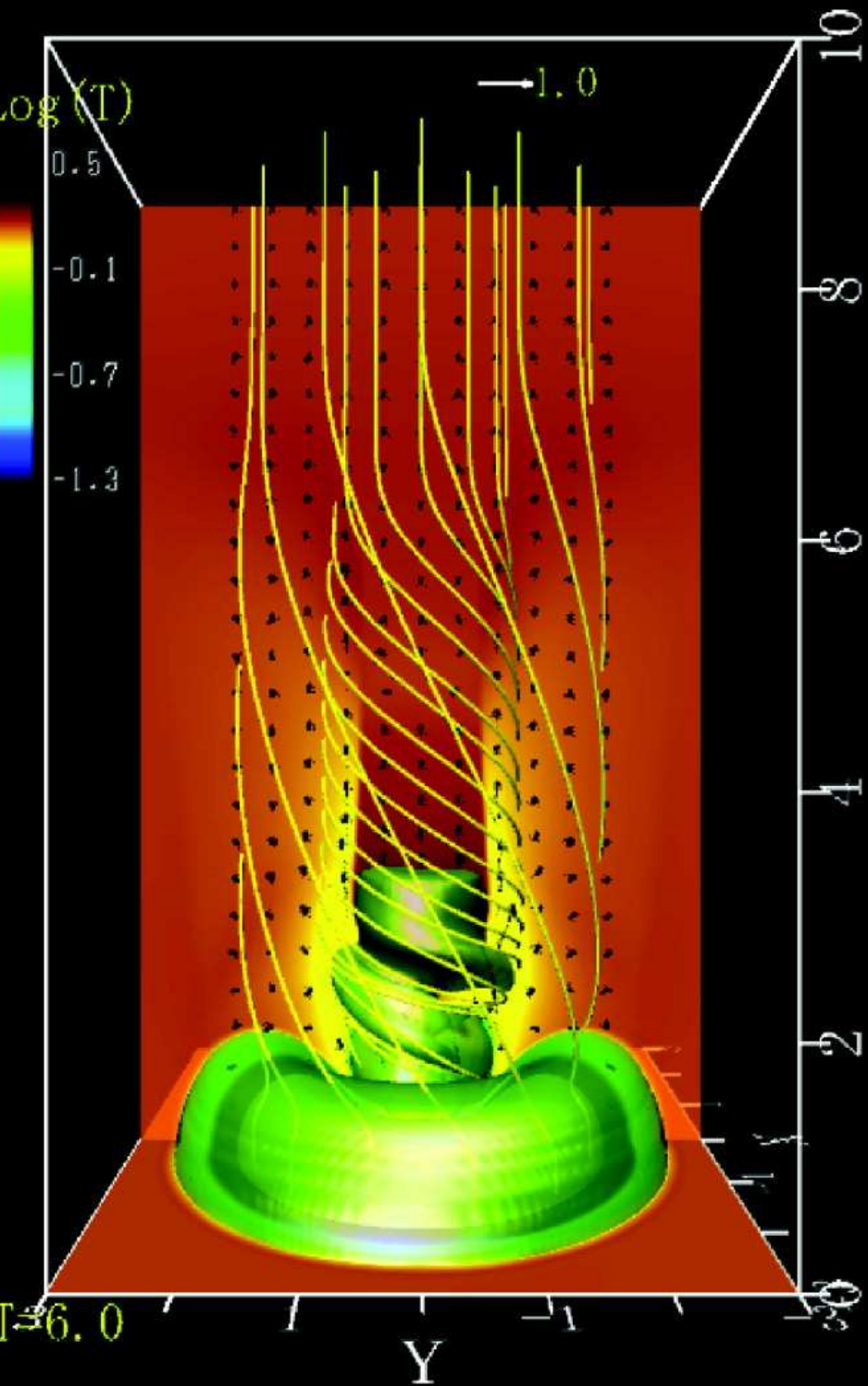


## Jet Formation



Evolution of a newly launched jet (Kigure & Shibata, 2005)

To study jet confinement and propagation: use **magnetohydrodynamical simulations**

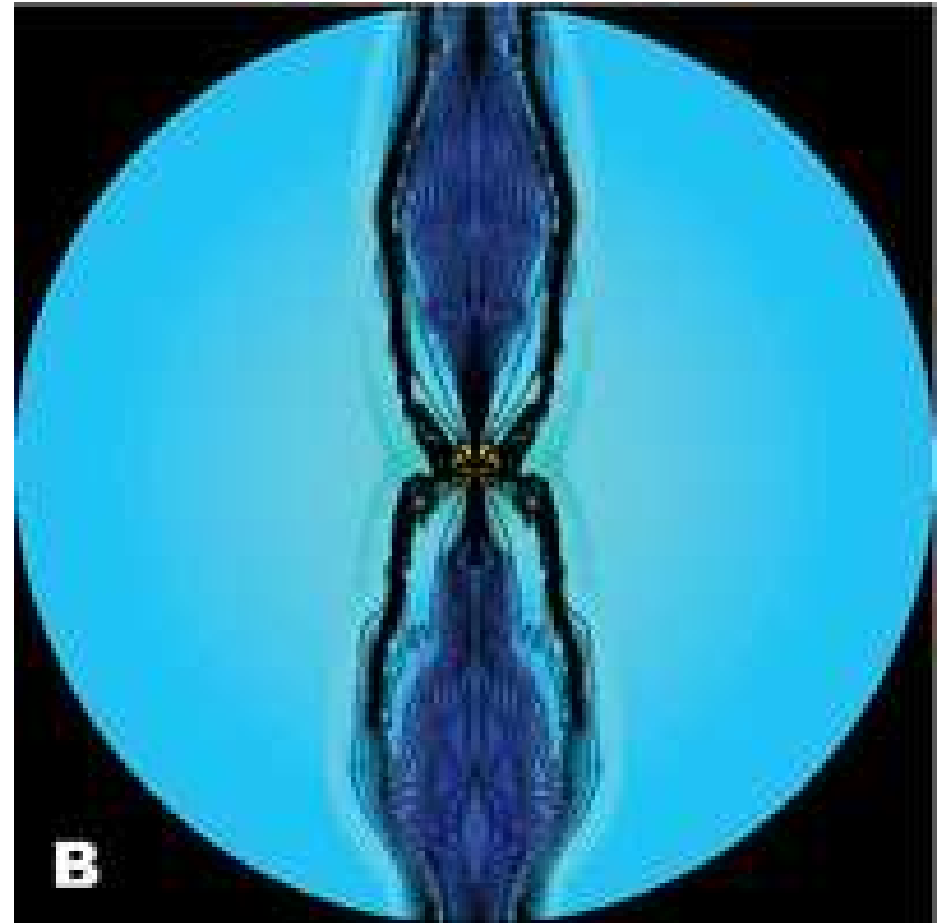
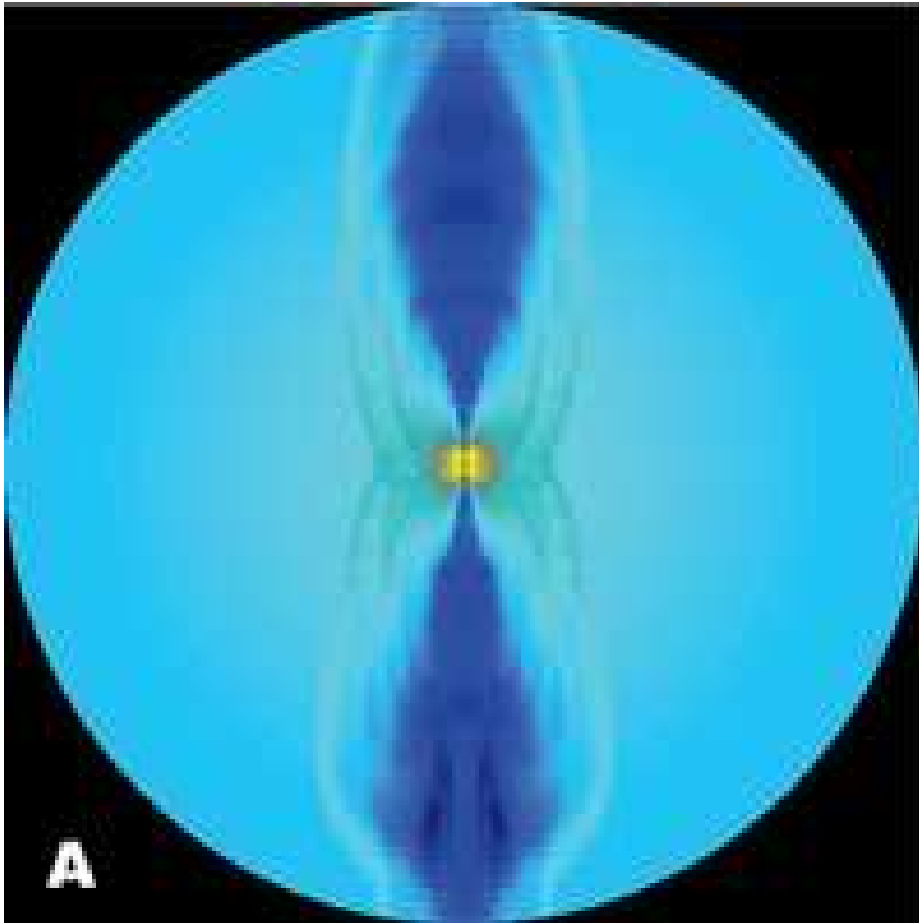


## Temperature profile and $B$ -field configuration of a MHD-jet

Movie: `jetmovies/d155mvj.avi`: Time evolution of  $B$ -field and density close to a BH (Matsumoto&Machida).

(Kigure & Shibata, 2005, Fig. 6)

## Jet Formation

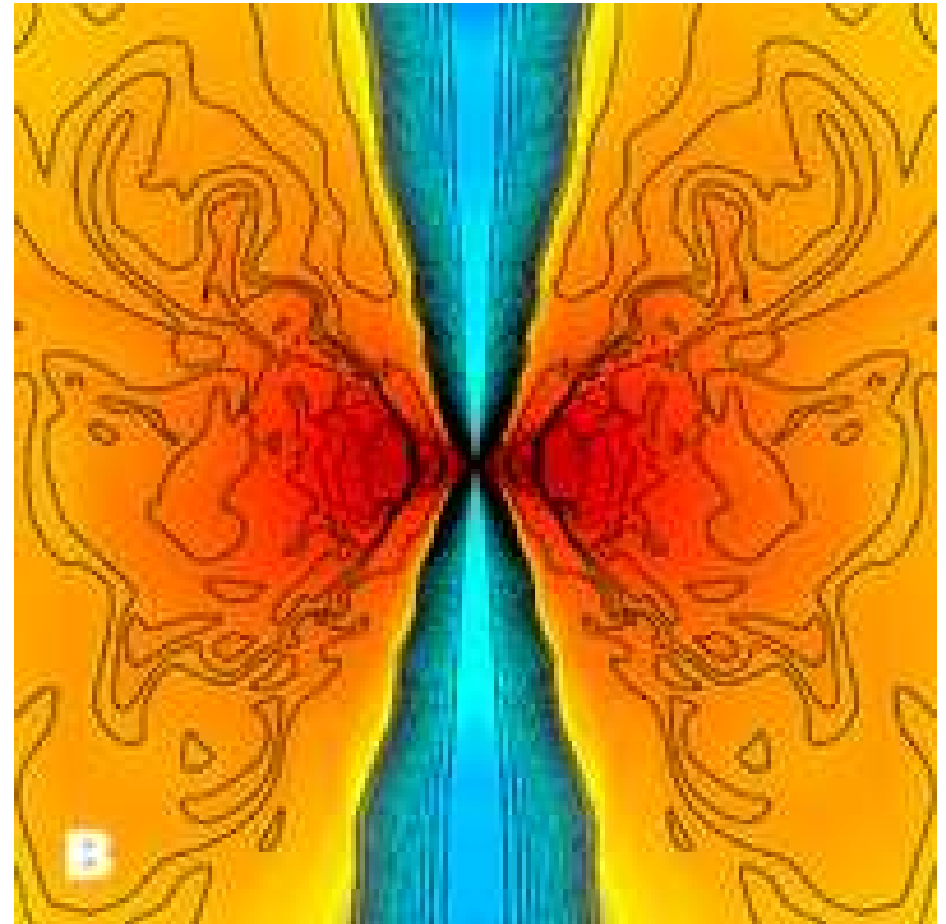
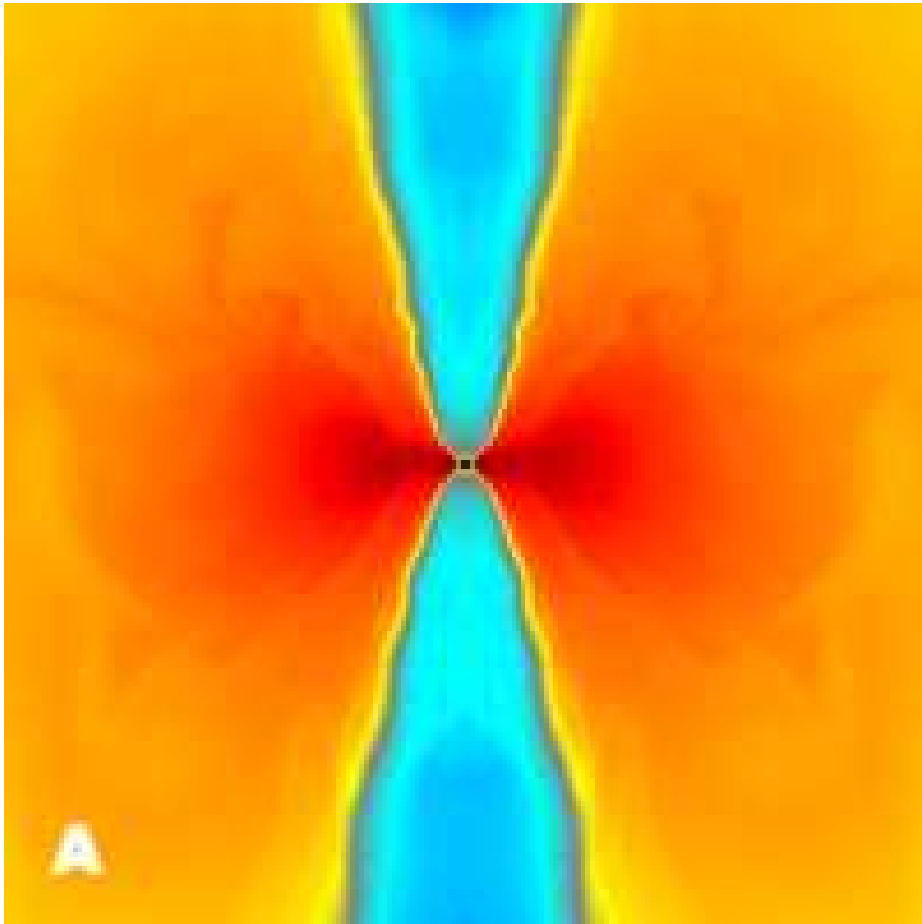


(McKinney, 2006, Fig. 1)

$\log \rho$  (left) and  $\log \rho$  and  $B$  for a jet launched via a disk.

Outer radius is  $10^4 GM/c^2$ .

## Jet Formation



(McKinney, 2006, Fig. 2)

$\log \rho$  (left) and  $\log \rho$  and  $B$  for a jet launched via a disk.

Outer radius is  $10^2 GM/c^2$ .



## Jet Formation

Movie time:

- `diskmovies/rho3.mpg`: jet simulation out to  $40GM/c^2$  (McKinney)
- `diskmovies/rout400new.1rho.3.mpg`: jet simulation out to  $400GM/c^2$  (McKinney)

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