



Distance Ladder and H_0



Introduction, I

Distances are required for determination of H_0 .

⇒ Need to measure distances out to ~ 200 Mpc to obtain reliable values.

To get this far: cosmological distance ladder.

1. Trigonometric Parallax and Moving Cluster
2. Main Sequence Fitting
3. RR Lyr
4. Baade-Wesselink
5. Cepheids
6. (Light echos)
7. Brightest Stars
8. Type Ia Supernovae
9. Tully-Fisher
10. $D_n - \sigma$ for ellipticals
11. Brightest Cluster Galaxies
12. Gravitational Lenses

Still the **best reference** on this subject is ROWAN-ROBINSON, M., 1985, The Cosmological Distance Ladder, New York: Freeman.

Distance Determination 1



Classical Cosmology

To understand what universe we live in, we need to determine observationally the following numbers:

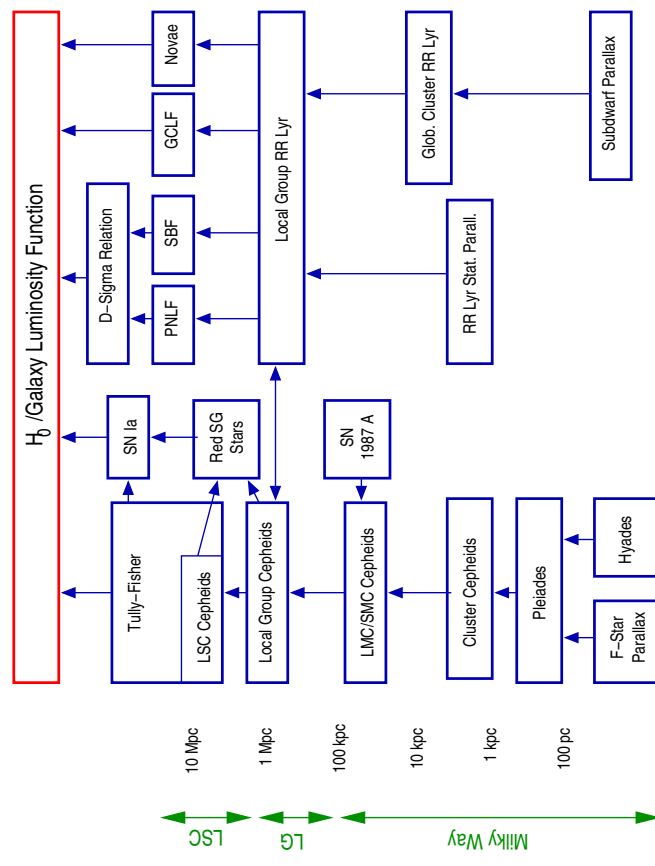
1. The Hubble constant, H_0
⇒ Requires distance measurements.
2. The current density parameter, Ω_0
⇒ Requires measurement of the mass density.
3. The cosmological constant, Λ
⇒ Requires acceleration measurements.
4. The age of the universe, t_0 , for consistency checks
⇒ Requires age measurements.

The determination of these numbers is the realm of classical cosmology.

First part: Distance determination and H_0 !

Classical Cosmology

(after Jacoby et al., 1992, Fig. 1)





Units

Basic unit of length in astronomy: **Astronomical Unit (AU)**.

Colloquial Definition: 1 AU = mean distance Earth–Sun.

Measurement: (Venus) radar ranging, interplanetary satellite positions,

χ^2 minimization of N -body simulations of solar system

$$1 \text{ AU} \sim 149.6 \times 10^6 \text{ km}$$

In the astronomical system of units (IAU 1976), the AU is defined via Gaussian gravitational constant (k), where the acceleration

$$\ddot{r} = -\frac{k^2(1+m)r}{r^3}$$

where $k := 0.01720209895$, leading to $a_{\oplus} = 1.00000105726665$, and $1 \text{ AU} = 1.4959787066 \times 10^{11} \text{ m}$ (Seidelmann, 1992).

Reason for this definition: k much better known than G .

(2006 CODATA: $G = 6.67428(67) \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$, so only known to 4 significant digits)

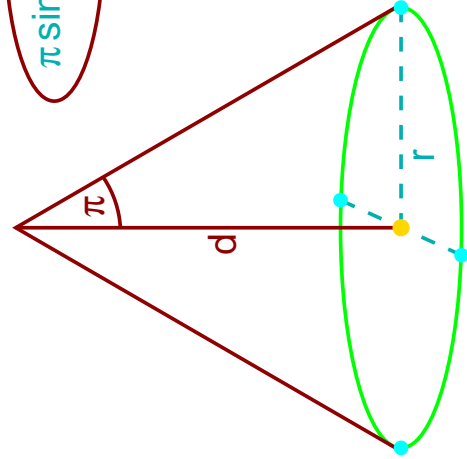
Distance Determination

3



Trigonometric Parallax, I

9-6



Motion of Earth around Sun \implies Parallax produces apparent motion by amount

$$\tan \pi \sim \pi = r_{\oplus}/d \quad (9.1)$$

π is called the trigonometric parallax, and *not* 3.141!

If star is at ecliptic latitude b , then ellipse with axes π and $\pi \sin b$.

Measurement difficult: $\pi \lesssim 0.76''$ (α Cen). Define unit for distance:

$$\begin{aligned} \text{Parsec: Distance where } 1 \text{ AU has } \pi &= \\ 1'' &, 1 \text{ pc} = 206265 \text{ AU} = 3.08 \times \\ 10^{18} \text{ cm} &= 3.26 \text{ ly} \end{aligned}$$

after Rowan-Robinson (1985, Fig. 2.1)

Geometric Methods

1



Trigonometric Parallax, II

Best measurements to date: Hipparcos satellite (1989–1993)

- systematic error of position: $\sim 0.5 \text{ mas}$ for stars brighter 9 mag
- effective distance limit: 1 kpc
- standard error of proper motion: $\sim 1 \text{ mas yr}^{-1}$
- broad band photometry
- narrow band: B – V, V – J
- magnitude limit: 12 mag
- complete to mag: 7.3–9.0

Results available at <http://www.rssd.esa.int/index.php?project=HIPPARCOS>

Hipparcos catalogue: 118 218 objects with milliarcsecond precision.

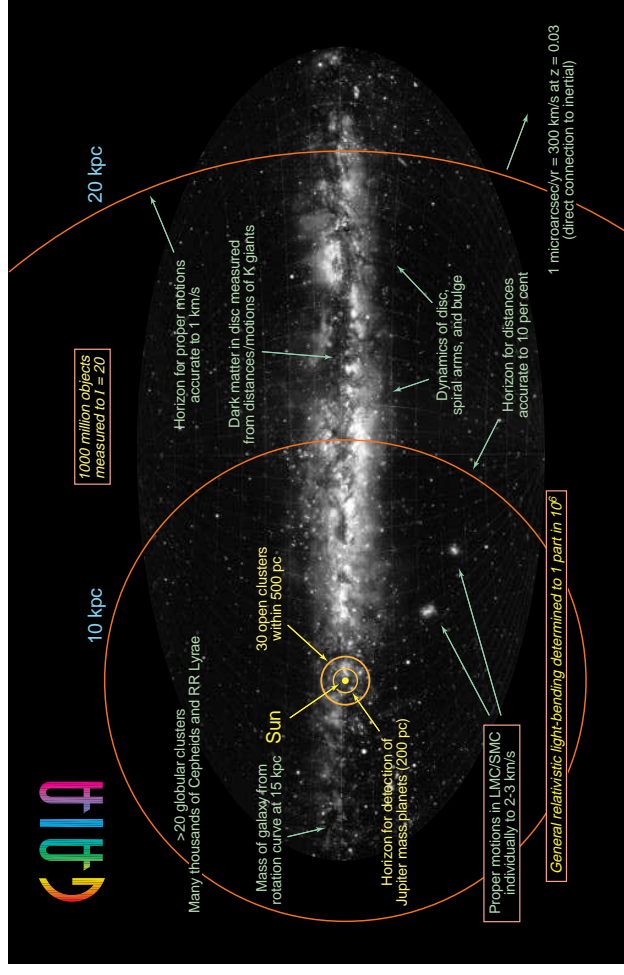
Tycho catalogue: 2 539 913 stars with 20–30 mas precision, two-band photometry (99% complete down to 11 mag)

Revised Hipparcos calibration: see van Leeuwen (2007).

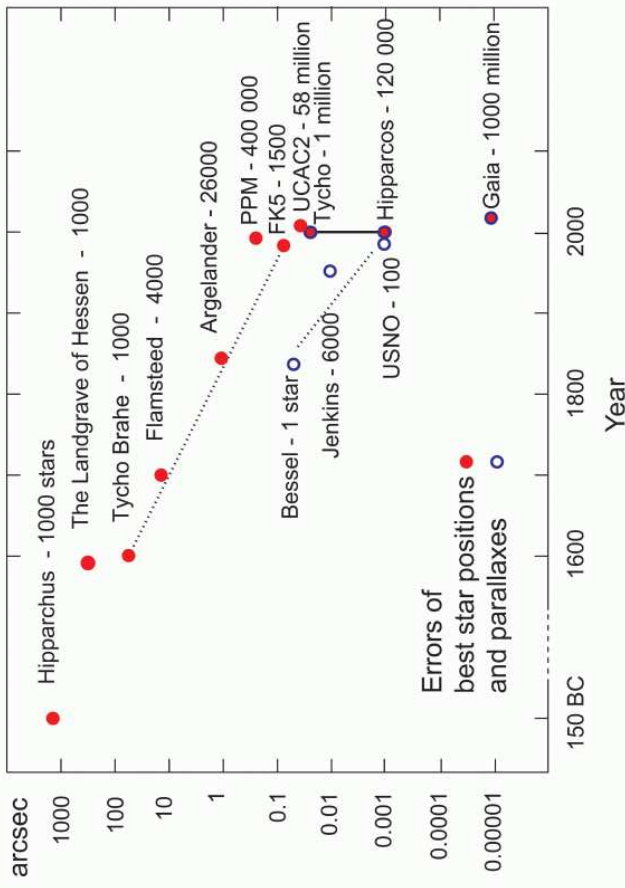
Geometric Methods

2

GAIA (ESA mission, to be launched 2011 Dec on Soyuz from Kourou):



GAIA: $\sim 4 \mu\text{arcsec}$ precision, 4 color to $V = 20$ mag, 10^9 objects.

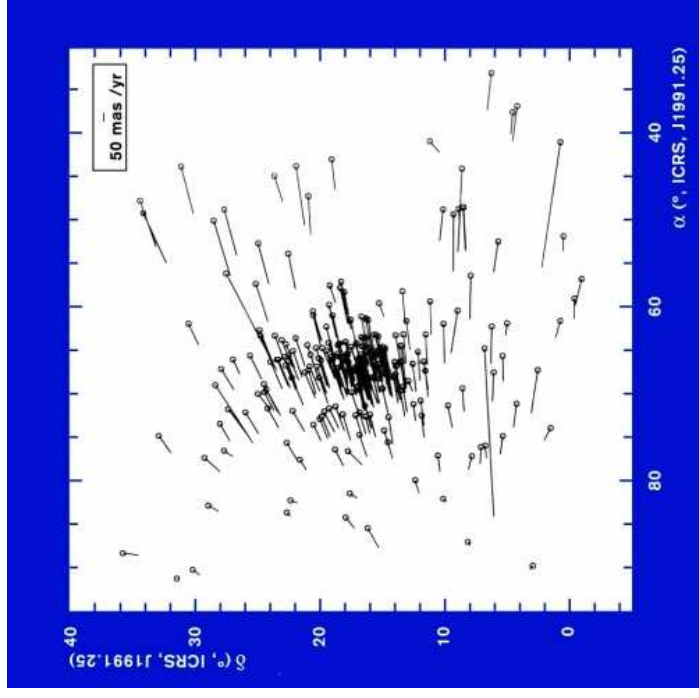


ESAM, Perryman

Development of the precision of astronomical position measurements



© Till Credner



Source: ESA



9-12

Moving Cluster

Perspective effect of spatial motion towards convergent point:

$$\tan \lambda = \frac{v_t}{v_r} = \frac{\mu d}{v_r} \quad (9.2)$$

$$\frac{d}{1 \text{ pc}} = \frac{v_r / (1 \text{ km/s}) \tan \lambda}{4.74 \mu / (1''/\text{a})} \quad (9.3)$$

Problem: determination of convergent point

Less error prone: moving cluster method = rate of variation of angular diameter of cluster:

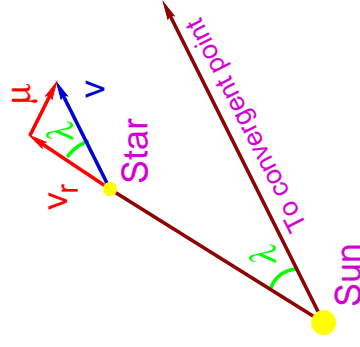
$$\dot{\theta} d = \theta v_r \quad (9.4)$$

Observation of proper motions gives

$$\frac{\dot{\theta}}{\theta} = \frac{d \mu_\alpha}{\mu_\alpha d} = \frac{d \mu_\delta}{\mu_\delta d} \quad (9.5)$$

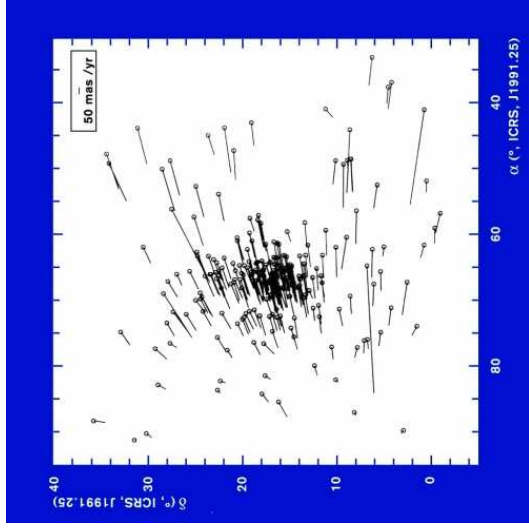
where $\mu_{\alpha, \delta}$ proper motion in α and δ . Therefore, from Eq. (9.4),

$$d = v_r \frac{\theta}{\dot{\theta}} \quad (9.6)$$





Moving Cluster



Source: ESA

Application: Distance to Hyades.
Tip of "arrow": Position of stars in 100000 years.
Hanson (1980) finds from this a distance of 46 pc
However: *Hipparcos*: geometric distance to Hyades is $d = 46.34 \pm 0.27$ pc from parallax measurements.
⇒ Moving cluster method only of historic interest.

Geometric Methods



Interlude

Parallax and Moving Cluster: geometrical methods.

All other methods (exception: light echoes): standard candles.

Requirements for standard candles (Mould, Kennicutt, Jr. & Freedman, 2000):

1. **Physical basis** should be understood.
2. Parameters should be measurable **objectively**.
3. **No corrections** ("fudges") required.
4. **Small intrinsic scatter** (⇒ requiring small number of measurements).
5. **Wide dynamic range** in distance.

Interlude



Magnitudes

Assuming isotropic emission, distance and luminosity are related ("inverse square law") ⇒ luminosity distance:

$$F = \frac{L}{4\pi d_L^2} \quad (9.7)$$

where F is the measured flux ($\text{erg cm}^{-2} \text{s}^{-1}$) and L the luminosity (erg s^{-1}).

Definition also true for flux densities, I_ν ($\text{erg cm}^{-2} \text{s}^{-1} \text{\AA}^{-1}$).

The magnitude is defined by

$$m = A - 2.5 \log_{10} F \quad (9.8)$$

where A is a constant used to define the zero point (defined by $m = 0$ mag for Vega).

For a filter with **transmission function** ϕ_ν ,

$$m_i = A_i - 2.5 \log \int \phi_\nu F_\nu d\nu \quad (9.9)$$

where, e.g., $i = U, B, V$.

Interlude



Magnitudes

To enable comparison of luminosities: define

absolute magnitude $M = \text{magnitude at distance } 10 \text{ pc}$

Thus, since $m = A - 2.5 \log(L/4\pi d^2)$,

$$M = m - 5 \log \left(\frac{d_L}{10 \text{ pc}} \right) \quad (9.10)$$

The difference $m - M$ is called the distance modulus, μ_0 :

$$\mu_0 = \text{DM} = m - M = 5 \log \left(\frac{d_L}{10 \text{ pc}} \right) \quad (9.11)$$

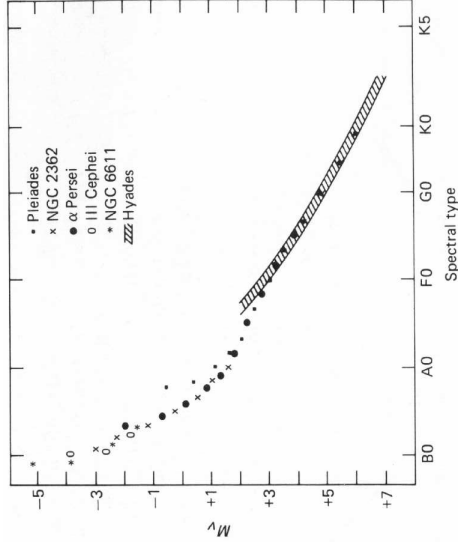
Often, distances are given in terms of $m - M$, and not in pc.

DM [mag]	3	5	10	15	20	25	30
d	40 pc	100 pc	1 kpc	10 kpc	100 kpc	1 Mpc	10 Mpc

Interlude



Main Sequence Fitting, I



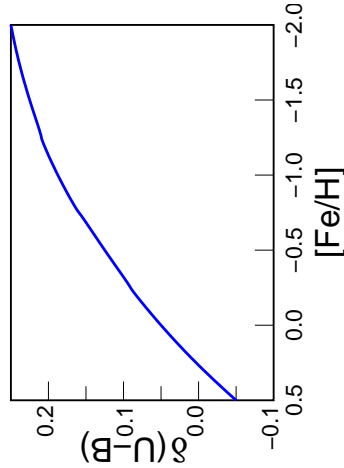
All open clusters are comparably young
 \Rightarrow Hertzsprung Russell Diagram (HRD) dominated by Zero Age Main Sequence (ZAMS).
 \Rightarrow Measure HRD (or Color Magnitude Diagram; CMD), shift magnitude scale until main sequence aligns \Rightarrow distance modulus.

after Rowan-Robinson (1985, Fig. 2.11)

Standard Candles: Galactic Distances



Main Sequence Fitting, II



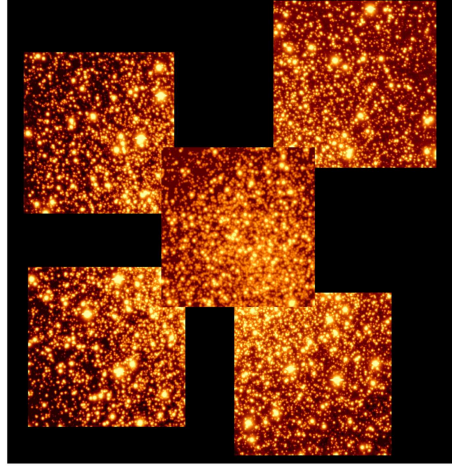
(after Rowan-Robinson, 1985, Fig. 2.12)

van den Bergh (1977): $Z_{\text{Hyades}} \sim 1.6 Z_{\odot}$, while other open clusters have solar metallicity \Rightarrow Cepheid DM were overestimated by 0.15 mag.

4. identification of unevolved stars crucial (evolution to larger magnitudes on MS during stellar life).

Currently: distances to ~ 200 open clusters known (Fenkart & Binggeli, 1979), limit ~ 7 kpc.

Standard Candles: Galactic Distances

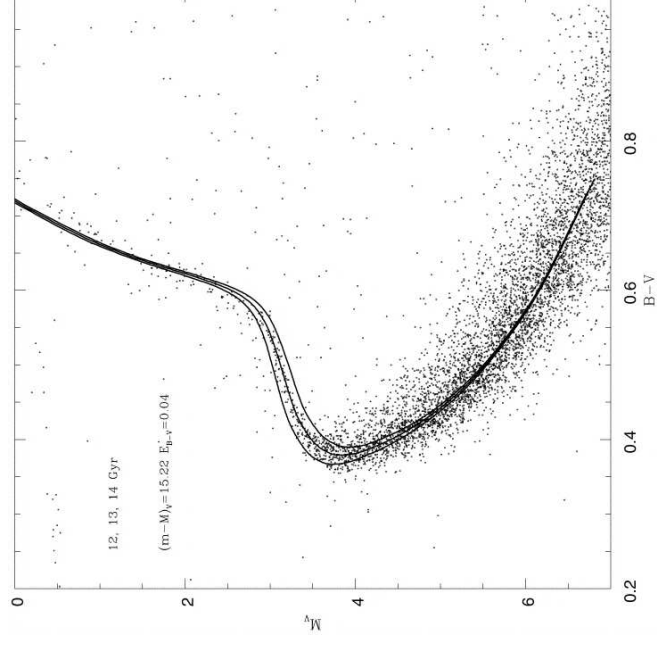


Globular Cluster NGC 6712

ESO PR Photo 06a/99 (18 February 1999)



© European Southern Observatory



Globular clusters: HRD different from open clusters:

- population II $\Rightarrow Z \ll Z_{\odot}$
- evolved

Use theoretical HRDs (isochrones) to obtain distance.

For distant clusters: MS unobservable

\Rightarrow position of horizontal branch.

(M68, Straniero, Chieffi & Limongi, 1997, Fig. 11)

**Baade-Wesselink**

Basic principle (Baade, 1926): Assume black body

- ⇒ Use color/spectrum to get kT_{eff}
- ⇒ Emitted intensity is Planckian, B_ν
- ⇒ Observed Intensity is $I_\nu \propto \pi R_*^2 \cdot B_\nu$.

Radius from integrating velocity profile of spectral lines:

$$R_2 - R_1 = p \int_1^2 v \, dt \quad (9.12)$$

(p : projection factor between velocity vector and line of sight).

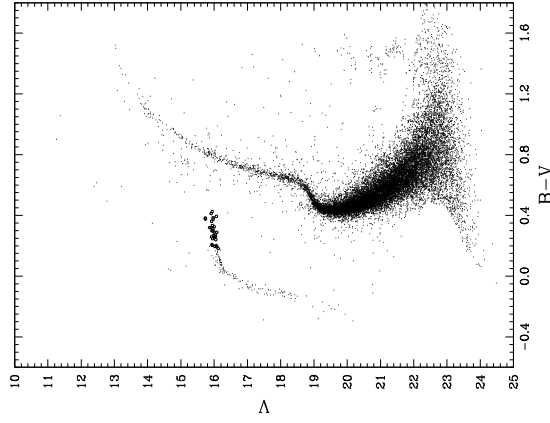
Wesselink (1947): Determine brightness for times of same color

- ⇒ rather independent of knowledge of stellar spectrum (deviations from B_ν).

Stars: Calibration using interferometric diameters of nearby giants.

Baade-Wesselink works for pulsating stars such as RR Lyr, Cepheids, Miras, and expanding supernova remnants.

Standard Candles: Galactic Distances

**RR Lyr**

RR Lyrae variables: Stars crossing instability strip in HRD
 ⇒ Variability ($P \sim 0.2 \dots 1$ d)
 ⇒ RR Lyr gap (change in color!).

Absolute magnitude of RR Lyr gap:

$$M_V = 0.6, M_B = 0.8 \text{ mag, i.e.,}$$

$$L_{RR} \sim 50 L_\odot.$$

M determined from ZAMS fitting, statistical parallax, and Baade-Wesselink method.

M2: Lee & Carney (1999, Fig. 2)

Standard Candles: Galactic Distances

**RR Lyr**

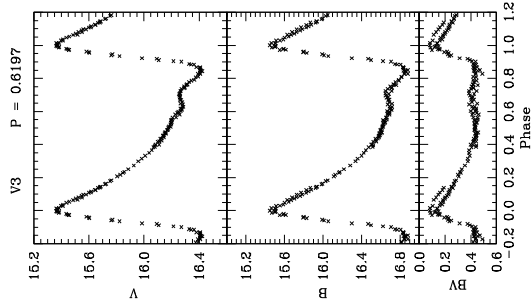
Lightcurve shows characteristic color variations over pulsation (temperature change!), and a fast rise, slow decay behavior.

RR Lyr in GCs show bimodal number distribution due to a metallicity effect:

- RRab with $P > 0.5$ d and most probable period of $P_{\text{ab}} \sim 0.7$ d, and
- RRC, with $P < 0.5$ d and $P_c \sim 0.3$ d.

M is larger for higher Z , i.e., metal-rich RR Lyr are fainter
 ⇒ difference in RR Lyr from population I and II.

RR Lyr work out to LMC and other dwarf galaxies of local group, however, used mainly for globular clusters.



(Lee & Carney, 1999, Fig. 5)

Standard Candles: Galactic Distances

**Interlude**

Previous methods: Selection of methods for distances within Milky Way (and Magellanic Clouds): Basis for extragalactic distance scale.

Primary extragalactic distance indicators: Distance can be calibrated from observations within Milky Way or from theoretical grounds.

Primary indicators usually work within our neighborhood (i.e., out to Virgo cluster at 15–20 Mpc).

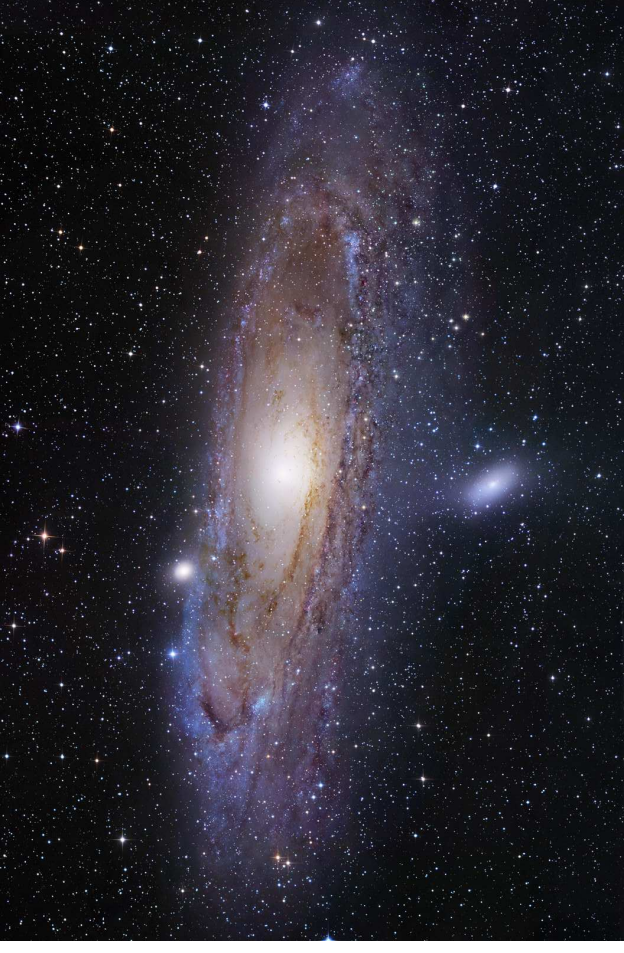
Examples: Cepheids, light echos, ...

Secondary extragalactic distance indicators: Distance calibrated from primary distance indicators.

Examples: Type Ia SNe, methods based on integral galaxy properties.

Interlude

700 kpc: M31 (Andromeda)

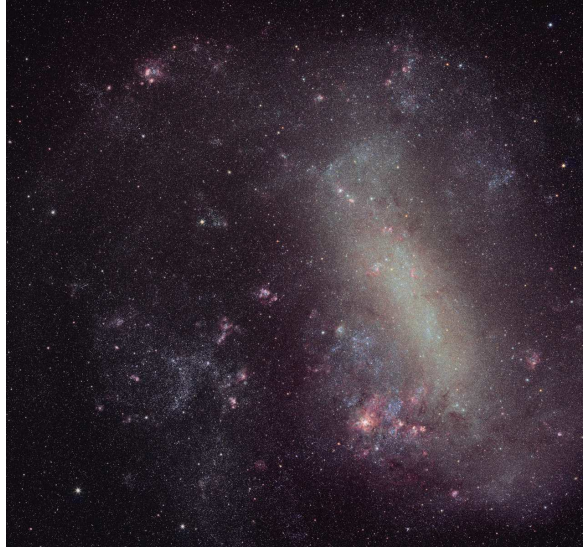


Robert Gendler

the largest astronomical picture ever taken, 21904 × 14454 pixels

To get a feel for the distances in our "neighborhood":

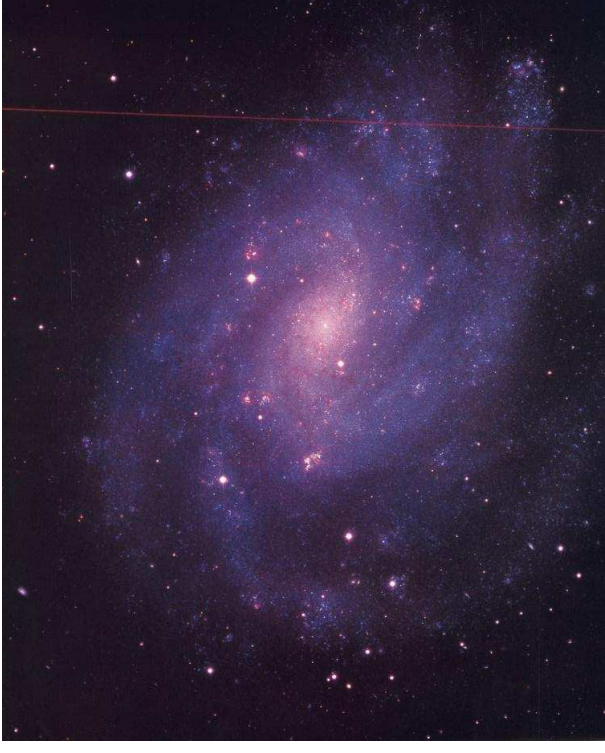
50 kpc: LMC, SMC, some other dwarf galaxies



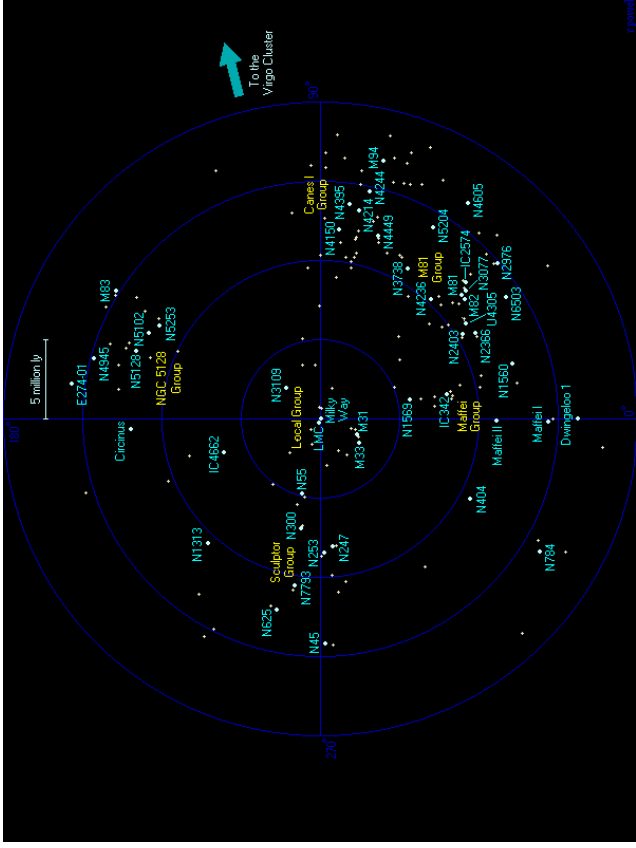
Loke Kun Tan

2–3 Mpc: Sculptor and M81 group

(groups similar to local group: a few large spirals, plus smaller stuff).



NGC 300 (Sculptor; Lautsen, Madsen, West, 1991)

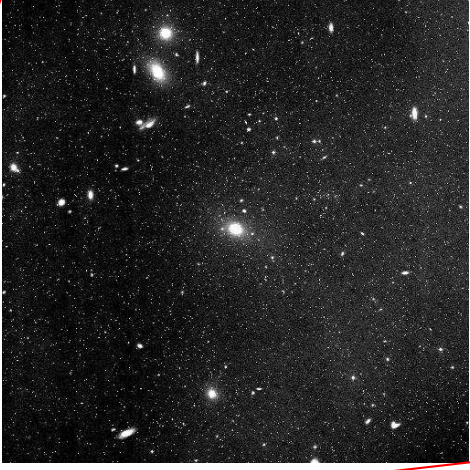
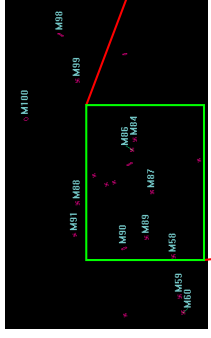


source: <http://www.atlasoftheuniverse.com/galgrps.html>

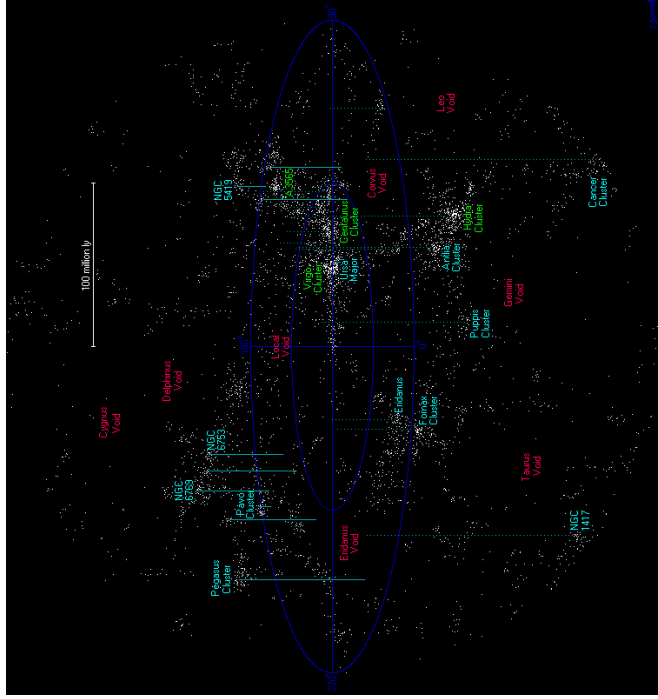
5–7 Mpc: M101 group (“pinwheel galaxy”). Important because of high L .



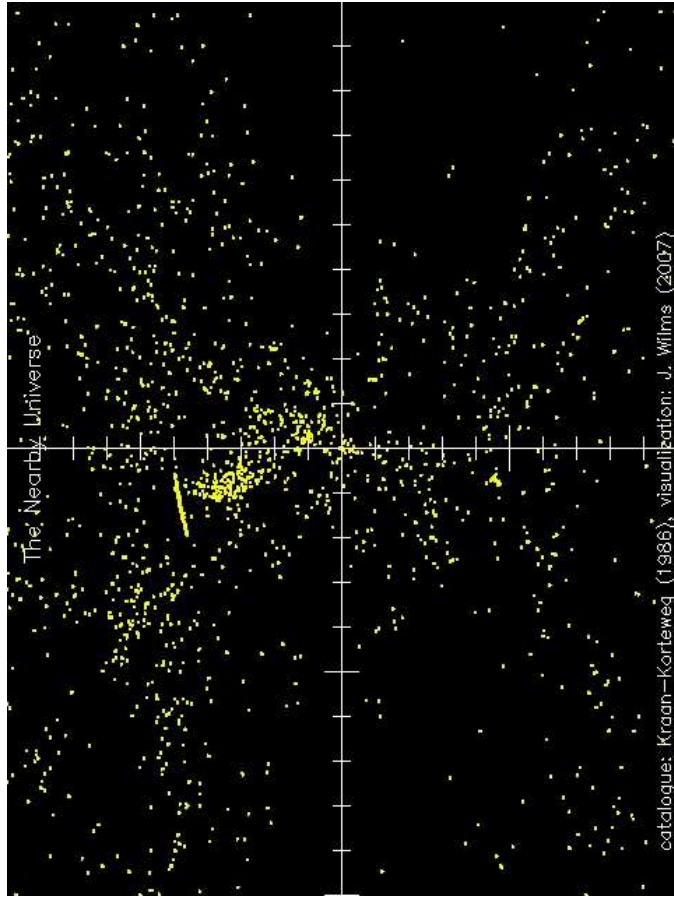
Adam Block/NOAO/AURA/NSF



15–20 Mpc: Virgo cluster.

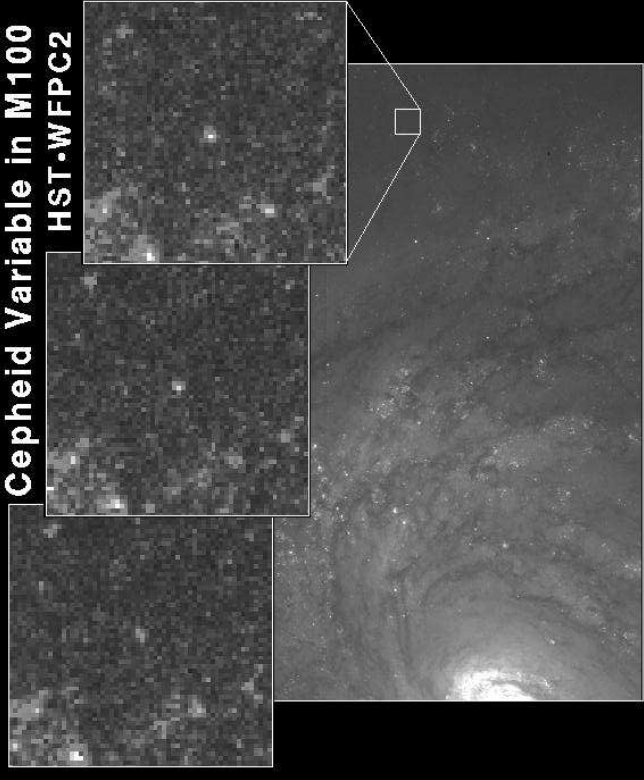


source: <http://www.atlasoftheuniverse.com/200mill.html>





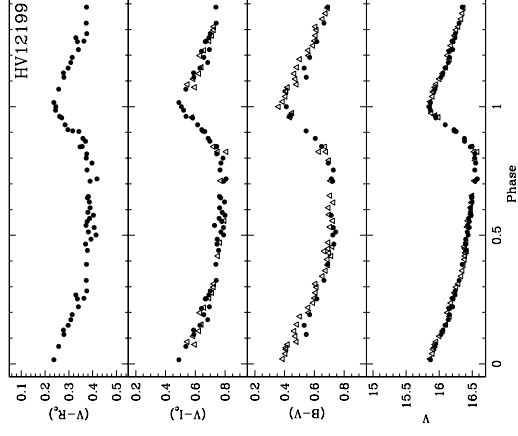
Cepheid Variable in M100 HST-WFPC2



STScI PR94-49

Cepheids, III

9-35



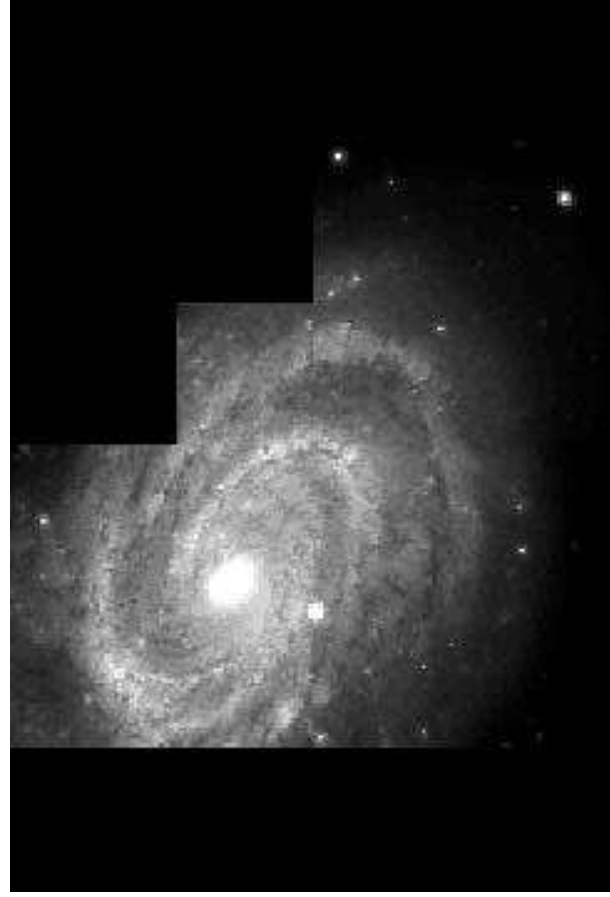
Cepheids:

- Luminous stars ($L \sim 1000 L_{\odot}$) in instability strip (He II-He III ionization)
 - **large intensity amplitude variation**,
 - $P \sim 2 \dots 150$ d (easily measurable).
- Review: Feast (1999).

(Gieren et al., 2000, Fig. 3)

Standard Candles: Extragalactic

3



STScI

Cepheids, IV

9-36



Henrietta Leavitt (1868–1921):

- Graduated from Radcliffe College
- from 1895: volunteer at Harvard Observatory
- was ill, and partially deaf as a result
- 1902: back at Harvard Obs
- discovered 1777 variable stars in LMC

© ASP

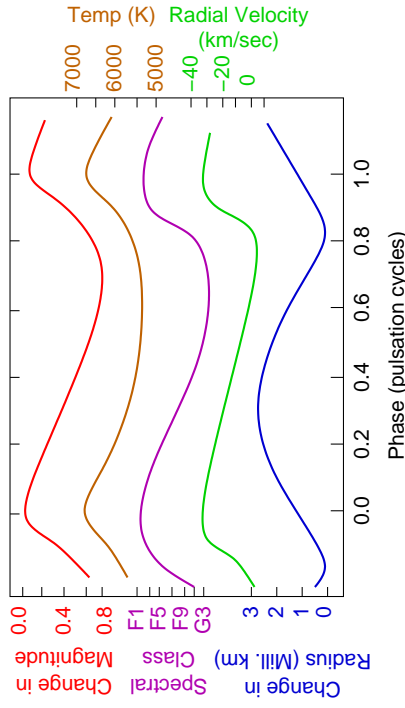
- 1912: discovered Period-Luminosity relation of Cepheids in SMC, but was not allowed to follow up on this
- later: defined Harvard photographic magnitude system
- died of cancer in 1921

Standard Candles: Extragalactic

4



Cepheids, VII



after <http://csep10.phys.utk.edu/astr162/lect/index.html>

Typical variation of measurable parameters over one pulsation.

Standard Candles: Extragalactic



Cepheids, VIII

Physics of Period-Luminosity-Color relation:

Star pulsates such that outer parts remain bound:

$$\frac{1}{2} \left(\frac{R}{P} \right)^2 \lesssim \frac{GM}{R} \implies \frac{M}{R^3} \propto P^{-2} \tag{9.13}$$

where P period. Therefore:

$$P \propto \rho^{-1/2} \iff P \rho^{1/2} = Q \tag{9.14}$$

(Q : pulsational constant, $\rho \propto MR^{-3}$ mean density). But Radius R related to luminosity L :

$$L = 4\pi R^2 \sigma T^4 \implies R \propto L^{1/2} T^{-2} \tag{9.15}$$

Inserting everything into Eq. (9.14) gives:

$$P L^{-3} T^3 = \text{const.} \iff \log P - 3 \log L + 3 \log T = \text{const.} \tag{9.16}$$

But: bolometric magnitude: $M_{\text{bol}} \propto -\log L$, and colors: $B - V \propto \log T$ such that

$$c_1 \log P + c_2 M_{\text{bol}} + c_3 (B - V) = \text{const.} \tag{9.17}$$

where $c_{1,2,3}$ calibration constants.

Standard Candles: Extragalactic

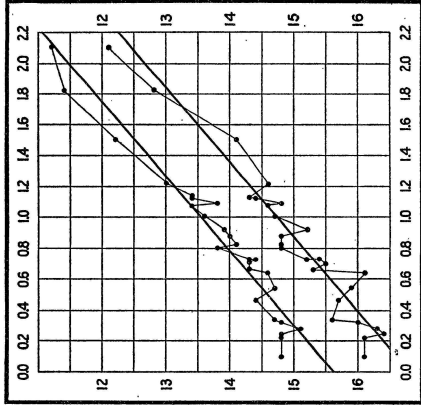


Fig. 2.

X-axis: period in days, Y-axis: magnitude

Leavitt & Pickering, 1912, Periods of 25 Variable Stars in the Small Magellanic Cloud, Harvard College Observatory Circular, vol. 173, pp. 1-3

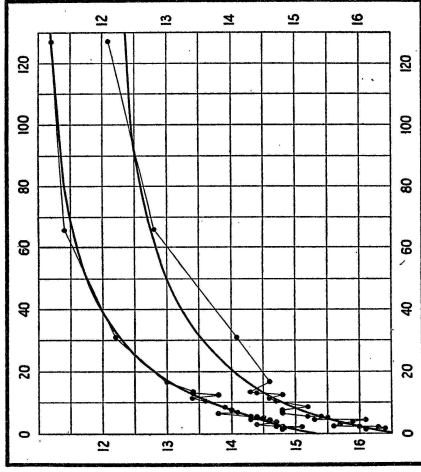


Fig. 1.



Cepheids, VI

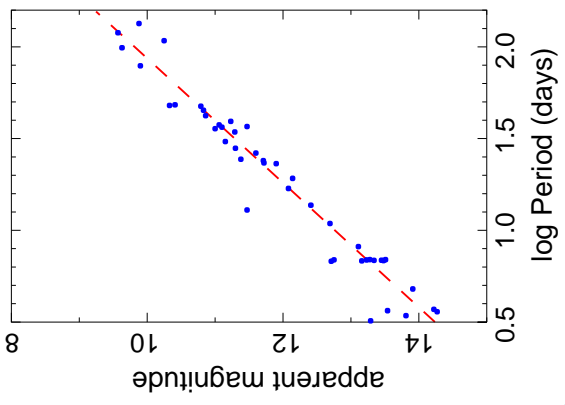
Period-Luminosity (PL) relation: $M_V \propto -2.76 \log P$.

Low luminosity Cepheids have lower periods.

There are indications that there is also an influence of the color

\implies Period-Luminosity-Color (PLC) relation

Note: W Vir stars, also called type II Cepheids = "little brother of Cepheids" (present in globular clusters). Less luminous than normal Cepheids, similar PLC relation, first confused with Cepheids \implies Cause for early thoughts of much smaller universe.



PL relation for the LMC Cepheids (after Mould, Kennicutt, Jr. & Freedman, 2000, Fig. 2).

Standard Candles: Extragalactic



Cepheids, IX

Calibration: Need **slope** and **zero point** of PLC.

Slope: Observations of nearby galaxies (e.g., open clusters in LMC)

Zero point is difficult:

- Cepheids in galactic clusters, distance to these via ZAMS fitting
 ⇒ problematic due to age dependency of ZAMS.
- Hipparcos: geometrical distances
 ⇒ problematic due to low SNR (resulting in 9% systematic error).
- Baade-Wesselink using IR info (low metallicity dependence).

Typical relations (Mould et al., 2000, 32 Cepheids):

$$M_V = -2.76 \log P - 1.40 + C(Z) \quad (9.18)$$

$$M_I = -3.06 \log P - 1.81 + C(Z)$$

The metallicity (color) dependence is roughly

$$(m - M)_{\text{true}} = (m - M)_{\text{PL}} - \gamma \log Z / Z_{\text{LMC}} \quad (9.19)$$

where $\gamma = -0.11 \pm 0.03 \text{ mag/dex}$ (Z : metallicity) (=Cepheids with larger Z are fainter).

Standard Candles: Extragalactic



Cepheids, X

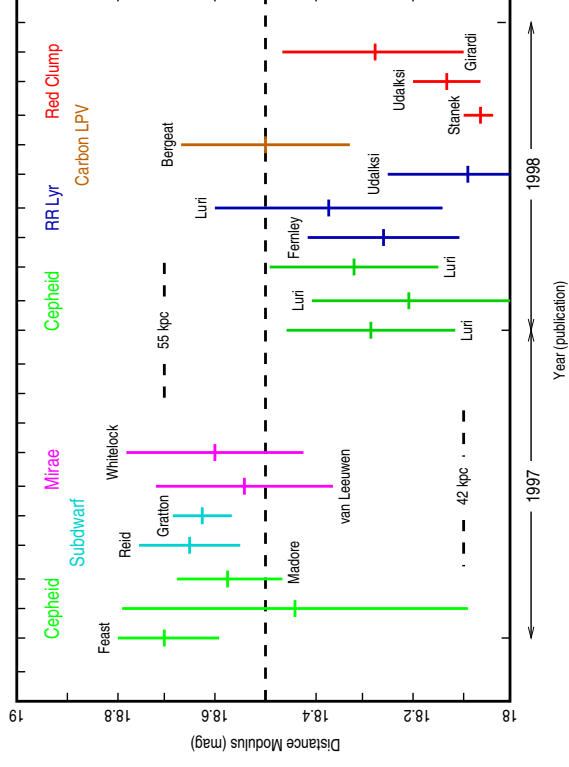
Notes:

1. Is the pulsational constant a constant? (or is $Q = Q(\rho, P)$?)
 ⇒ possible deviation from PLC, especially at high luminosity
 ⇒ adds uncertainty at large distances.
2. M_V depends on metallicity
 ⇒ LMC Cepheids are bluer [$Z_{\text{LMC}} < Z_{\odot}$], but the exact value of γ in Eq. (9.19) is very uncertain.

For V and I magnitudes, most probably $\delta(m - M)_{\text{O}} / \delta[\text{O}/\text{H}] \lesssim -0.4 \text{ mag dex}^{-1}$, however, others find $+0.75 \text{ mag dex}^{-1}$, see Ferrarese et al. (2000) for details...

3. Stellar evolution unclear (multiple crossings of instability strip are possible).

Standard Candles: Extragalactic



LMC distance:
 “anchor point” of
 extragalactic
 distance scale.

After Gaia
 Workgroup

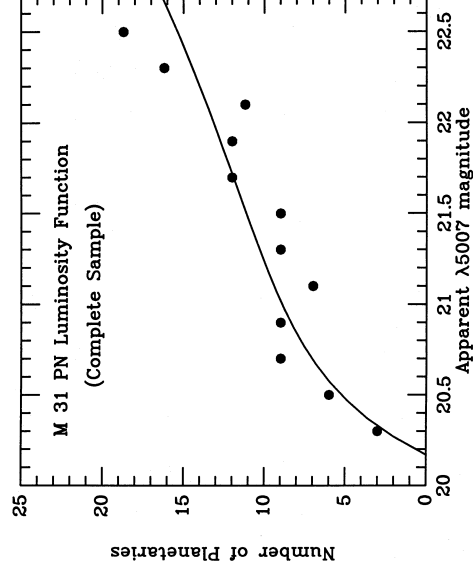
Strong dependence on Hipparcos calibration.

DM ranges between $18.7 \pm 0.1 \text{ mag}$ (Feast & Catchpole) and $18.57 \pm 0.11 \text{ mag}$ (Madore & Freedman)

Currently, the distance to the LMC is less well known than desirable.



PN Luminosity Function, I



Planetary Nebulae have
 empirical universal
 luminosity function.

Measurement of “cutoff
 magnitude” M_{PN}

⇒ Standard candle!
 PN detection with narrow band
 filter of $\text{O}[\text{III}]\lambda 5007\text{\AA}$.

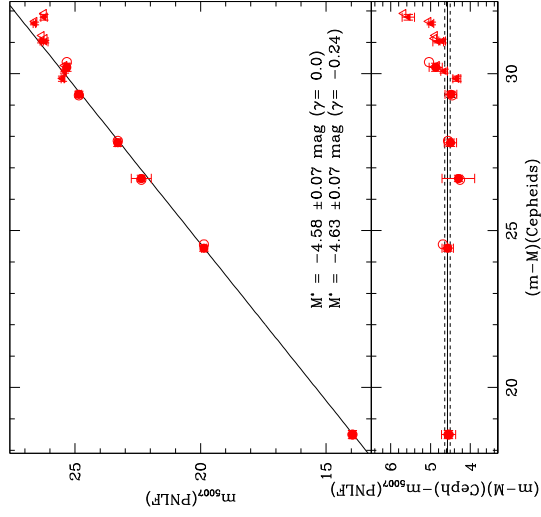
(Ciardullo et al., 1989, Fig. 4)

$$N(M) \propto e^{0.307M} (1 - e^{3(M_{\text{PN}} - M)}) \quad (9.20)$$

Standard Candles: Extragalactic



PN Luminosity Function, II



Result of calibration using Cepheid distances (Ferrarese et al., 2000):

Cutoff of luminosity function:

$$M_{\text{PN}} = -4.58 \pm 0.13 \text{ mag} \quad (9.21)$$

Works out to ~ 40 Mpc with 8 m class telescope.

(Ferrarese et al., 2000, Fig. 3), left to right: LMC, M31, NGC 300, M81, M101, NGC 3368, and several galaxy groups.

Standard Candles: Extragalactic

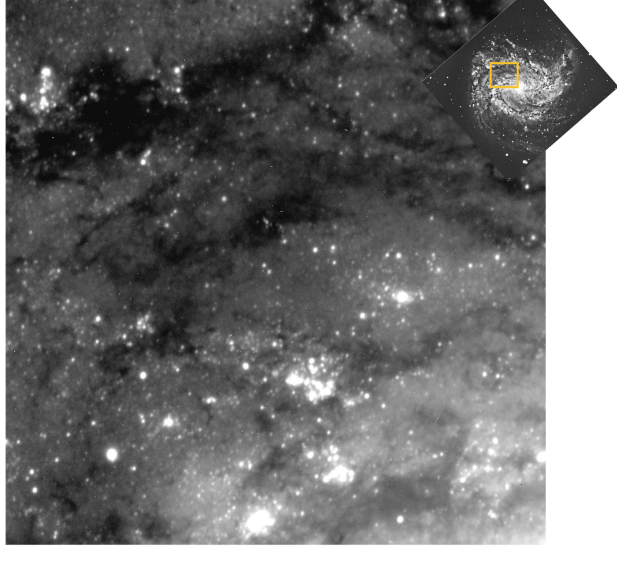


PN Luminosity Function, III

Caveats: Effects of metallicity, population age, parent galaxy most probably small, but

- Contamination by H II regions (but distinguish using $H\alpha/[O III]$ ratio.
- Background emission-line galaxies at $z \approx 3.1$
- intracluster PNe (i.e., PNe outside galaxies)

Standard Candles: Extragalactic



The VLT Looks Deep into a Spiral Galaxy



ESO PR Photo 20/98 (23 June 1998)

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Brightest Stars, II

Brightest Stars= O, B, A supergiants, absolute magnitudes usable in local group, although there is a large scatter.

Reason: there is an upper limit to stellar luminosity due to mass loss in supergiants.

Possible Improvement: Strength of Balmer series lines. $H\alpha$ and $H\beta$ appear biased (class of supergiants with anomalously strong Balmer lines?).

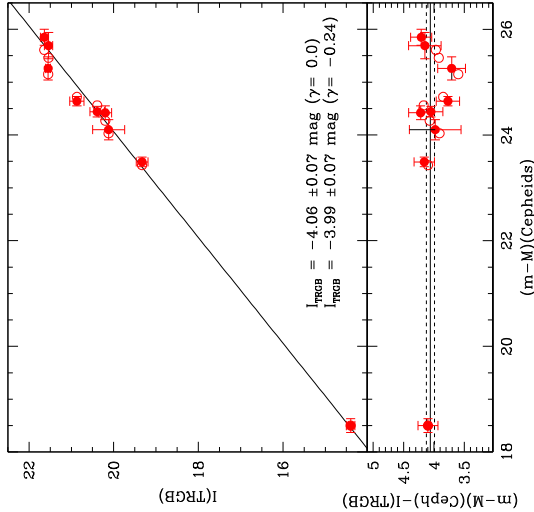
Problems:

- Contamination by foreground halo stars
 - ⇒ Choose stars with unusual color (rare, i.e. less foreground contamination): $B - V < 0.4$ or $B - V > 2.0$ ⇒ Tip of Red Giant Branch
- Internal extinction.
- Scatter in max. L
 - ⇒ Average over brightest N stars (Sandage, Tammann: $N = 3$).
- Metallicity dependence.

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Brightest Stars, III



Tip of Red Giant Branch: Usable within local group, possibly out to Virgo.

Calibration:

$$M_T = -4.06 \pm 0.13 \text{ mag} \quad (9.22)$$

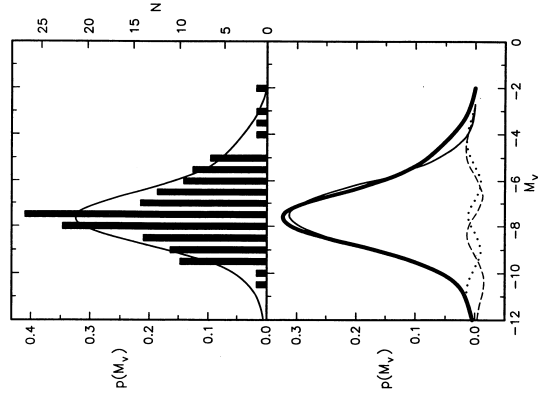
(Ferrese et al., 2000, Fig. 1)

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Globular Clusters



Globular Cluster Luminosity Function is \sim Gaussian
 \Rightarrow Use maximum of distribution ("turnover magnitude", M_T) as standard candle.
 From Virgo and Fornax Cepheid distances (Ferrese et al., 2000):

$$M_{T,V} = -7.60 \pm 0.25 \text{ mag} \quad (9.23)$$

Caveats:

1. M_T depends on luminosity and type of host galaxy (GC of dwarf galaxies weaker by ~ 0.3 in V).
2. Metallicity of galaxy cluster influences M_T .
3. Measurement difficult (need the weak GCs).
4. Large scatter in data \Rightarrow Method rather unreliable.

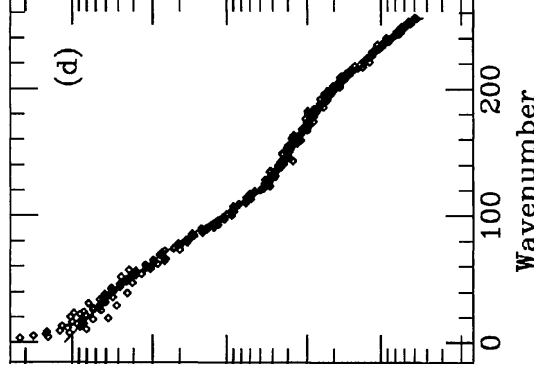
(MW GCs, Abraham & van den Bergh, 1995, Fig. 1)

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Surface Brightness Fluctuations, I



For early type galaxies: Assume N stars in picture element (pixel), with average flux f each.

$$\Rightarrow \text{Mean pixel intensity: } \mu = Nf \quad (9.24)$$

independent of distance, since $N \propto r^2$ and $f \propto r^{-2}$.
 Standard deviation between pixels (Poisson):

$$\sigma = \sqrt{N}f \propto r^{-1} \quad (9.25)$$

and therefore

$$f = \frac{\sigma^2}{\mu} = \frac{L}{4\pi r^2} \quad (9.26)$$

which gives the distance r .

Review: Blakeslee, Aljar & Tonry (1999).

Complication: Adjacent pixels not independent (point spread function of telescope)

\Rightarrow Use radial power spectrum to obtain σ^2 and μ .

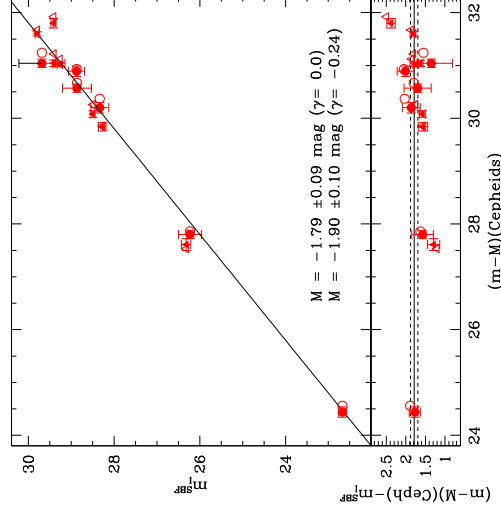
(Aljar et al., 1997, Fig. 3d)

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Surface Brightness Fluctuations, II



Luminosity of galaxy dominated by Red Giant Branch stars
 \Rightarrow Strong wavelength and color dependence
 \Rightarrow Primary calibration: I-band plus broad-band color dependency to give standard candle.

Often also used: HST WFPC2 plus F814W filter (close to I-band),

$$M_{\text{F814W}} = (-1.70 \pm 0.16) + (4.5 \pm 0.3)[(V-I)_0 - 1.15] \quad (9.27)$$

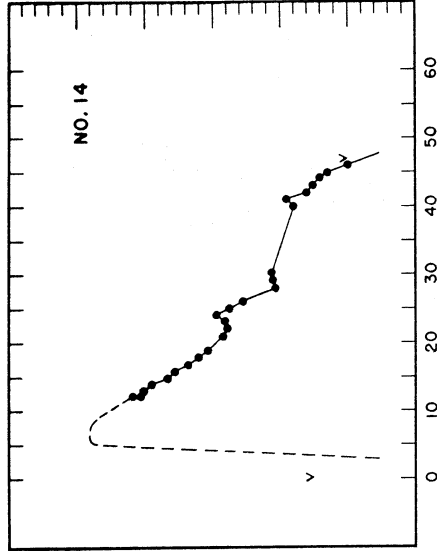
Works out to ~ 70 Mpc with HST. (Ferrese et al., 2000, Fig. 5)

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Novae, I



"classical nova" = explosion on surface of white dwarf
 Novae only in binary systems
 \Rightarrow slow accretion of material onto WD
 \Rightarrow outer skin reaches M_{crit} for fusion
 \Rightarrow explosion
 \Rightarrow ejection of $10^{-6} \dots 10^{-4} M_{\odot}$ with $v \sim 500 \text{ km s}^{-1}$
 Explosion produces characteristic lightcurve.

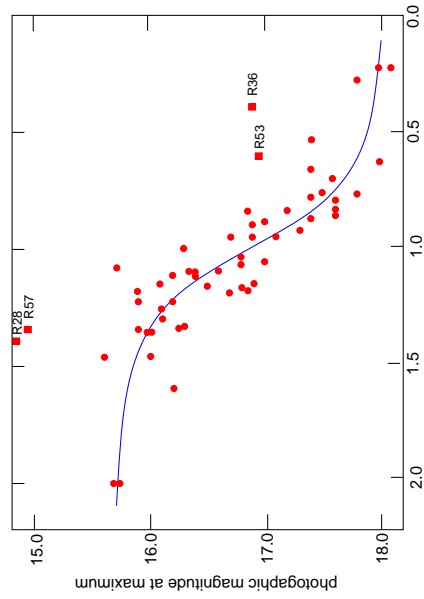
(Nova in M31, Arp, 1956, p. 18)

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Novae, II



(after van den Bergh & Pritchett, 1986, Fig. 1).

Strong scatter in lightcurves (higher $L_{\text{max}} \Rightarrow$ faster decline, but typically $\sim 3 \times$ brighter than Cepheids), but good Correlation luminosity vs. decline timescale (t_i , time to reach $m(t_i) = m_{\text{max}} + i$). Calibration: galactic novae.

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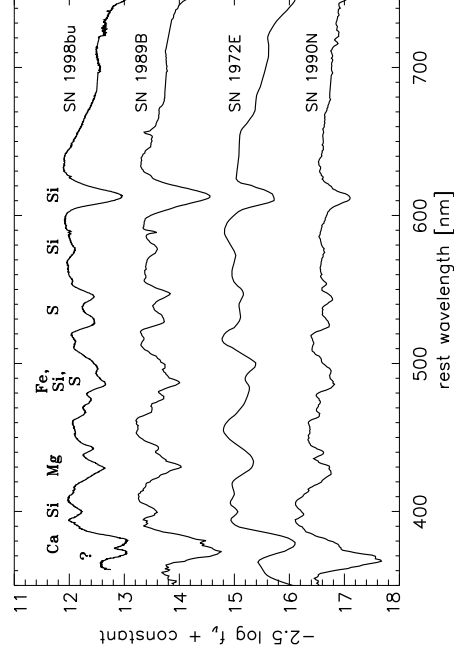


Supernovae have luminosities comparable to whole galaxies:
 $\sim 10^{51} \text{ erg s}^{-1}$ in light,
 $100 \times$ more in neutrinos.

SN1994d (HST WFPC)



Type Ia Supernovae, II



Different supernovae can have very similar spectra.



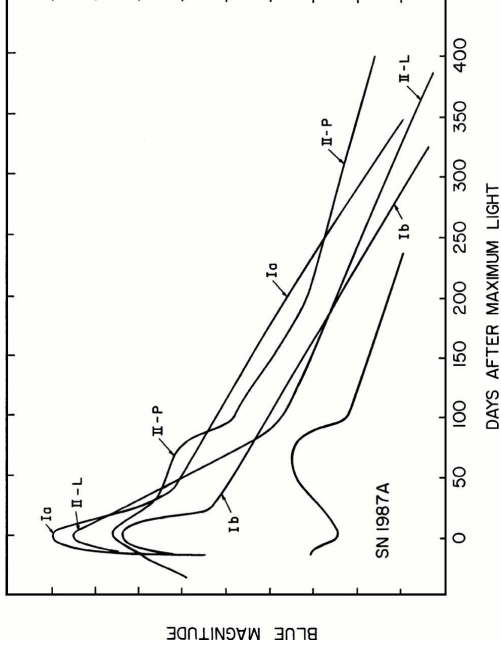
Allows their classification.

(Spectra of several SNe at maximum light Jha et al., 1999, Fig. 6)

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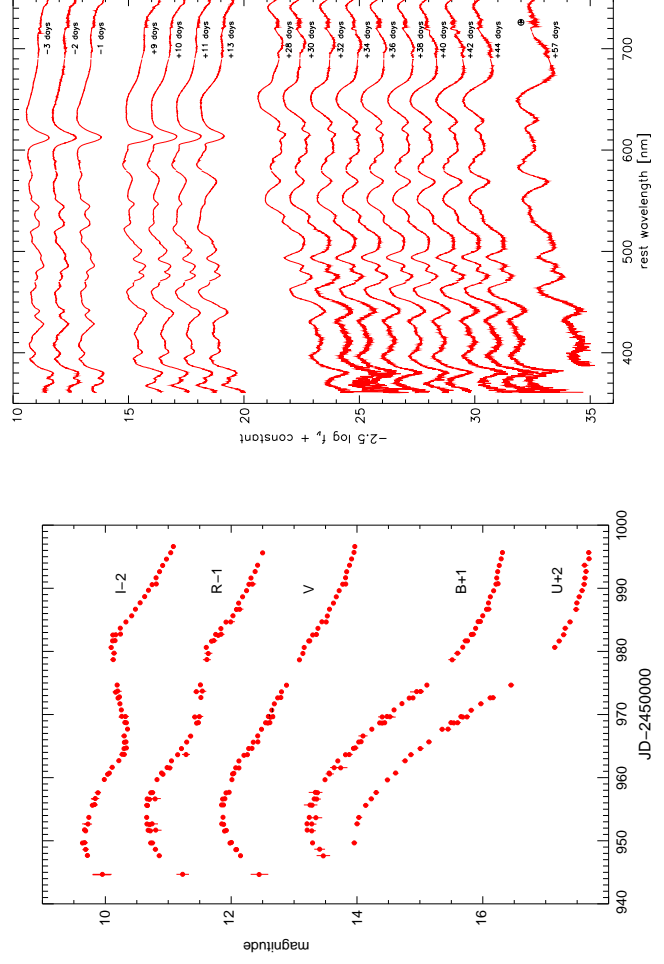
Type Ia Supernovae, V



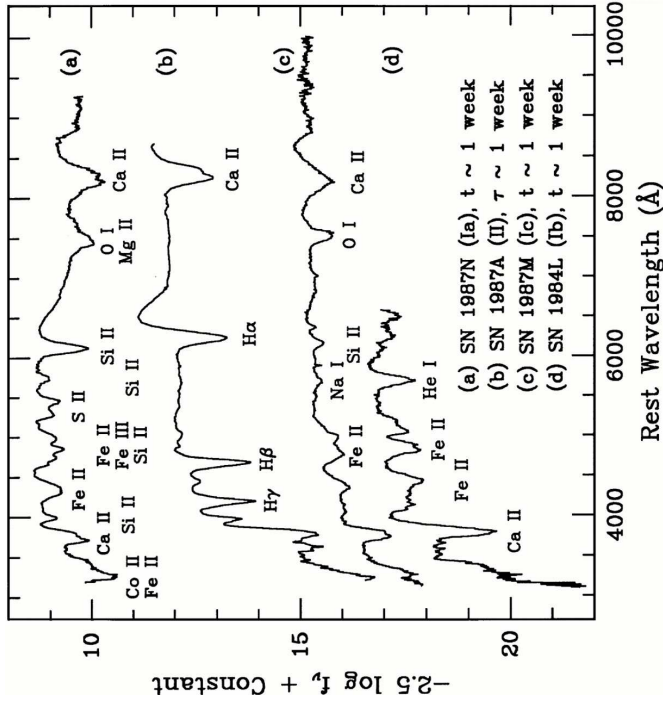
Light curves of SNe I all very similar, SNe II have much more scatter. SNe II-L ("linear") resemble SNe I SNe II-P ("plateau") have const. brightness to within 1 mag for extended period of time.

(Filippenko, 1997, Fig. 3)

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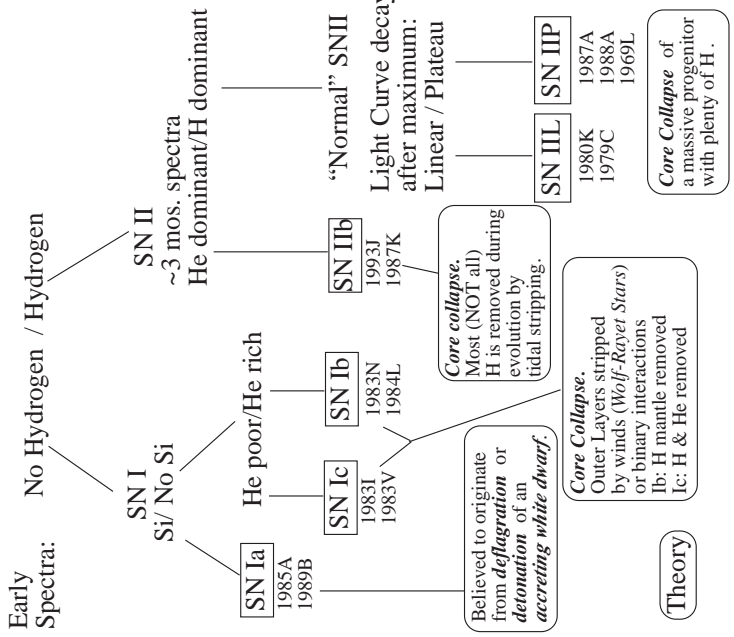
(SN 1998bu in M96, Jha et al., 1999, Figs. 2 and 4)



(Filippenko, 1997, Fig. 1); t : time after maximum light; τ : time after explosion; P Cyg profiles give $v \sim 10000 \text{ km s}^{-1}$

Rough classification (Minkowski, 1941):
Type I: no hydrogen in spectra;
 subtypes Ia, Ib, Ic
Type II: hydrogen present, subtypes II-L, II-P

Note: pre 1985 subtypes Ia, Ib had different definition than today \implies beware when reading older texts.



Type Ia Supernovae, VII

Clue on origin from supernova statistics:

- SNe II, Ib, Ic: never seen in ellipticals; rarely in S0; generally associated with spiral arms and H II regions.
- ⇒ progenitor of SNe II, Ib, Ic: massive stars ($\gtrsim 8 M_{\odot}$) ⇒ core collapse
- SNe Ia: all types of galaxies, no preference for arms, almost no scatter in lightcurves
- ⇒ progenitor of SNe Ia: accreting carbon-oxygen white dwarfs, undergoing thermonuclear runaway

Rule of thumb: 1...3 SNe per galaxy and per century

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Type Ia Supernovae, IX

SN Ia = Explosion of CO white dwarf when pushed over Chandrasekhar limit ($1.4 M_{\odot}$) (via accretion?).

- ⇒ Always similar process
- ⇒ Very characteristic light curve: fast rise, rapid fall, exponential decay ("FRED") with half-time of 60 d.
- 60 d time scale from radioactive decay $Ni^{56} \rightarrow Co^{56} \rightarrow Fe^{56}$ ("self calibration" of lightcurve if same amount of Ni^{56} produced everywhere).

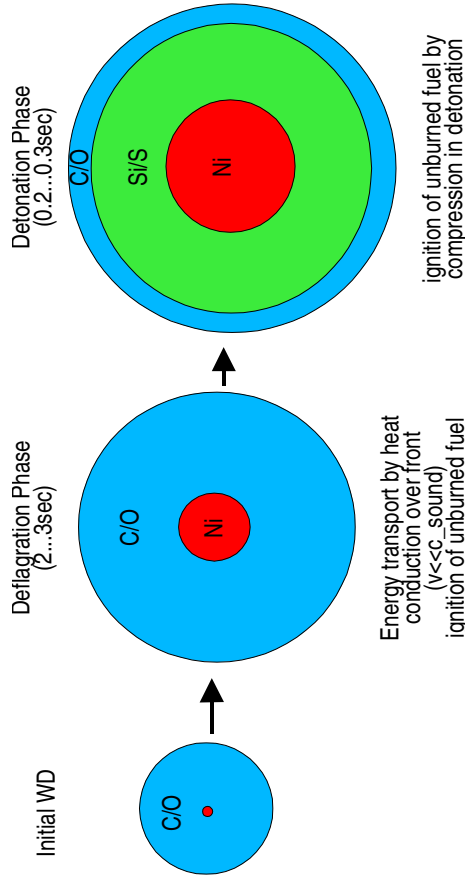
Calibration: SNe Ia in nearby galaxies where Cepheid distances known.
At maximum light:

$$M_B = -18.33 \pm 0.11 + 5 \log h_{100} \quad (L \sim 10^{9...10} L_{\odot}) \quad (9.28)$$

Intrinsic dispersion: $\lesssim 0.25$ mag (possibly due to size of clusters analyzed?!?)
Observable out to 1000 Mpc

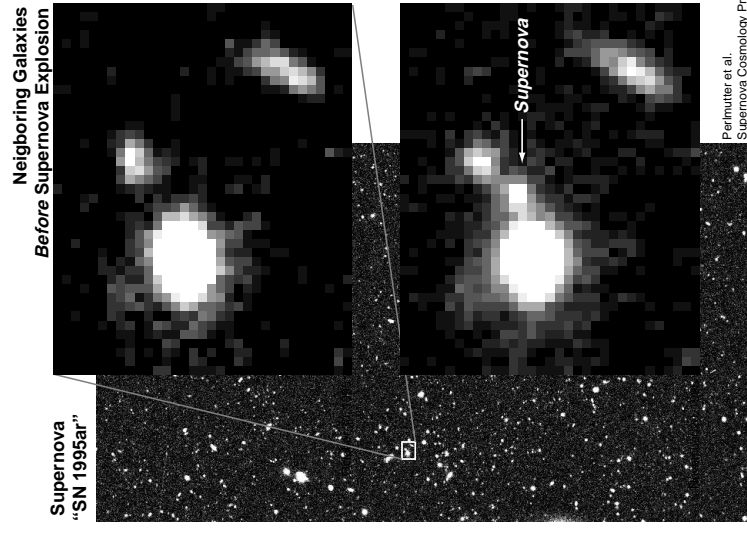
Standard Candles: Extragalactic

Type Ia Supernovae, VIII

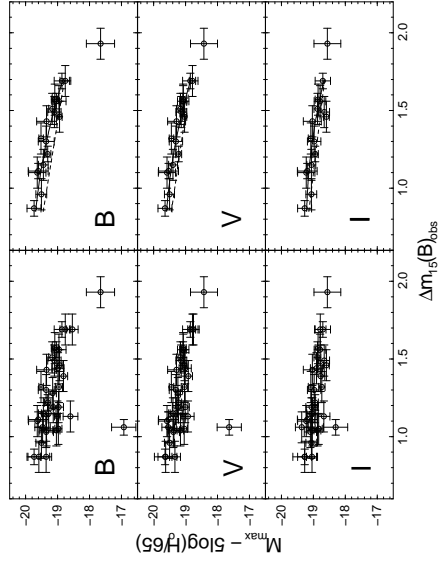


after P. Höflich

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Type Ia Supernovae, XI



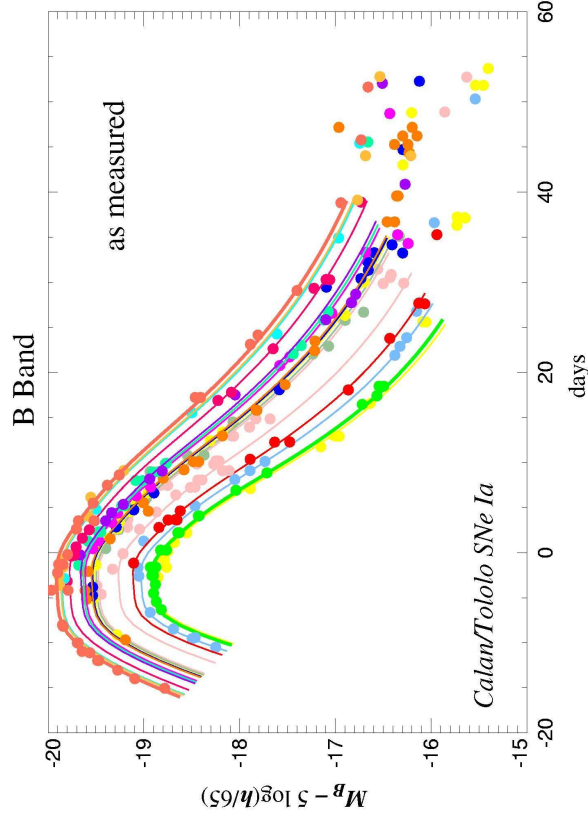
(Phillips et al., 1999, Fig. 8)

Caveats:

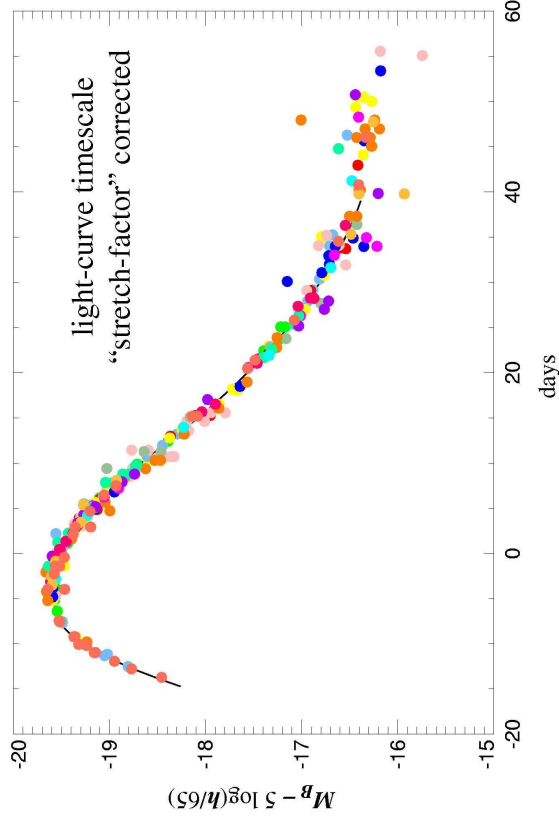
1. Are they really identical?
 ⇒ history of pre-WD star?
2. Correction for extinction in parent galaxy difficult.
3. Baade-Wesselink for calibration Eq. (9.28) depends crucially on assumed $(B - V) - T_{\text{eff}}$ relation.
4. Some SN Ia spectroscopically peculiar ⇒ Do not use these!
5. Decline rate and color vary, but max. brightness and decline rate correlate (see figure).

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Lightcurves of Hamuy et al. SN Ia sample (18 SNe discovered within 5 d past maximum, with $3.6 < \log cz < 4.5$, i.e., $z < 0.1$)



Kim, et al. (1997)

Lightcurves of Hamuy et al. SN Ia sample (18 SNe discovered within 5 d past maximum, with $3.6 < \log cz < 4.5$, i.e., $z < 0.1$), after correction of systematic effects and time dilatation (Kim et al., 1997).



Type Ia Supernovae, XIV

Recalibration of SN Ia distances with Cepheids gives (Gibson et al., 2000):

$$\log H_0 = 0.2 \left\{ M_B^{\text{max}} - 0.720 (\pm 0.459) \cdot [\Delta m_{B,15,t} - 1.1] - 1.010 (\pm 0.934) \cdot [\Delta m_{B,15,t} - 1.1]^2 + 28.653 (\pm 0.042) \right\} \quad (9.29)$$

where

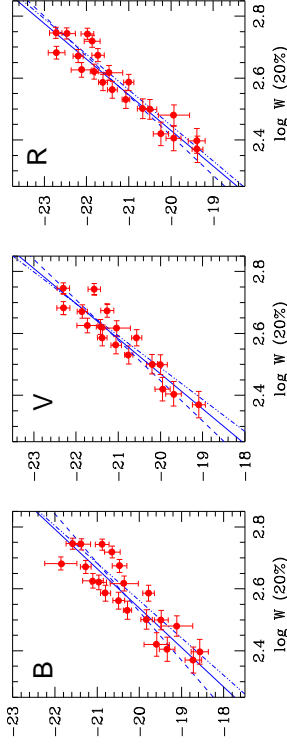
$$\Delta m_{B,15,t} = \Delta m_{B,15} + 0.1E(B - V) \quad (9.30)$$

where

$\Delta m_{B,15}$: observed 15 d decline rate,
 $E(B - V)$: total extinction (galactic+intrinsic).

Eq. (9.29) valid for B-band, equivalent formulae exist for V and I.

Overall, the calibration is good to better than 0.2 mag in B.

**Tully-Fisher, I**

(after Sakai et al., 2000, Fig. 1)

Tully-Fisher relation for spiral galaxies: Width of 21 cm line of H correlated with galaxy luminosity:

$$M = -a \log \left(\frac{W_{20}}{\sin i} \right) - b \quad (9.31)$$

where W_{20} : 20% line width (km s^{-1}); typically $W_{20} \sim 300 \text{ km s}^{-1}$, i inclination angle.

For the B- and I-Bands (Sakai et al., 2000):

	B	I
a	7.97 ± 0.72	9.24 ± 0.75
b	19.80 ± 0.11	21.12 ± 0.12

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**Tully-Fisher, II**

Qualitative Physics: Line width related to mass of galaxy. $W/2 \sim V_{\text{max}}$, where

V_{max} max. velocity of rotation curve

\implies Assume $M/L = \text{const.}$ (good assumption)

\implies width related to luminosity.

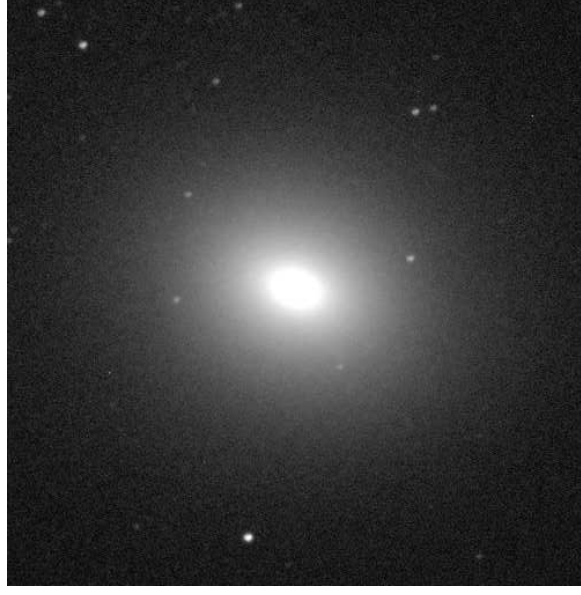
Detailed physical basis unknown. Might be related to galaxy formation ("hierarchical clustering", see later).

I-band is better (less internal extinction).

Caveats:

1. Determination of inclination i .
2. Influence of turbulent motion within galaxy.
3. Constants dependent on galaxy type (Sa and Sb similar, Sc more luminous by factor of ~ 2).
4. Optical extinction.
5. Intrinsic dispersion ~ 0.2 mag.
6. Barred Galaxies problematic.

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"Faber-Jackson" law for elliptical galaxies:

The luminosity L of an elliptical galaxy scales with its intrinsic velocity dispersion, σ , as $L \propto \sigma^4$.

Note that ellipticals have virtually no Hydrogen

\implies cannot use 21 cm.

M32 (companion of Andromeda),

courtesy W. Keel

Ellipticals: $M_B = -19.38 \pm 0.07 - (9.0 \pm 0.7)(\log \sigma - 2.3)$ (9.32)

Lenticulars (Type S0): $M_B = -19.65 \pm 0.08 - (8.4 \pm 0.8)(\log \sigma - 2.3)$ (9.33)

 **D_n - σ**

The Faber-Jackson law is a specialized case of the more general D_n - σ -relation:

The intensity profile of an elliptical galaxy is given by de Vaucouleurs' $r^{1/4}$ law:

$$I(r) = I_0 \exp \left(-\left(\frac{r}{r_0} \right)^{1/4} \right) \implies L = \int I \propto I_0 r_0^2 \quad (9.34)$$

Because of the virial theorem ($E_{\text{kin}} = -E_{\text{pot}}/2$):

$$\frac{1}{2} m \sigma^2 = G \frac{m M}{r_0} \iff \sigma^2 \propto \frac{M}{r_0} \quad (9.35)$$

where σ : velocity dispersion.

Assume a mass-to-light ratio

$$M/L \propto M^\alpha \quad (9.36)$$

($\alpha \sim 0.25$), and use r_0 from Eq. (9.34) to obtain

$$L^{1+\alpha} \propto \sigma^{4-4\alpha} I_0^{\alpha-1} \quad (9.37)$$

This is called the "fundamental plane" relationship (Dressler et al., 1987).

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 **D_n - σ**

Observational version of the fundamental plane relationship: Instead of inserting r_0 and I_0 , measure diameter D_n of aperture to reach some mean surface brightness (typically sky brightness, 20.75 mag arcsec⁻² in B), and use calibration.

Note: Assumptions are

1. M/L same everywhere.
2. ellipticals have same stellar population everywhere

Calibration paper: Kelson et al. (2000).

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**Path to H_0**

To obtain H_0 , we need distances, and redshifts.

Redshifts: Trivial

Distances: Hubble Space Telescope Key Project on Extragalactic Distance Scale.

Summary paper: Freedman et al. (2001), there are a total of 29 papers on the HST key project!

Strategy:

1. Use high-quality candles: Cepheid variables as primary distance calibrator.
2. Calibrate secondary calibrators that work out to $cz = 10000 \text{ km s}^{-1}$:
 - Tully-Fisher,
 - Type Ia Supernovae,
 - Surface Brightness Fluctuations,
 - Fundamental-plane for Ellipticals.
3. Combine uncertainties from these methods.

Hubble Constant

1

**Velocity Field, I**

Before determining H_0 : correct for influence of velocity field (cluster motion with respect to comoving coordinates).

The observed redshift is given by

$$1 + z = (1 + z_R) \left(1 - \frac{v_0}{c} + \frac{v_G}{c} \right) \quad (9.38)$$

where

v_0 : observer's radial velocity in direction of galaxy

v_G : radial velocity of the galaxy, difficult to find

z_R : cosmological redshift

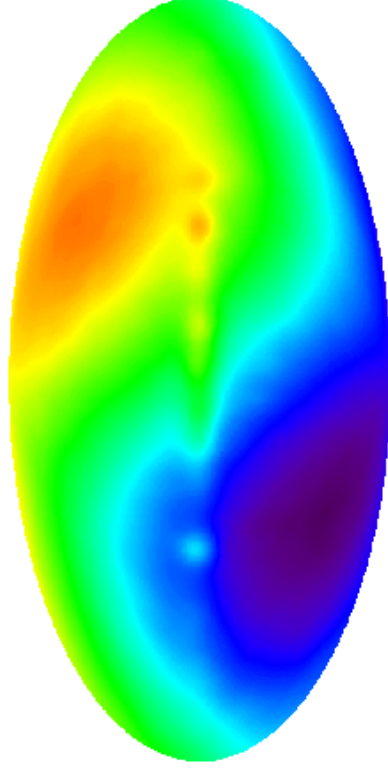
Older galaxy catalogues often attempt to correct the measured values of z to produce "corrected redshifts", e.g., by setting $v_G = 0$ and

$$1 + z = (1 + z_R) \left(1 + \frac{v_0}{c} \right) \sim 1 + z_R - \frac{v_0}{c} \implies z_R \sim z + \frac{v_0}{c} \quad (9.39)$$

since v_0 was not well known before COBE \implies introduces unnecessary problems \implies correction not used in recent redshift surveys! (see Harrison & Noonan, 1979, for details)

Hubble Constant

2



(COBE DMR; Bennett et al., 1996)

v_0 is easy to find \implies Measure velocity of Earth with respect to 3K radiation. COBE finds $\Delta T = 3.353 \pm 0.024 \text{ mK}$ of 3K black-body spectrum of $T = 2.725 \pm 0.020 \text{ K}$, using $\Delta T/T = v/c$.

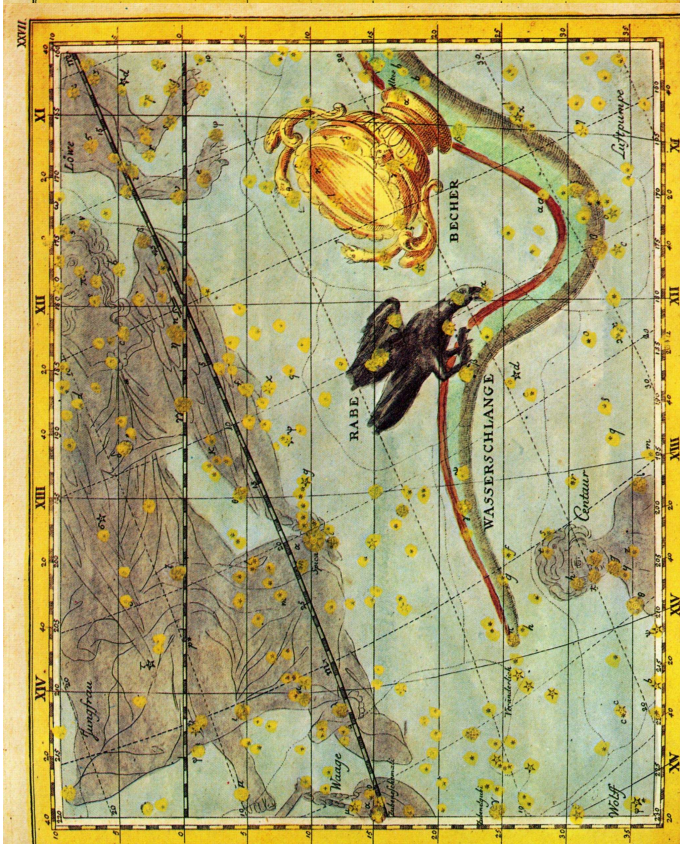
$$v_0 = (369.1 \pm 2.6) \text{ km s}^{-1} \cdot \cos \theta_{\text{CMB}} \quad (9.40)$$

where $\theta_{\text{CMB}} = \angle(v, v_{\text{CMB}})$, and v_{CMB} points towards

$$(l, b) = (264^\circ 26' \pm 0^\circ 33', 48^\circ 22' \pm 0^\circ 13')$$

$$(\alpha, \delta)_{\text{J2000.0}} = (11^{\text{h}} 12^{\text{m}} 2 \pm 0^{\text{m}} 8, -7^\circ 06' \pm 0' 16')$$

in constellation Crater.

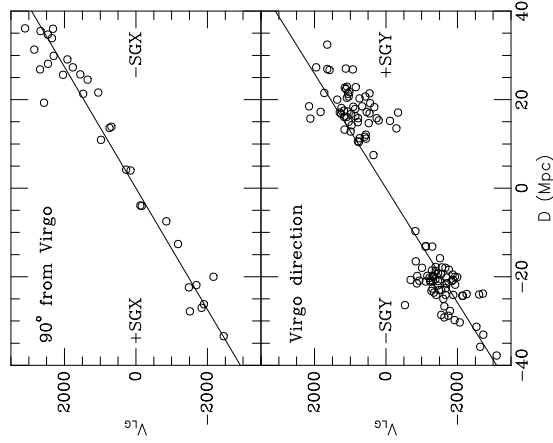


The constellation Crater ("Becher") in Johan Elert Bode's Sternatlas (after Slawik/Reichert, Atlas der Sternbilder, Spektrum, 2004)



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Velocity Field, IV



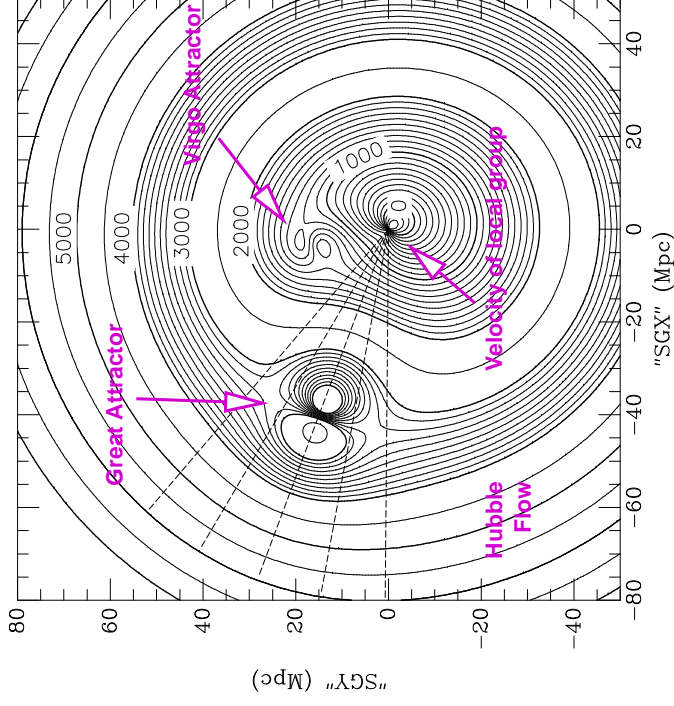
To get feeling for v_G out to Virgo, need to study local velocity field surrounding local group and beyond.

Two major velocity components:

1. Virgocentric infall (known since mid-1970s)
2. Motion towards great attractor ("Seven Samurai", 1980)

plus virialized galaxy motions within clusters. General analysis: build maximum likelihood model of velocity field including above components *plus* Hubble flow. See Tonry et al. (2000) for details.

Galaxy moves within local group with $v \sim 630 \text{ km s}^{-1}$



Decomposition of velocity field: (Mould et al., 2000, Tab. A1, note that Tonry et al. 2000 find slightly different values):

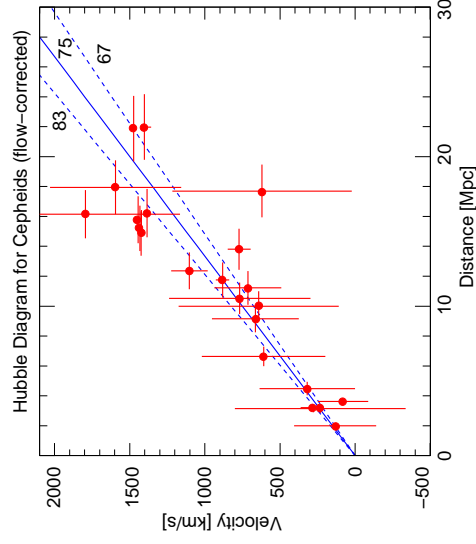
- | | | |
|---------|--|-------------------|
| | $\alpha_{1950.0}$ | $\delta_{1950.0}$ |
| Virgo | $12^{\text{h}}28^{\text{m}} + 12^{\circ}40'$ | |
| GA | $13^{\text{h}}20^{\text{m}} + 44^{\circ}00'$ | |
| Shapley | $13^{\text{h}}30^{\text{m}} + 31^{\circ}00'$ | |
- (v wrt. center of local group; not taking Hubble flow into account!).

(Tonry et al., 2000, Fig. 20)



9-80

H from HST



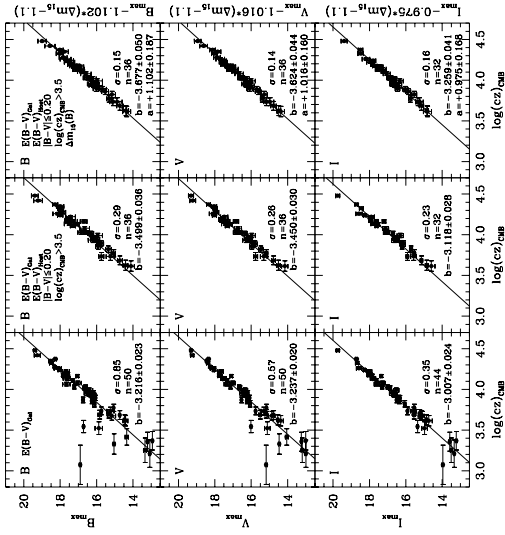
To obtain H_0 :

1. Determine d with Cepheids and HST
 2. Determine " v ", corrected for local velocity field
 3. Draw Hubble-diagram
 4. Regression Analysis $\Rightarrow H_0$
- Value from HST Key Project:

$$H_0 = 75 \pm 10 \text{ km s}^{-1} \text{ Mpc}^{-1} \quad (9.41)$$

Freedman et al. (2001, Fig. 1)

H from HST

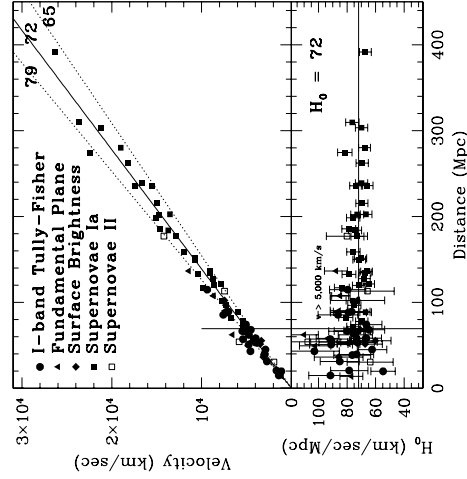


Cepheids alone: **nearby**
 ⇒ systematic uncertainties due to local flow correction and small overall v
 ⇒ use secondary candles to get to larger distances.
 Example: magnitude-redshift diagram, analogous to Hubble diagram ($m \propto -5 \log I$, and $I \propto 1/r^2 \propto 1/z^2$ because of Hubble $\Rightarrow m \propto \log cz$).
 (SN Ia Hubble relations; left: full sample, middle: excluding strongly reddened SN Ia, right: same as middle, correcting for light-curve shape Freedman et al., 2001, Fig. 2)

Hubble Constant

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H from HST



Combining all secondary methods, best value found:

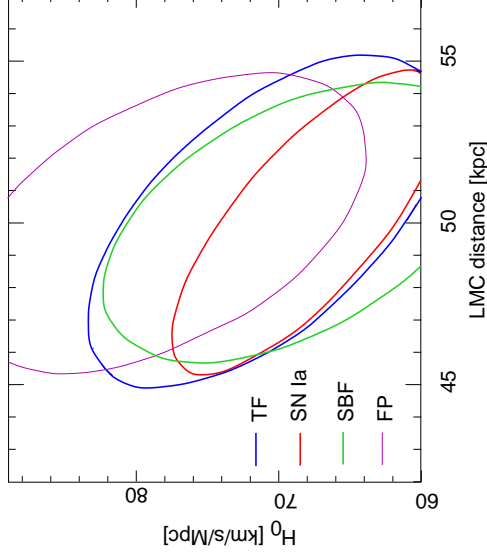
$H_0 = 72 \pm 8 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (9.42)

Freedman et al. (2001, Fig. 4)

Hubble Constant

9

H from HST



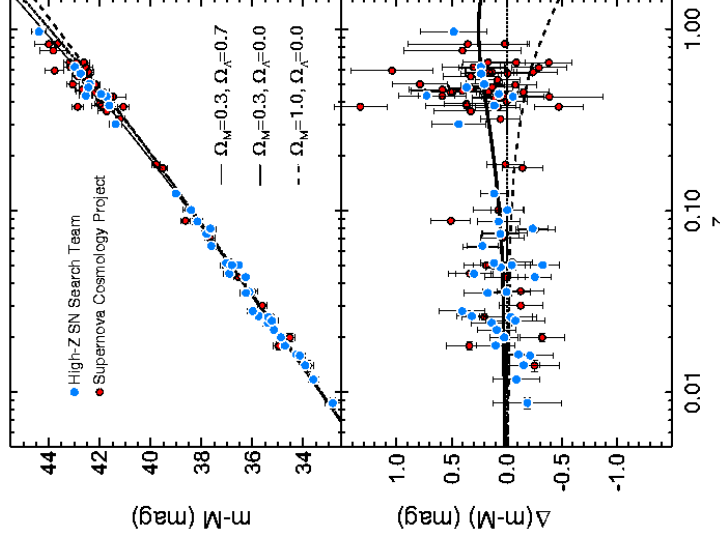
Major systematic uncertainty in current H_0 value: zero-point of Cepheid scale, i.e., distance to Large Magellanic Cloud.
 Despite these problems:
 ⇒ All current values approach $\sim 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, with uncertainty $\sim 10\%$

H_0 controversy is over

(after Mould et al., 2000, Fig. 5)

Hubble Constant

10



For larger distances: There are deviations from Hubble-Relation! Before we understand why: Need to understand the Big-Bang itself!

Hubble Constant

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