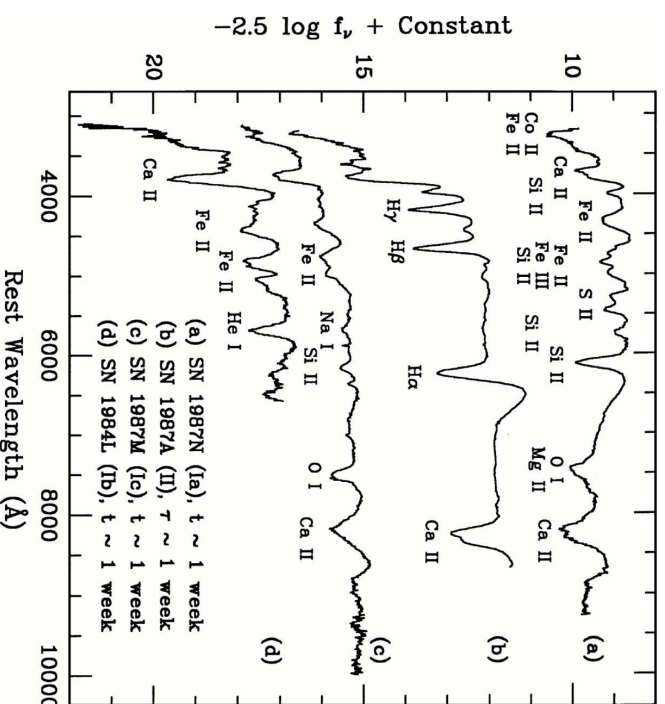


Supernovae have luminosities comparable to whole galaxies: $\sim 10^{51}$ ergs $^{-1}$ in light, $100 \times$ more in neutrinos.

SN1994d (HST WFPC)



(Filippenko, 1997, Fig. 1); t : time after maximum light; τ : time after explosion; P Cyg profiles give $v \sim 10000 \text{ km s}^{-1}$

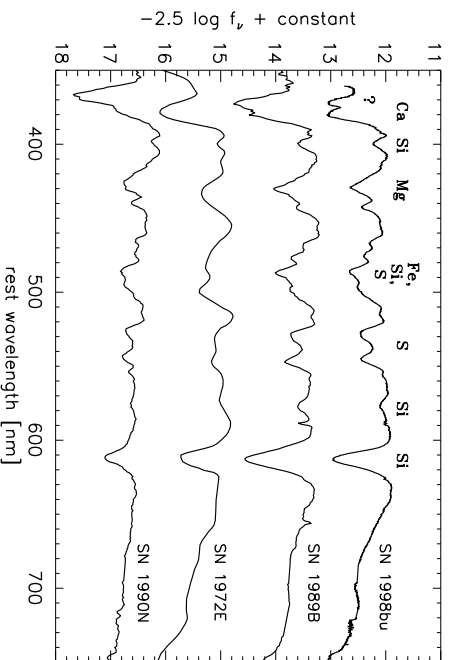
Rough classification (Minkowski, 1941):
Type I: no hydrogen in spectra;
 subtypes Ia, Ib, Ic
Type II: hydrogen present, subtypes II-L, II-P

Note: pre 1985 subtypes Ia, Ib had different definition than today \Rightarrow beware when reading older texts.



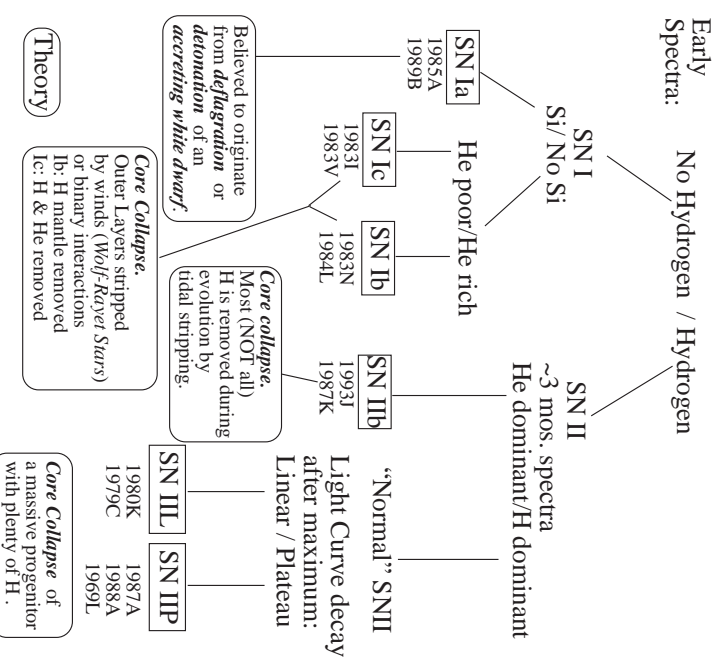
Type Ia Supernovae, II

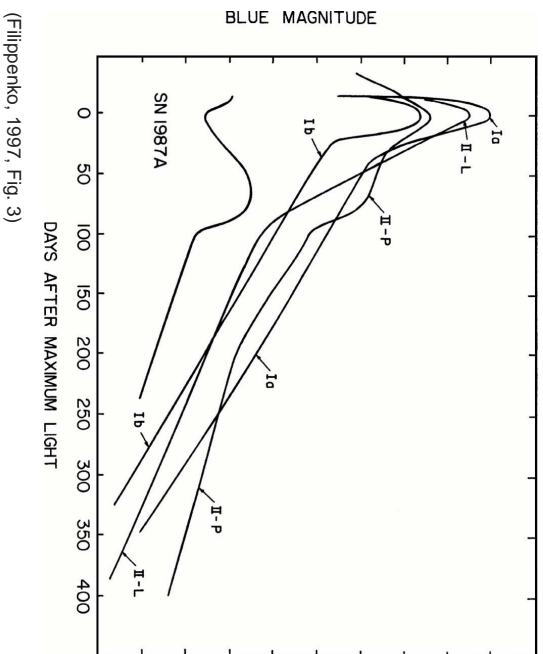
5-61



(Spectra of several SNe at maximum light Jha et al., 1999, Fig. 6)

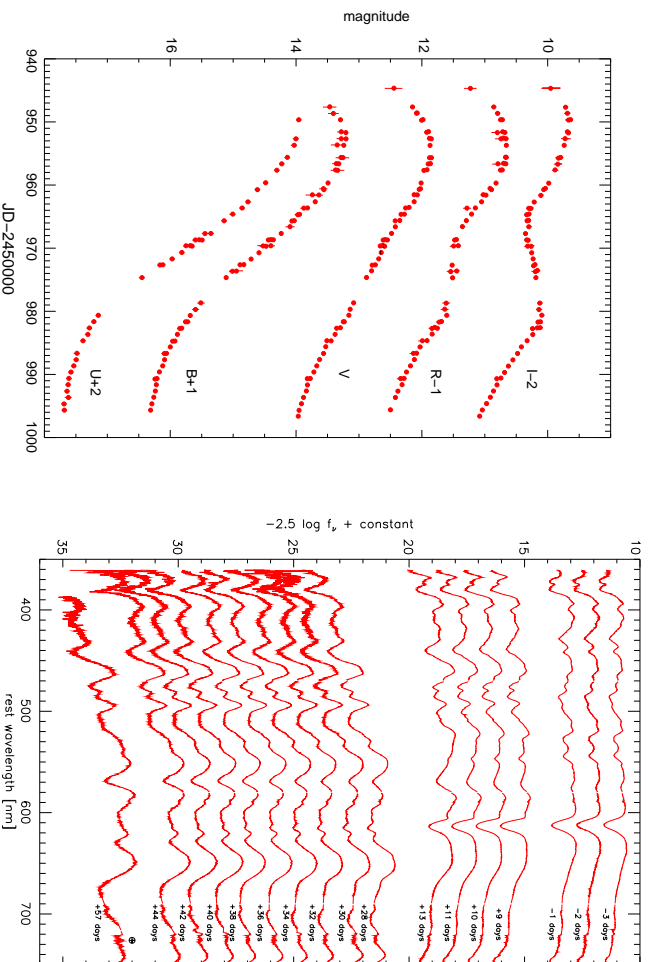
Different supernovae can have very similar spectra. \Rightarrow Allows their classification.





Light curves of SNe I all very similar, SNe II have much more scatter. SNe II-L ("linear") resemble SNe I SNe II-P ("plateau") have const. brightness to within 1 mag for extended period of time.

Standard Candles: Extragalactic



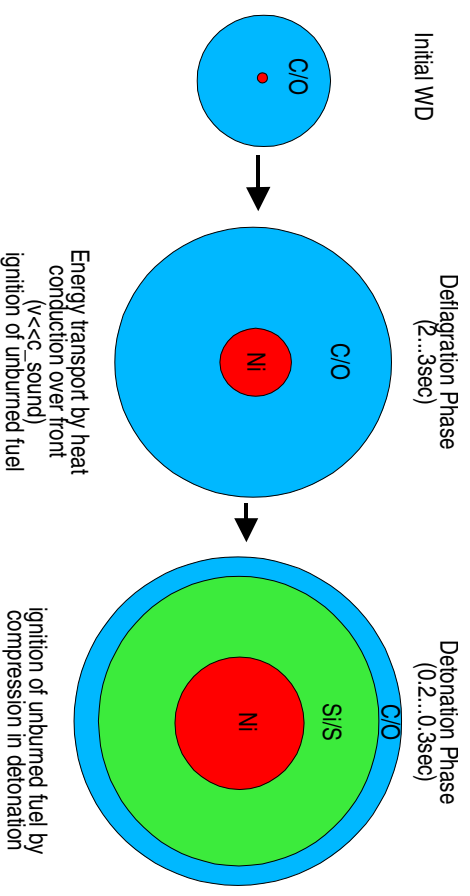
(SN 1998bu in M96, Jha et al., 1999, Figs. 2 and 4)

Clue on origin from supernova statistics:

- SNe II, Ib, Ic: never seen in ellipticals; rarely in SO; generally associated with spiral arms and H II regions.
- ⇒ progenitor of SNe II, Ib, Ic: massive stars ($\gtrsim 8 M_{\odot}$) ⇒ core collapse
- SNe Ia: all types of galaxies, no preference for arms, almost no scatter in lightcurves
- ⇒ progenitor of SNe Ia: accreting carbon-oxygen white dwarfs, undergoing thermonuclear runaway

Rule of thumb: 1...3 SNe per galaxy and per century

Standard Candles: Extragalactic



after P. Höflich

Standard Candles: Extragalactic

Type Ia Supernovae, IX

SN Ia = Explosion of CO white dwarf when pushed over Chandrasekhar limit ($1.4 M_{\odot}$) (via accretion?).

⇒ Always similar process

⇒ Very characteristic light curve: fast rise, rapid fall, exponential decay ("FRED") with half-time of 60 d.

60 d time scale from radioactive decay $\text{Ni}^{56} \rightarrow \text{Co}^{56} \rightarrow \text{Fe}^{56}$ ("self calibration" of lightcurve if same amount of Ni^{56} produced everywhere).

Calibration: SNe Ia in nearby galaxies where Cepheid distances known.

At maximum light:

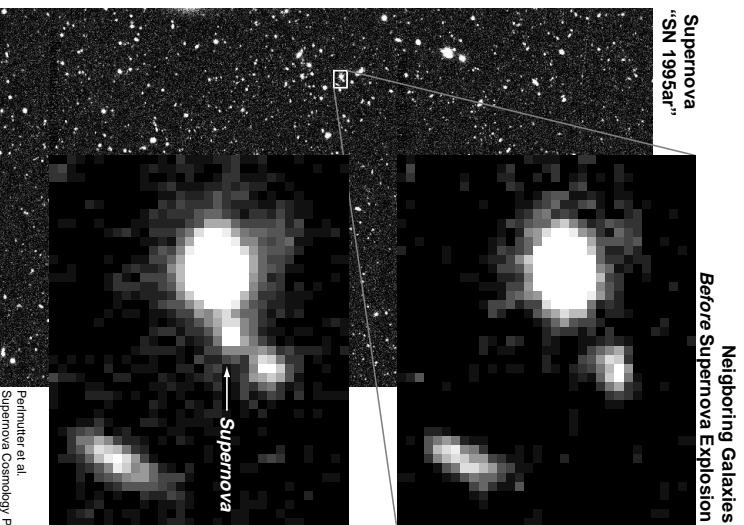
$$M_B = -18.33 \pm 0.11 + 5 \log h_{100} \quad (L \sim 10^9 \dots 10^9 L_{\odot}) \quad (5.33)$$

Intrinsic dispersion: $\lesssim 0.25$ mag (possibly due to size of clusters analyzed?!)?

Observable out to 1000 Mpc

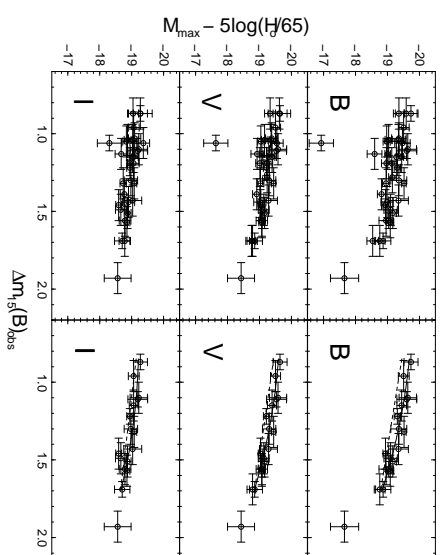
Standard Candles: Extragalactic

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Perlmutter et al.
Supernova Cosmology Project

Type Ia Supernovae, XI

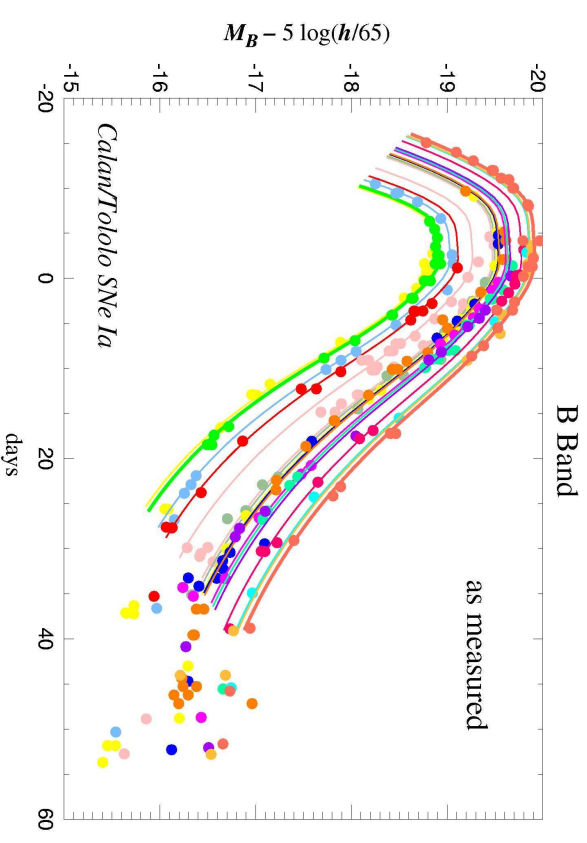


(Phillips et al., 1999, Fig. 8)

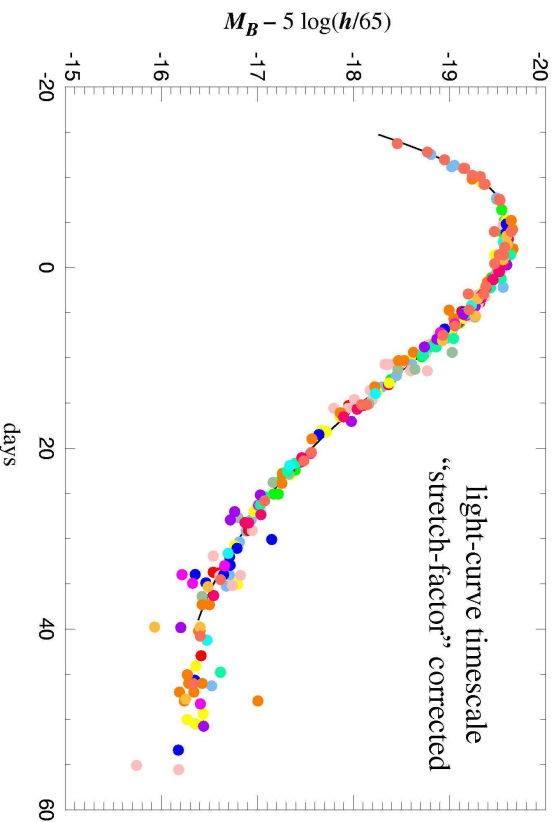
- Caveats:
1. Are they really identical? ⇒ history of pre-WD star?
 2. Correction for extinction in parent galaxy difficult.
 3. Baade-Wesselink for calibration Eq. (5.33) depends crucially on assumed $(B - V)_{\text{off}}$ relation.
 4. Some SN Ia spectroscopically peculiar ⇒ Do not use these!
 5. Decline rate and color vary, but max. brightness and decline rate correlate (see figure).

Standard Candles: Extragalactic

38



Lightcurves of Hamuy et al. SN Ia sample (18 SNe discovered within 5 d past maximum, with $3.6 < \log cz < 4.5$, i.e., $z < 0.1$)



Lightcurves of Hamuy et al. SN Ia sample (18 SNe discovered within 5 d past maximum, with $3.6 < \log cz < 4.5$, i.e., $z < 0.1$), after correction of systematic effects and time dilatation (Kim et al., 1997).



Type Ia Supernovae, XIV

5-73

Recalibration of SN Ia distances with Cepheids gives (Gibson et al., 2000):

$$\log H_0 = 0.2 \{ M_B^{\max} - 0.720 (\pm 0.459) \cdot [\Delta m_{B,15,t} - 1.1] - 1.010 (\pm 0.934) \cdot [\Delta m_{B,15,t} - 1.1]^2 + 28.653 (\pm 0.042) \} \quad (5.34)$$

where

$$\Delta m_{B,15,t} = \Delta m_{B,15} + 0.1 E(B - V) \quad (5.35)$$

where

$\Delta m_{B,15}$: observed 15 d decline rate,
 $E(B - V)$: total extinction (galactic+intrinsic).

Eq. (5.34) valid for B-band, equivalent formulae exist for V and I.

Overall, the calibration is good to better than 0.2 mag in B.

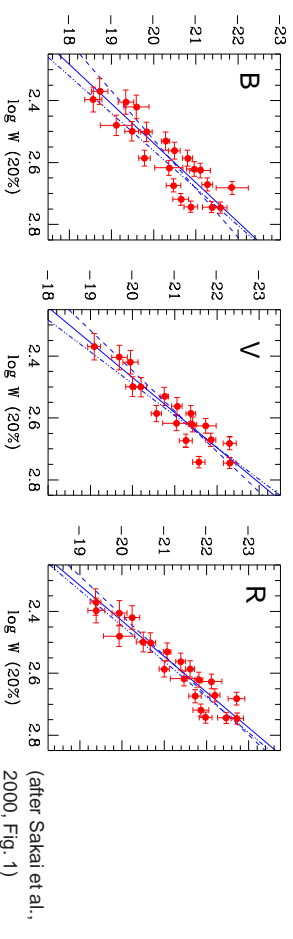
Standard Candles: Extragalactic

41



Tully-Fisher, I

5-74



Tully-Fisher relation for spiral galaxies: Width of 21 cm line of H correlated with galaxy luminosity:

$$M = -a \log \left(\frac{W_{20}}{\sin i} \right) - b \quad (5.36)$$

where W_{20} : 20% line width (km s^{-1}), typically $W_{20} \sim 300 \text{ km s}^{-1}$, i : inclination angle.

For the B- and I-Bands (Sakai et al., 2000):

	B	I
a	7.97 ± 0.72	9.24 ± 0.75
b	19.80 ± 0.11	21.12 ± 0.12

Standard Candles: Extragalactic

42



Tully-Fisher, III

5-75

Qualitative Physics: Line width related to mass of galaxy: $W/2 \sim V_{\max}$, where

V_{\max} max. velocity of rotation curve

\Rightarrow Assume $M/L = \text{const.}$ (good assumption)

\Rightarrow width related to luminosity.

Detailed physical basis unknown. Might be related to galaxy formation ("hierarchical clustering", see later).

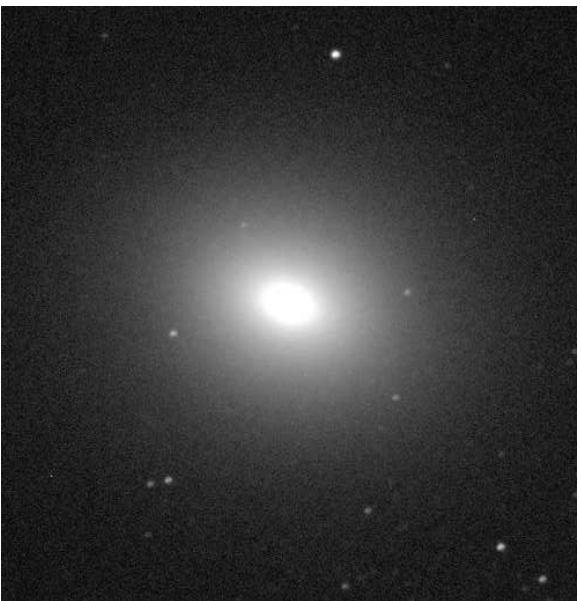
I-band is better (less internal extinction).

Caveats:

1. Determination of inclination i .
2. Influence of turbulent motion within galaxy.
3. Constants dependent on galaxy type (Sa and Sb similar, Sc more luminous by factor of ~ 2).
4. Optical extinction.
5. Intrinsic dispersion ~ 0.2 mag.
6. Barred Galaxies problematic.

Standard Candles: Extragalactic

43



M32 (companion of Andromeda),
courtesy W. Keel

“Faber-Jackson” law for elliptical galaxies:
The luminosity L of an elliptical galaxy scales with its intrinsic velocity dispersion, σ , as $L \propto \sigma^4$.
Note that ellipticals have virtually no Hydrogen
 \Rightarrow cannot use 21 cm.

Ellipticals: $M_B = -19.38 \pm 0.07 - (9.0 \pm 0.7)(\log \sigma - 2.3)$ (5.37)
Lenticulars (Type S0): $M_B = -19.65 \pm 0.08 - (8.4 \pm 0.8)(\log \sigma - 2.3)$ (5.38)



D_n - σ

5-77

The Faber-Jackson law is a specialized case of the more general D_n - σ -relation:
The intensity profile of an elliptical galaxy is given by de Vaucouleurs' $r^{1/4}$ law:

$$I(r) = I_0 \exp\left(-\left(r/r_0\right)^{1/4}\right) \implies L = \int I \propto I_0 r_0^2 \quad (5.39)$$

Because of the virial theorem ($E_{\text{kin}} = -E_{\text{pot}}/2$):

$$\frac{1}{2} m \sigma^2 = G \frac{m M}{r_0} \iff \sigma^2 \propto \frac{M}{r_0} \quad (5.40)$$

where σ : velocity dispersion.

Assume a mass-to-light ratio

$$M/L \propto M^\alpha \quad (5.41)$$

($\alpha \sim 0.25$). and use r_0 from Eq. (5.39) to obtain

$$L^{1+\alpha} \propto \sigma^{4-4\alpha} I_0^{\alpha-1} \quad (5.42)$$

This is called the “fundamental plane” relationship (Dressler et al., 1987).

Standard Candles: Extragalactic

45



D_n - σ

5-78

Observational version of the fundamental plane relationship: Instead of inserting r_0 and I_0 , measure diameter D_n of aperture to reach some mean surface brightness (typically sky brightness, 20.75 mag arcsec⁻² in B), and use calibration.

Note: Assumptions are

1. M/L same everywhere.

2. ellipticals have same stellar population everywhere

Calibration paper: Kelson et al. (2000).

Standard Candles: Extragalactic

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Path to H_0

5-79

To obtain H_0 , we need distances, and redshifts.

Redshifts: Trivial

Distances: Hubble Space Telescope Key Project on Extragalactic Distance Scale.

Summary paper: Freedman et al. (2001), there are a total of 29 papers on the HST key project!

Strategy:

1. Use high-quality candles: Cepheid variables as primary distance calibrator.
2. Calibrate secondary calibrators that work out to $cz = 10000 \text{ km s}^{-1}$:
 - Tully-Fisher,
 - Type Ia Supernovae,
 - Surface Brightness Fluctuations,
 - Fundamental-plane for Ellipticals.
3. Combine uncertainties from these methods.

Hubble Constant

1

Velocity Field, I

Before determining H_0 : correct for influence of velocity field (cluster motion with respect to comoving coordinates).

The observed redshift is given by

$$1 + z = (1 + z_R) \left(1 - \frac{v_0}{c} + \frac{v_G}{c} \right) \quad (5.43)$$

where

v_0 : observer's radial velocity in direction of galaxy

v_G : radial velocity of the galaxy, difficult to find

z_R : cosmological redshift

Older galaxy catalogues often attempt to correct the measured values of z to produce "corrected redshifts", e.g., by setting $v_G = 0$ and

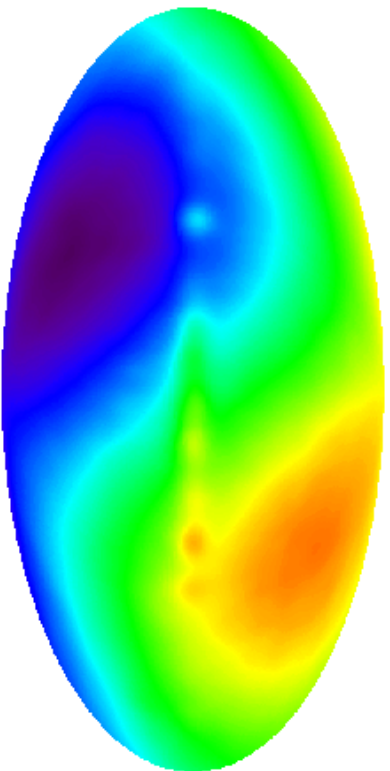
$$1 + z = (1 + z_R) \left(1 + \frac{v_0}{c} \right) \sim 1 + z_R - \frac{v_0}{c} \implies z_R \sim z + \frac{v_0}{c} \quad (5.44)$$

since v_0 was not well known before COBE \implies introduces unnecessary problems

\implies correction not used in recent redshift surveys! (see Harrison & Noonan, 1979, for details)

Hubble Constant

2



(COBE DMR; Bennett et al., 1996)

v_0 is easy to find \implies Measure velocity of Earth with respect to 3K radiation. COBE finds $\Delta T = 3.353 \pm 0.024 \text{ mK}$ of 3K black-body spectrum of $T = 2.725 \pm 0.020 \text{ K}$, using $\Delta T/T = v/c$.

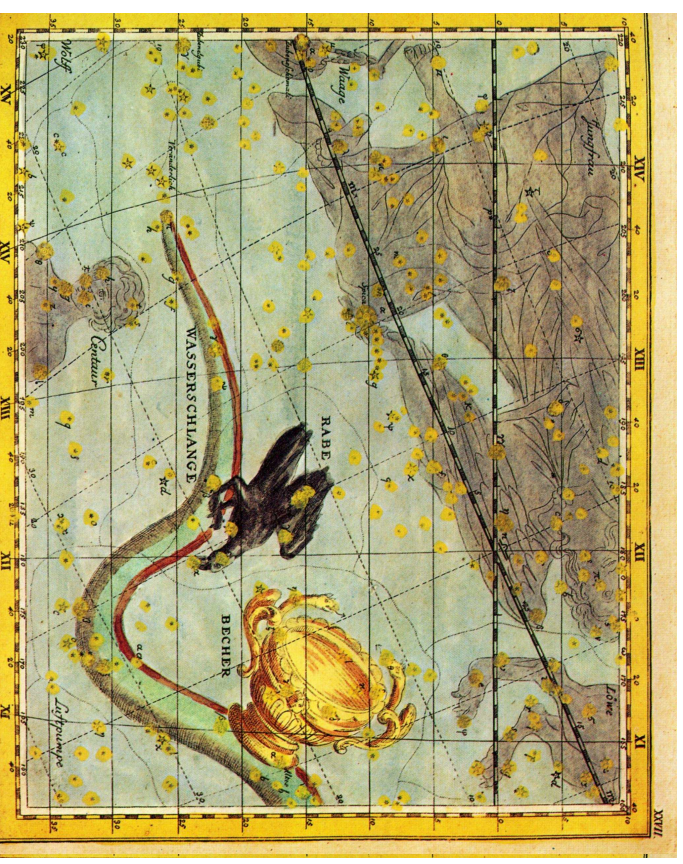
$$v_0 = (369.1 \pm 2.6) \text{ km s}^{-1} \cdot \cos \theta_{\text{CMB}} \quad (5.45)$$

where $\theta_{\text{CMB}} = \angle(v, v_{\text{CMB}})$, and v_{CMB} points towards

$$(l, b) = (264^\circ 26' \pm 0^\circ 33', 48^\circ 22' \pm 0^\circ 13')$$

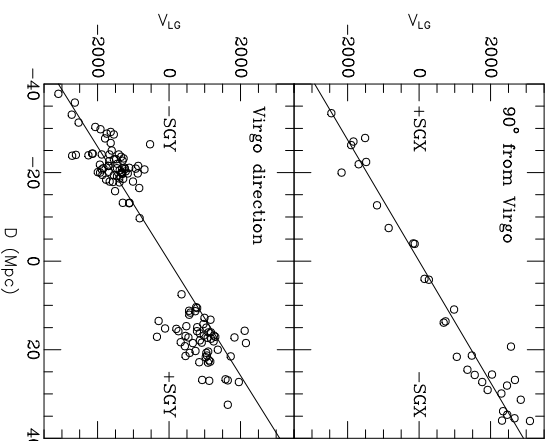
$$(\alpha, \delta)_{\text{J2000.0}} = (1^{\text{h}} 12^{\text{m}} 2^{\text{s}} \pm 0^{\text{m}} 8', -7^\circ 06' \pm 0^\circ 16')$$

in constellation Crater.



The constellation Crater ("Becher") in Johan Elert Bode's Sternatlas (after Slawik/Reichert, Atlas der Sternbilder, Spektrum, 2004)

Velocity Field, IV



To get feeling for v_G out to Virgo, need to study local velocity field surrounding local group and beyond.

Two major velocity components:

1. Virgo-centric infall (known since mid-1970s)

2. Motion towards great attractor ("Seven Samurais", 1980)

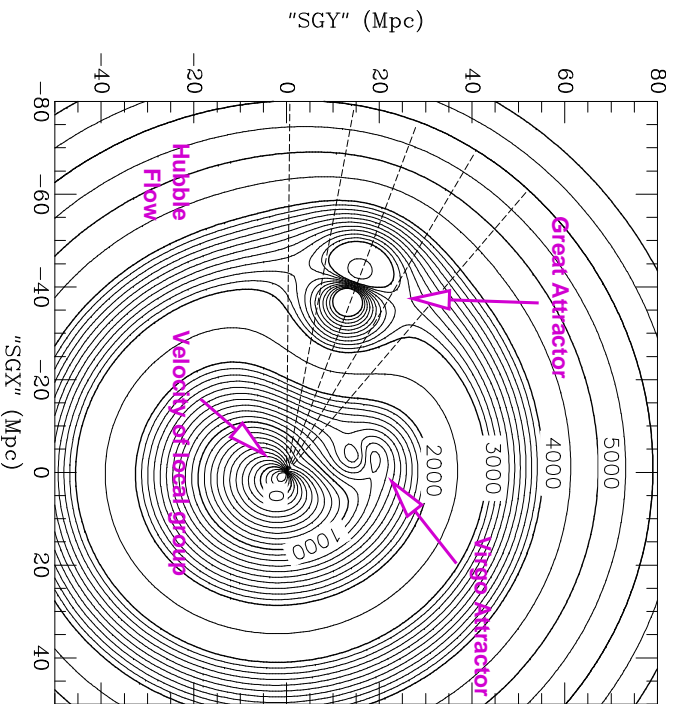
plus virtualized galaxy motions within clusters.

General analysis: build maximum likelihood model of velocity field including above components *plus* Hubble flow. See Tony et al. (2000) for details.

Galaxy moves within local group with $v \sim 630 \text{ km s}^{-1}$

Hubble Constant

5



Decomposition of velocity field: (Mould et al., 2000, Tab. A1, note that Tonry et al. 2000 find slightly different values):

Virgo	$0^{\text{h}}19^{\text{m}}00^{\text{s}}$	$\delta^{\text{h}}19^{\text{m}}00^{\text{s}}$
GA	$12^{\text{h}}28^{\text{m}}13^{\text{s}}$	$+12^{\circ}40'00''$
Shapley	$13^{\text{h}}30^{\text{m}}13^{\text{s}}$	$+31^{\circ}00'00''$

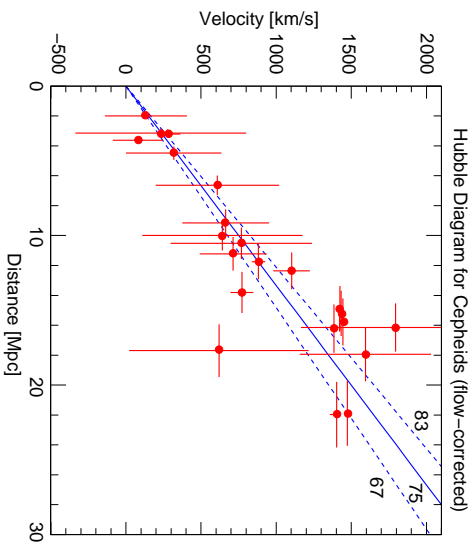
(v wrt. center of local group; *not* taking Hubble flow into account!).

(Tonry et al., 2000, Fig. 20)



H from HST

5-85



- To obtain H_0 :
1. Determine d with Cepheids and HST
 2. Determine " v ", corrected for local velocity field
 3. Draw Hubble-diagram
 4. Regression Analysis $\Rightarrow H_0$ Value from HST Key Project:

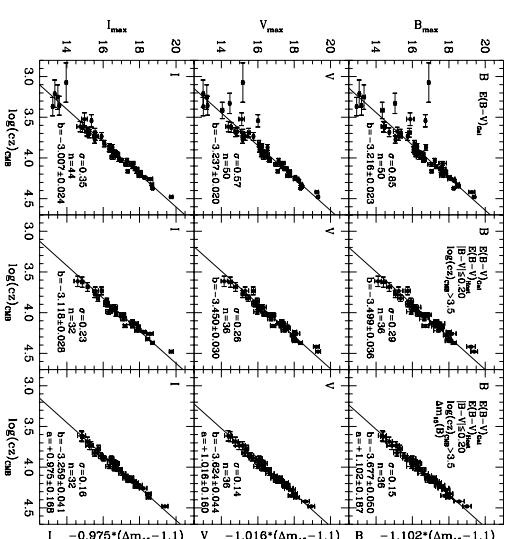
$H_0 = 75 \pm 10 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (5.46)

Freedman et al. (2001, Fig. 1)



H from HST

5-86



Cepheids alone: nearby \Rightarrow systematic uncertainties due to local flow correction and small overall v

\Rightarrow use secondary candles to get to larger distances.

Example: magnitude-redshift diagram, analogous to Hubble diagram ($m \propto -5 \log L$, and $L \propto 1/r^2 \propto 1/z^2$ because of Hubble $\Rightarrow m \propto \log cz$).

(SN Ia Hubble relations; left: full sample, middle: excluding strongly reddened SN Iae, right: same as middle, correcting for light-curve shape Freedman et al., 2001, Fig. 2)

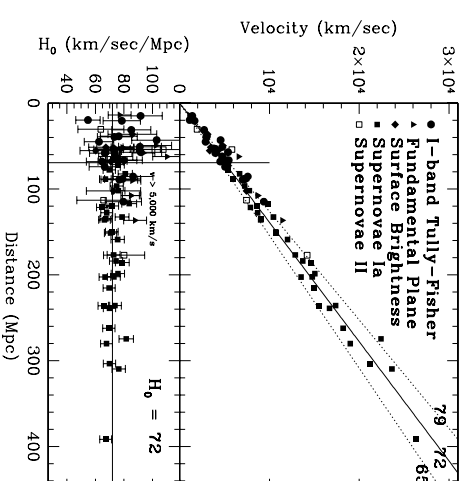
Hubble Constant

8



H from HST

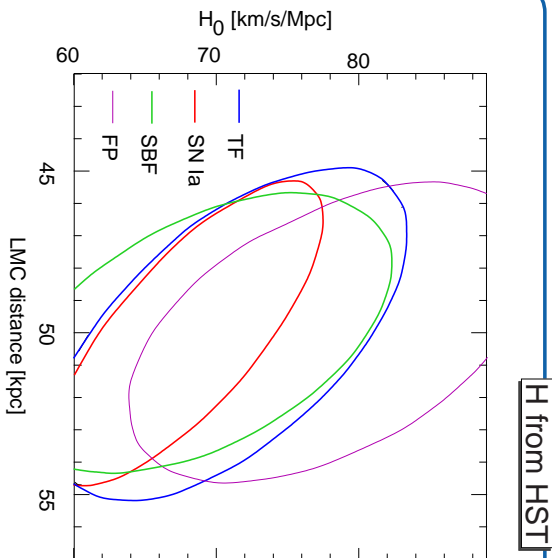
5-87



Combining all secondary methods, best value found:

$H_0 = 72 \pm 8 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (5.47)

Freedman et al. (2001, Fig. 4)



(after Mould et al., 2000, Fig. 5)

Hubble Constant

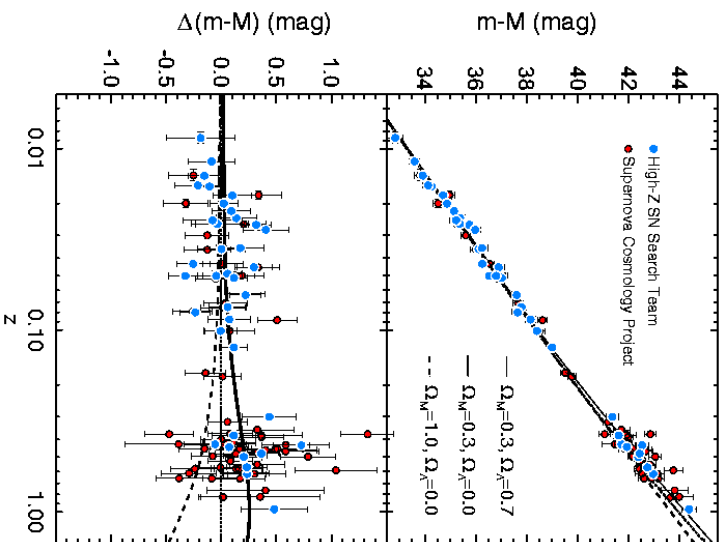
H from HST

Major systematic uncertainty in current H_0 value: zero-point of Cepheid scale, i.e., distance to Large Magellanic Cloud.

Despite these problems:
 ⇒ All current values approach $\sim 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, with uncertainty $\sim 10\%$

H_0 controversy is over

10



For larger distances: There are deviations from Hubble-Relation!
 Before we understand why: Need to understand the Big-Bang itself!

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