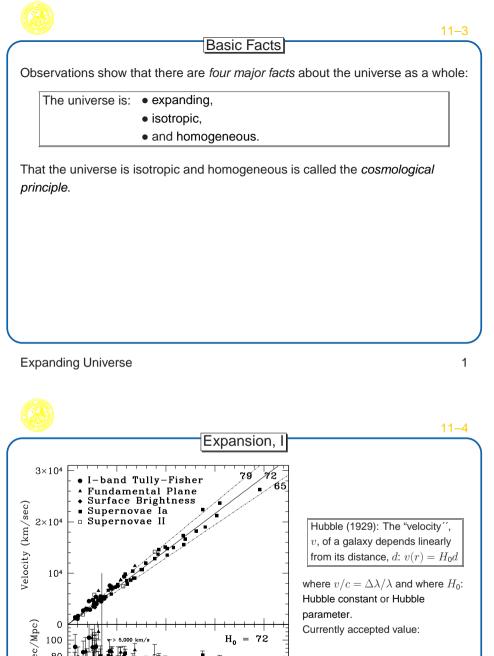
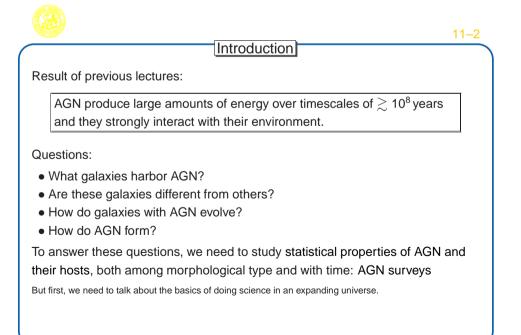
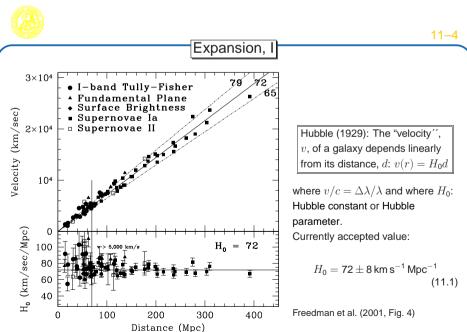


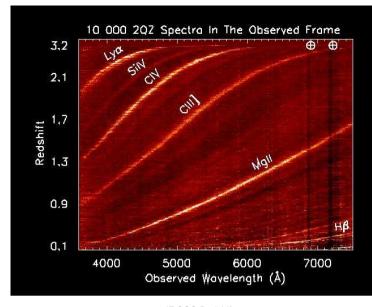
11 - 1

AGN Surveys and AGN Environment

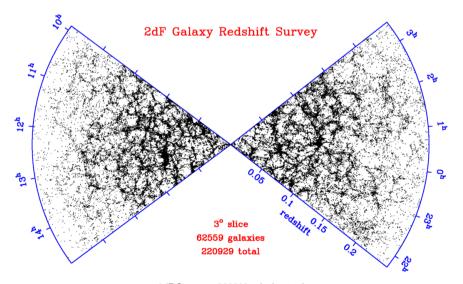




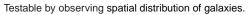




 $\label{eq:good} \begin{array}{l} \mbox{courtesy 2dF QSO Redshift survey} \\ \mbox{As a consequence of the cosmological redshift, for different z different parts of the spectrum of a distant source are visible. \end{array}$

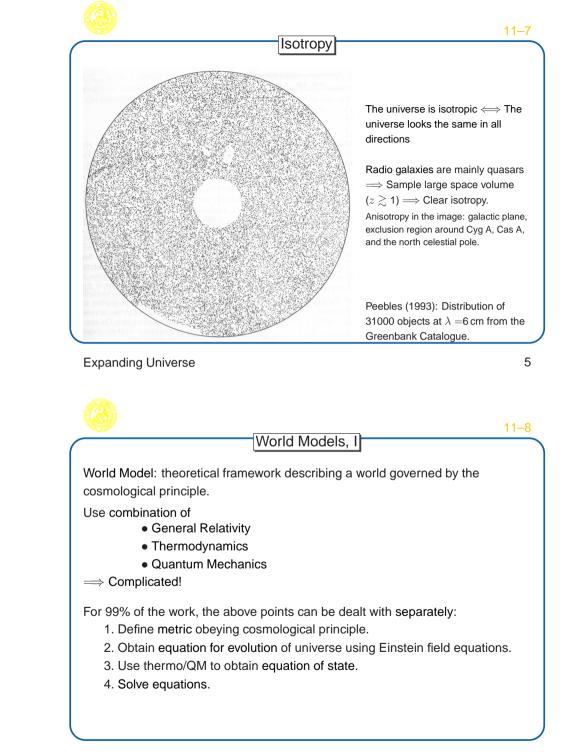


 $[\]begin{array}{c} 2 \text{dF Survey}, \sim 220000 \, \text{galaxies total} \\ \text{The universe is homogeneous} \\ \longleftrightarrow \\ \text{The universe looks the same everywhere in space} \end{array}$



On scales $\gg 100\,\text{Mpc}$ the universe looks indeed the same. Below that: structure.

Structures seen are galaxy clusters (gravitationally bound) and superclusters (larger structures, not [yet] gravitationally bound).



Expanding Universe



World Models, II

Before we can start to think about universe: Brief introduction to assumptions of general relativity.

 \implies See theory lectures for the gory details, or check with the literature (Weinberg or MTW).

Assumptions of GRT:

- Space is 4-dimensional, might be curved
- Matter (=Energy) modifies space (Einstein field equation).
- Covariance: physical laws must be formulated in a coordinate-system independent way.
- Strong equivalence principle: There is no experiment by which one can distinguish between free falling coordinate systems and inertial systems.
- At each point, space is locally Minkowski (i.e., locally, SRT holds).
- \implies Understanding of geometry of space necessary to understand physics.

Expanding Universe

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11 - 10



- Cosmological principle + expansion $\Longrightarrow \exists$ freely expanding cosmical coordinate system.
 - Observers =: fundamental observers
 - Time =: cosmic time

This is the coordinate system in which the 3K radiation is isotropic, clocks can be synchronized, e.g., by adjusting time to the local density of the universe.

 \implies Metric has temporal and spatial part.

This also follows directly from the equivalence principle.

• Homogeneity and isotropy \implies spatial part is spherically symmetric:

$$\mathrm{d}\psi^2 := \mathrm{d}\theta^2 + \sin^2\theta \; \mathrm{d}\phi^2 \tag{11.2}$$

• *Expansion:* \exists scale factor, $R(t) \Longrightarrow$ measure distances using comoving coordinates.

11-11

g

A metric based on these points looks like

$$ds^{2} = c^{2} dt^{2} - R^{2}(t) \left[f^{2}(r) dr^{2} + g^{2}(r) d\psi^{2} \right]$$
(11.3)

where f(r) and g(r) are arbitrary.

Metrics of the form of eq. (11.3) are called Robertson-Walker (RW) metrics (1935), but have been previously also studied by Friedmann and Lemaître.

RW Metric. II

One common choice is

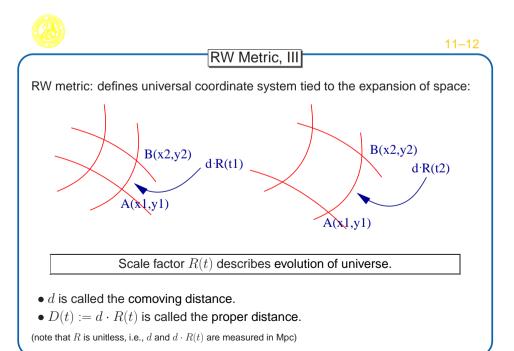
$$ds^{2} = c^{2} dt^{2} - R^{2}(t) \left[dr^{2} + S_{k}^{2}(r) d\psi^{2} \right]$$
(11.4)

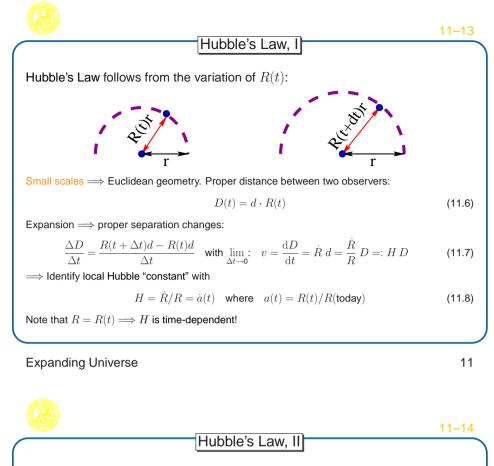
where R(t): scale factor, containing the physics, t: cosmic time, r, θ , ϕ : comoving coordinates, and where

$$S_k(\theta) = \begin{cases} \sin \theta & \text{for } k = +1 \\ \theta & \text{for } k = 0 \\ \sinh \theta & \text{for } k = -1 \end{cases}$$
(11.5)

Remark: θ and ϕ describe directions on sky, as seen from the arbitrary center of the coordinate system (=us), r can be interpreted as a radial coordinate.

Expanding Universe





The cosmological redshift is a consequence of the expansion of the universe:

Since the comoving distance is constant:

$$d = \frac{D(t = \text{today})}{R(t = \text{today})} = \frac{D(t)}{R(t)} = \text{const.} \tag{11.9}$$

Set a(t) = R(t)/R(t = today), then Eq. (11.9) implies

$$\lambda_{\rm obs} = \frac{\lambda_{\rm emit}}{a_{\rm emit}} \quad \Longleftrightarrow \quad z = \frac{\lambda_{\rm obs} - \lambda_{\rm emit}}{\lambda_{\rm emit}} = \frac{\lambda_{\rm obs}}{\lambda_{\rm emit}} - 1 \tag{11.10}$$

(z: observed redshift, $\lambda_{\rm obs}$: observed wavelength, $\lambda_{\rm emit}$: emitted wavelength)

$$1+z = \frac{1}{a_{\text{emit}}} = \frac{R(t = \text{today})}{R(t)} \tag{11.11}$$

Light emitted at z = 1 was emitted when the universe was half as big as today!

z: measure for relative size of universe at time the observed light was emitted.

Hubble's Law, III

For light, $d = c\Delta t$. Therefore

$$\frac{c \ \Delta t_{\rm e}}{R(t_{\rm emit})} = \frac{c \ \Delta t_{\rm obs}}{R(t_{\rm obs})} \quad \text{such that} \quad \frac{\mathrm{d}t}{R(t)} = \text{const.} \tag{11.12}$$

This means that

$$\frac{\mathrm{d}t_{\mathrm{obs}}}{\mathrm{d}t_{\mathrm{emit}}} = \frac{R(t_{\mathrm{obs}})}{R(t_{\mathrm{emit}})} = \mathbf{1} + z \tag{11.13}$$

 \implies Time dilatation of events at large z.

This cosmological time dilatation has been observed in the light curves of supernova outbursts.

Expanding Universe

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	11–16
Expansion and Spectra	11-10
The total number of photons in a box $\mathrm{d}A\cdot c\mathrm{d}t$ and in a frequency range $ u$ to $ u+\mathrm{d} u$ is	
$N = n_{\nu}(\nu) \mathrm{d}A \mathrm{d}\nu c \mathrm{d}t$	(11.14)
This number is conserved during the expansion of the universe:	
$n_{\nu}(\nu_{\text{emit}}) \mathrm{d}A \mathrm{d}\nu_{\text{emit}} c \mathrm{d}t_{\text{emit}} = n_{\nu}(\nu_{\text{obs}}) \frac{d\nu_{\text{emit}}}{1+z} \mathrm{d}A c \mathrm{d}t_{\text{emit}}(1+z)$	(11.15)
$n_{ u}(u_{obs}) \mathrm{d}A \mathrm{d} u_{obs} c \mathrm{d}t_{obs}$	(11.16)
but: arrival time differs \Longrightarrow energy flux density changes:	
$F_{\nu}(\nu_{\rm obs}) = h\nu_{\rm obs}n_{\nu}(\nu_{\rm obs}) = h\frac{\nu_{\rm emit}}{1+z}\nu_n(\nu_{\rm emit}) = \frac{F_{\nu}(\nu_{\rm emit})}{1+z}$	(11.17)
and consequently the total flux in a certain energy band changes as well:	
$F_{\rm obs} = \int F_{\nu}(\nu_{\rm obs}) \mathrm{d}\nu_{\rm obs} = \int \frac{F_{\nu}(\nu_{\rm emit})}{1+z} \cdot \frac{\mathrm{d}\nu_{\rm emit}}{1+z} = \frac{F_{\rm emit}}{(1+z)^2}$	(11.18)
One power of $1 + z$ from decreased photon energy, one from decreased arrival rate.	
For wavelength based flux densities, since $F_{\lambda} = F_{\nu}c/\lambda^2$ one finds $F_{\lambda}(\lambda_{obs}) = F_{\lambda}(\lambda_{emit})/(1+z)^3$.	