

Galaxies and Cosmology

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ERLANGEN CENTRE
FOR ASTROPARTICLE
PHYSICS

Friedrich-Alexander-Universität
Erlangen-Nürnberg



1-2

Contents: Galaxies

Introduction

- 18 Oct Organization; Stars and Galaxy
- 24 Oct Galaxies, Evolution of the Universe

Local Group

- 25 Oct Members, Motions, ISM
- 07 Nov ISM, Chemical Evolution

Spiral Galaxies

- 08 Nov Global Properties, Distribution of Gas
- 15 Nov Density Wave Theory
- 21 Nov Density Wave Theory, Bulges and Centers

Elliptical Galaxies

- 22 Nov Global Properties, Distribution of Matter

Active Galactic Nuclei

- 29 Nov Seyfert Galaxies, Black Hole Paradigm - AM
- 06 Dec Radio Loud AGN

Galaxy Clusters

- 12 Dec Galaxy Statistics, Interactions, Starbursts - UH

Contents

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Contents: Cosmology

Classical Cosmology

- 19 Dec Introduction, FRW
- 20 Dec Distance Scale, H_0
- 16 Jan Distance Scale, H_0

The Early Universe

- 17 Jan Hot Big Bang, Nucleosynthesis
- 24 Jan Inflation

Properties of the Universe

- 30 Jan Measurement of Ω and Λ
- 31 Jan **EXAM**

Structure Formation

- 06 Feb Measurement of Structure
- 07 Feb Structure Formation & CMB

Contents

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1-1

Introduction



1-4

Textbooks

SPARKE & GALLAGHER, 2007, *Galaxies in the Universe – an Introduction*, Cambridge: CUP, 40.99 € (softcover)

Textbook for the 1st half of the class, somewhat lower level than what we will be teaching, but a very good overview nevertheless.

BINNEY & MERRIFIELD, 1998, *Galactic Astronomy*, Princeton: Princeton University Press, 55 €, 791 pp.

Advanced level book on Galactic astronomy, the standard for graduate level courses, so higher than what we will be doing, but a very good book if you want to continue to do astronomy. Recommended.

SCHNEIDER, P., 2005, *Einführung in die Extragalaktische Astronomie und Kosmologie*, Heidelberg: Springer, 59.95 € (available as an e-book)

Well written introduction to cosmology, approximately at the level of this lecture. Recommended.

Literature

1



1-5

Textbooks

PEACOCK, J.A., 1999, *Cosmological Physics*, Cambridge: Cambridge Univ. Press, 49.50 €

Very exhaustive, but difficult to read since the entropy per page is very high... still: a "must buy".

LONGAIR, M.S., 1998, *Galaxy Formation*, Berlin: Springer, 53.45 €

Clear and pedagogical treatment of structure formation.

CARROLL & OSTLIE, 2007, *Modern Astrophysics*, Reading: Addison-Wesley, 80 € (softcover), 1400 pp.

Advanced level, expects good physics background, generally I like their stellar astrophysics part better than their extragalactic one.

Literature

2



1-6

Exercises and Exam

We will have 2 h long exercise sessions led by Tobias Beuchert and Felicia Krauss approximately every 2 weeks at the following dates:

31 Oct	Milky Way
14 Nov	Spiral Galaxies
28 Nov	ADS, NED, Simbad, Proposals
05 Dec	AGN
13 Dec	1st Iteration Proposals
23 Dec	Proposal Email Submission Deadline
09 Jan	Observing Panel
10 Jan	World Models, Cosmology
23 Jan	Test Exam

Note that your presence at the exercise sessions is mandatory (unless you have a lab experiment)

In general, exercises are "in class" (i.e., no homeworks). We will also give out reading assignments and other exercises to help you with the course.

Exercises and Exam

1



1-7

Exercises and Exam

In addition to standard exercises, we will go through an "observing proposal" exercise, where you will

- ... write (alone!) a 1-2 page scientific justification for an astronomical observation
- ... discuss a preliminary draft with one of us
- ... read ~5 proposals written by your colleagues, present and discuss them in an "observing panel"
- ... rank proposals by scientific importance.

- 50% of final grade: Your Proposal and panel participation (grade set by us, not the panel!)

- 50% of final grade: Exam (31 January 2011).

Exercises and Exam

2



2-1

Overview

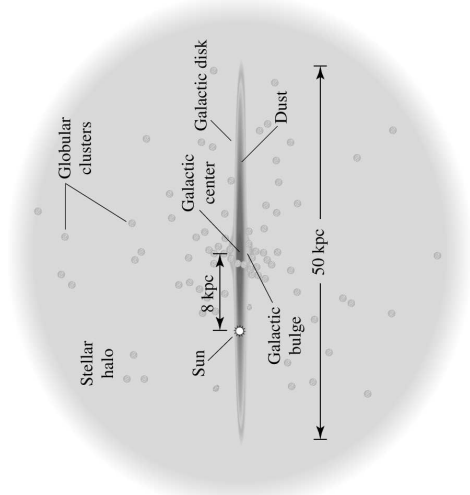


2-3

Structure of the Galaxy

components of the Milky Way:

- Galactic disk:
 - rotating
 - young & old stars, open star clusters
 - gas & dust
- Galactic halo:
 - non-rotating,
 - old stars only, globular clusters
 - no gas, no dust
- Galactic bulge: rigid rotation



Galaxies

1



2-2

Introduction

Galaxies and the universe consist of stars, and basic knowledge on the properties of stars and of Galaxies is required.

Before starting with this course, we will therefore briefly review the most important properties of the Milky Way, Galaxies and the Universe, to bring everybody up to speed.

For details please consult the lecture notes for "Introduction to Astronomy" at <http://pulsar.sternwarte.uni-erlangen.de/wilms/teach/intro>

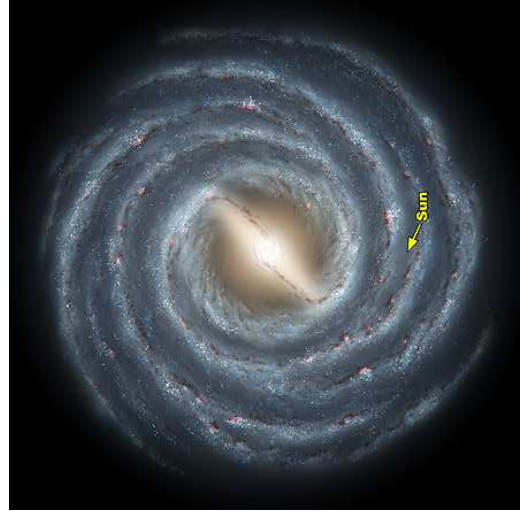
Introduction

1



2-4

Structure of the Galaxy



Milkyway is a barred spiral galaxy
 Luminosity: $\sim 2 \times 10^{10} L_{\odot}$
 Mass: $\sim 10^{11} M_{\odot}$ (radiating)
 $\sim 10^{12} M_{\odot}$ (total)
 Stellar density: $\sim 0.3 M_{\odot} \text{pc}^{-3}$

$$1 M_{\odot} = 2 \times 10^{33} \text{ g} = 2 \times 10^{30} \text{ kg,}$$

$$1 L_{\odot} = 4 \times 10^{33} \text{ erg s}^{-1} = 4 \times 10^{26} \text{ W}$$

Galaxies

2



Evidence for Spiral Arms

- Spins of electron and proton may be parallel ($F = 1$) or antiparallel ($F = 0$) ("hyperfine levels"); energy difference of $\Delta E \sim 6 \times 10^{-6}$ eV, corresponding to $\lambda = 21$ cm or $\nu = 1.4$ GHz.
- $F = 1$ is metastable, i.e., long life time (10^7 years); transition to $F = 0$ dipole forbidden in quantum mechanics, transition rate 10^{-6} smaller than for permitted transitions.
- Laboratory: $F = 1$ state is depopulated by collisions; no line is seen.
- ISM: low densities, i.e., no collisions; radiative transitions possible.

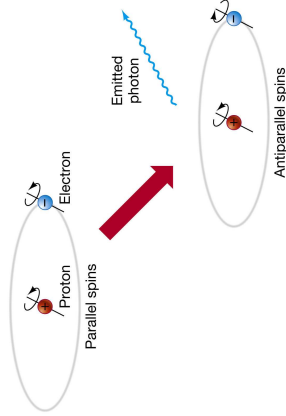


Image: 2005, Pearson Prentice Hall, Inc.

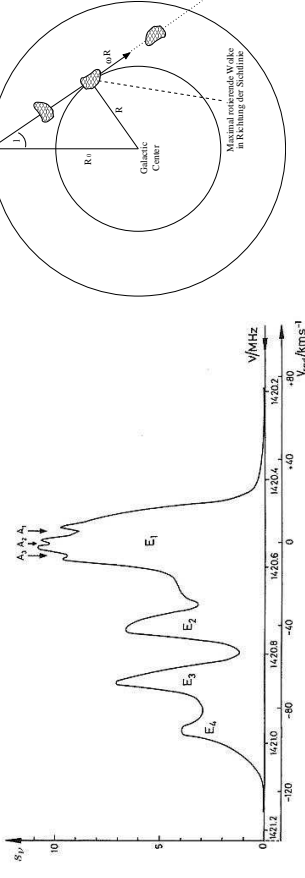
Because of the ubiquity of hydrogen, 21 cm line traces gas extremely well. Self-absorption of the line is extremely unlikely \Rightarrow line visible from everywhere except for the most dense regions.

Galaxies

3



Evidence for Spiral Arms



Sketch of a typical HI emission line profile. Note: v_z -axis has wrong sign!

In general multiple hydrogen clouds along the line of sight. Differential rotation \Rightarrow Differential Doppler shift, allows to obtain $\Omega(R)$ (note: maximum v_t at $R = R_0 \sin \ell$).

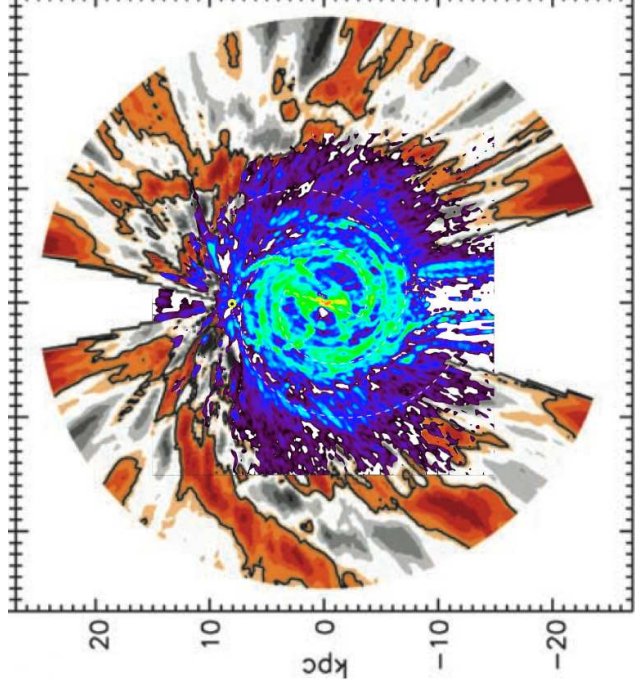
Overall: Probe of ISM structure and dynamics!

Integration over the full profile gives the column density of neutral hydrogen in this direction. Typical values: 10^{18} cm $^{-2}$ (at large gal. latitudes) to 10^{22} cm $^{-2}$ (in the gal. plane).

State of the art is the Leiden-Argentine-Bonn Survey (Kalberla et al., 2005).

Galaxies

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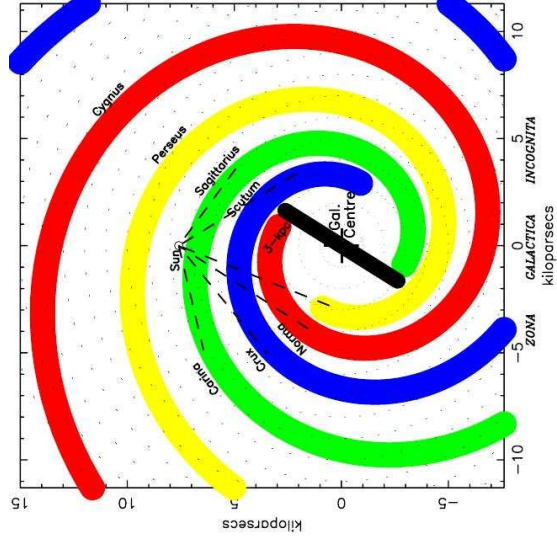


from Englmaier, Pohl, Bissantz (2008, Fig. 2; Sun is yellow dot)

Distribution of CO and H gas shows clearly the spiral structure.



Evidence for Spiral Arms



The spiral arm structure of Galaxy is now rather well understood

Vallee (2008)

Galaxies

6



Classification

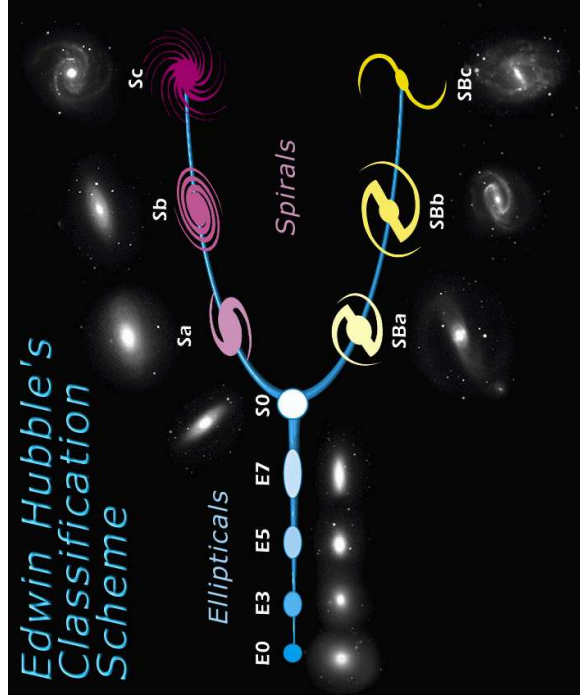
2-9

1920s: Hubble and others: classification of galaxies

- **Morphology:** Appearance on photographs, photographic emulsion is blue sensitive
- **Warning:** scheme is in parts not so well defined, incomplete, and not unique
- **Note:** photometric (colors) and spectroscopic information are not part of the Hubble scheme.

Galaxies

1



SDSS

Galaxy classification via the Hubble "tuning fork diagram": "early types": elliptical galaxies; "late types": spiral galaxies, Not an evolutionary sequence!



Elliptical galaxies: Classification as E: x where $x = 10(a - b)/a$ (integer part; between 0 and 7)

Ellipticals are low on dust and gas, reddish color (=old stars!), typically low luminosity and low mass ($10^6 M_{\odot}$)

Monsters: Also elliptical, from mergers in galaxy clusters (e.g., M87 in Virgo), M up to $10^{12} M_{\odot}$, designated cD.



M60 (NGC 4649), E1, U. of Alabama

Classification

2-11

Galaxies

3

Spiral Galaxies

2-12

Spiral Galaxies: Elliptical nucleus ("bulge") plus disk with spiral arms, designated Sa, Sb, Sc depending on opening angle of spiral (Sa: $\sim 10^{\circ}$, Sc: $\sim 20^{\circ}$) and dominance of nucleus.

Bluer than ellipticals.

Mass content $\sim 3 \times 10^{11} M_{\odot}$, with $M/L \sim 20$,

Gas content increases from Sa to Sc from 1% to 8%.

Spiral arms probably due to density wave.



M51 (NGC 5194 and 5195), Sc and Irr, Kitt Peak 0.9 m

Galaxies

4



Barred Spirals



M95 (NGC 3351), SBb, INT

Barred Galaxies: Classification as SBa, SBb, SBc similar to Sx galaxies, but additional presence of a bar (cause of bar production and stability are still debated).

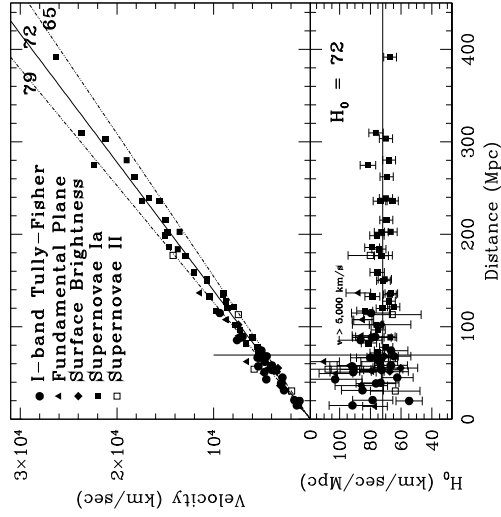
Similar masses and gas content as in normal spirals.

Milky Way is a barred spiral.

Galaxies



Expansion of the Universe



(Freedman, 2001, Fig.4)

Hubble relation (1929):

The redshift of a galaxy is proportional to its distance:
 $v = cz = H_0 d$

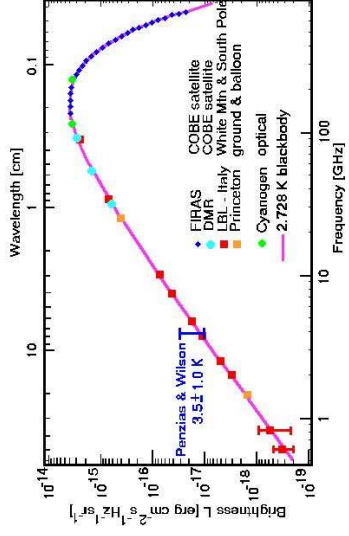
where H_0 : "Hubble constant".

Measurement: determine v from redshift (easy), d with standard candles (difficult)
 $\Rightarrow H_0$ from linear regression.
 Hubble Space Telescope finds

$$H_0 = 72 \pm 8 \text{ km s}^{-1} \text{ Mpc}^{-1}$$



CMB



There is a cosmic microwave background (CMB), which is a perfect black body with $T = 2.725 \pm 0.002 \text{ K}$

\Rightarrow Universe started hot, then temperature decreased as universe expanded,

$$T(z) = T_0(1+z) \quad (2.1)$$

Cosmology



CMB

$a(t)$	t since BB	T [K]	ρ_{matter} [g cm^{-3}]	Major Events
10^{-13}	10^{-42}	10^{30}		Planck era, "begin of physics"
	$10^{-40} \dots 10^{-30}$	10^{25}		Inflation?
	$\sim 10^{-5} \text{ s}$	$\sim 10^{13}$	$\sim 10^9$	generation of p-p $^+$, and baryon anti-baryon pairs from radiation background
3×10^{-9}	1 min	10^{10}	0.03	generation of e $^+$ -e $^-$ pairs out of radiation background
10^{-9}	10 min	3×10^9	10^{-3}	nucleosynthesis
$10^{-4} \dots 10^{-3}$	$10^{6.7} \text{ yr}$	$10^{3.4}$	$10^{-21} \dots 10^{-18}$	End of radiation dominated epoch
7×10^{-4}	10^7 yr	4000	10^{-20}	Hydrogen recombines, decoupling of matter and radiation
1	$15 \times 10^9 \text{ yr}$	3	10^{-30}	Formation of structures
	now			now

General structure formation

General idea of all theories of structure formation:

1. Big Bang generates initial density perturbations (=potential wells)
density perturbations caused by Poisson statistics in the early universe, e.g., decay of inflaton or similar
2. Those density fluctuations that can grow, grow.
3. Those density fluctuations that cannot grow get smoothed out by expansion and disappear.

How fluctuations grow depends on properties of material forming structures:

Early theory (Zeldovich, 1960s): structures=baryons; large structures must form first \implies this is not what is observed.

New theory: dark matter is important:

1. DM forms initial potential wells
2. Wells develop as universe expands
3. Baryons fall into potential wells once radiation and matter decouple
4. galaxies formed first, clusters still forming

Cosmology

Dark Matter

Detailed theory of structure formation uses numerical simulations, using CMB boundary conditions and assumptions on dark matter:

Hot Dark Matter: relativistic particles (e.g., neutrinos): moving with $v \sim c$. Fast particles

\implies smears out small density perturbations

\implies "top down structure formation"

Not what is observed

(observed: galaxies were there first, clusters are still forming)

Cold Dark Matter: slow particles, condense first, forming potential wells while baryonic matter is still coupled to radiation.

Once radiation decouples from matter (when universe is cold enough), matter falls in gravity wells.

\implies "bottom up structure formation"

Closer to what is observed

Luminous baryonic mass traces Dark Matter

Cosmology

Dark Matter

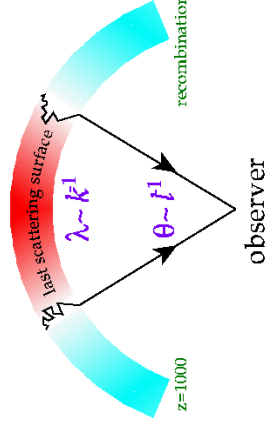
After BB: Universe is dense ("furry"), photons scatter efficiently off electrons \implies coupling of matter and radiation

Universe cools: recombination of protons and electrons to form hydrogen

\implies no free electrons

\implies no scattering

\implies photons stream freely

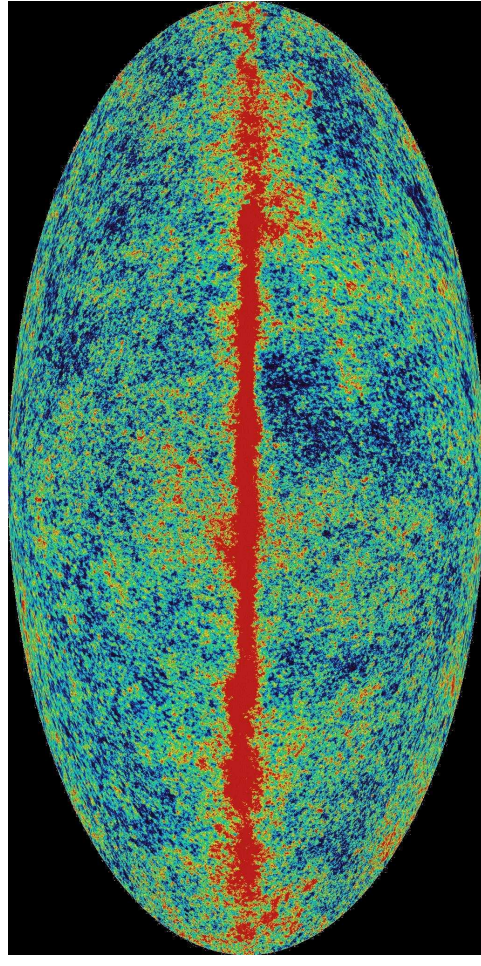


courtesy Wayne Hu

Photons leaving overdense regions lose energy (gravitational red shift) \implies visible as a temperature fluctuation (Sachs-Wolfe-Effect)

Leads to CMB fluctuations \sim gravitational potential at $z \sim 1100$ (380000 yr after big bang) \implies structure

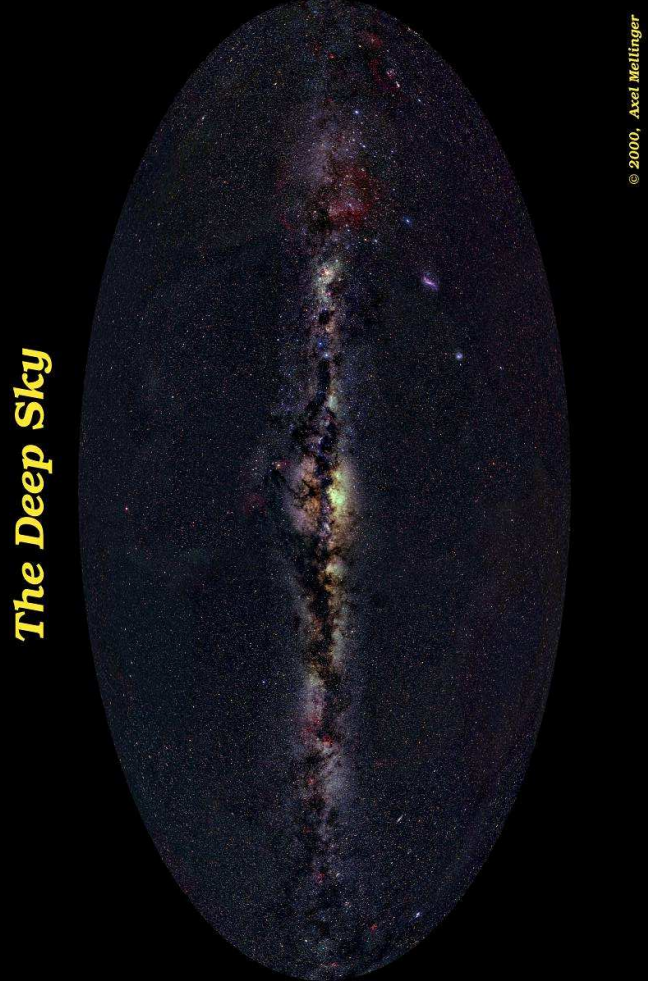
Cosmology



WMAP, W-Band, $\lambda = 3.2 \text{ mm}$, $\nu = 93.5 \text{ GHz}$, resolution 0.21°



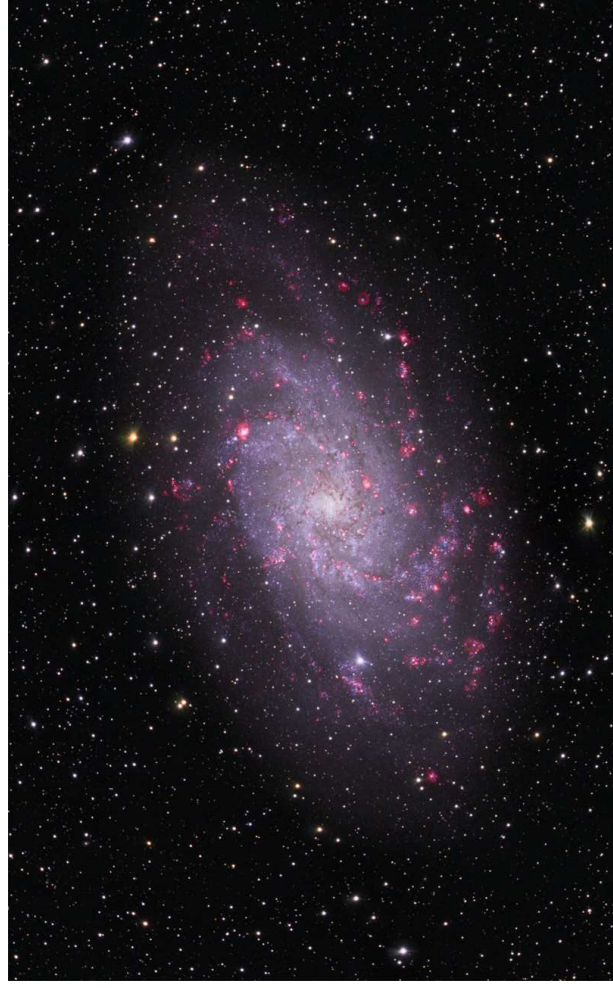
The Local Group



Milky Way



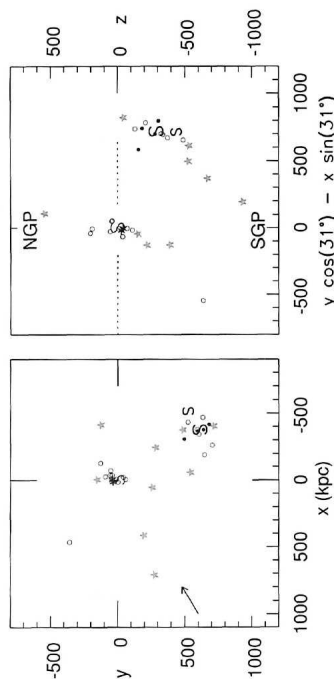
Andromeda galaxy (=M31; closest real neighbour galaxy, diam. 20kpc, distance: 675 kpc), NOAO/AURA/NSF



M 33 (= "Triangulum Galaxy"; $L \sim 0.2 L_{\text{Milky Way}}$)



Our Backyard: The Local Group



SG, Fig. 4.2; see also <http://www.astro.umass.edu/~fardal/local.vol/index.php>

Distribution of galaxies in local group is not random: hierarchy of galaxies:

- small galaxies surround massive ones
- Milky Way satellites lie in plane ⇒ joint formation?
- however, many small galaxies are *not* associated with large galaxies

Introduction



Our Backyard: The Local Group

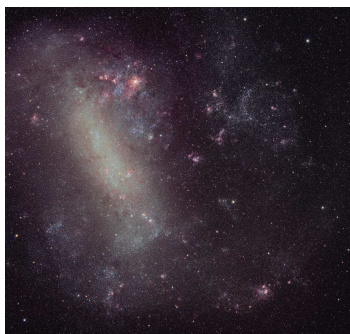
Types of Galaxies:

- two spirals, but only one large elliptical
 - rich in 'late type galaxies', i.e., spirals and irregulars
 - poor in 'early type' giant ellipticals and S0 galaxies
⇒ Typical for groups (not!) for galaxy clusters!
- Dynamics:
- Andromeda and Galaxy are approaching at $\sim 120 \text{ km s}^{-1}$
 - All other galaxies within of 60 km s^{-1} of Andromeda/Milky Way
⇒ Local Group is gravitationally bound

Half of all (known) galaxies are in groups or clusters, other half in loose associations.

Local group is hopefully a typical groups, so will study this here.
Big advantage: these are the last galaxies we can resolve into stars.

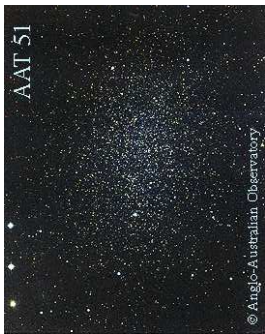
Introduction



LMC



Loke Kun Tan



Sag Dwarf

Leo Dwarf Galaxy

HST

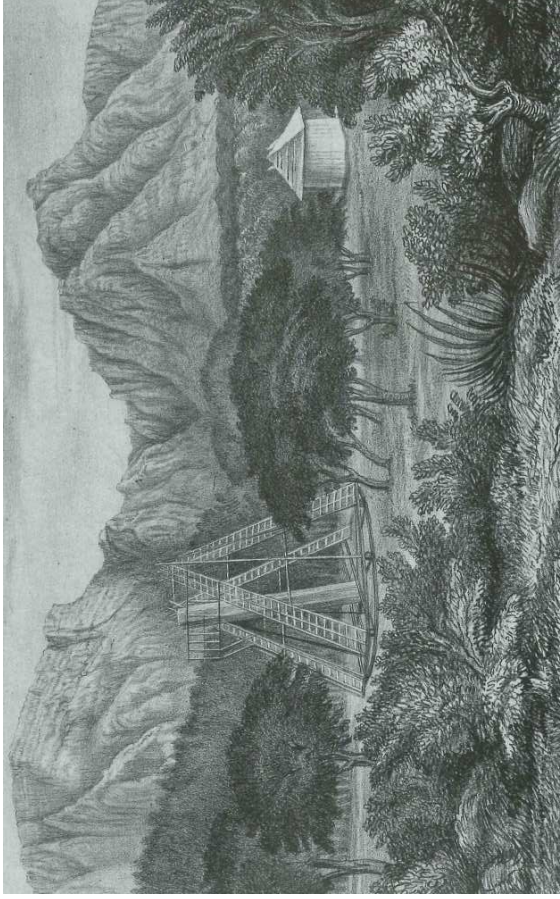
D. Malin (AAT)

Most other of the ~40 local group galaxies, however, are irregular galaxies, mainly bound to one of the three main members.

Table 1: Local Group Galaxies

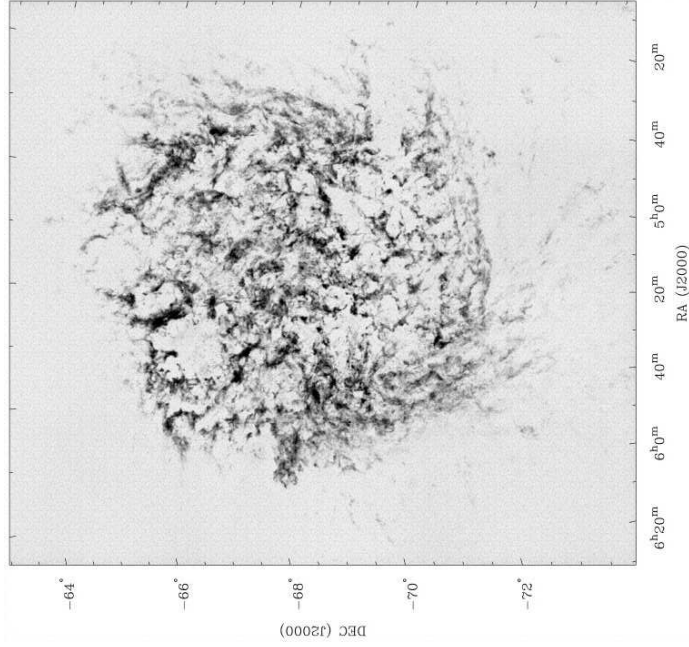
Galaxy (1)	Other Name (2)	RA (3)	Dec (4)	δ (5)	l (6)	b (7)	Type (8)	Shrump (9)	Notes (10)
WM1		00:15:48	-15:27:4	25.9	-73.6	163VV		1	
NGC 55	DDO 221	00:15:48	-30:13:2	282.7	-73.7	163VV	LGC	34,30	
IC 1613	DDO 192	00:15:48	-30:13:5	282.7	-73.7	163VV	LGC	33	
NGC 147	DDO 4	00:33:32	-45:32:5	19.9	-74.3	065	M31	7,51	
And III	UGCA 94	00:35:17	-48:30:15	19.3	-78.2	08h, 085	M31	8	
NGC 205	M10	00:40:22	-41:41:2	20.7	-73.1	09h, 085h, N	M31	7,51	
M32	NGC 221	00:42:42	-40:01:9	21.2	-72.0	E2	M31	9,10,41	
S10 ⁺	NGC 221	00:45:43	-45:00:4	21.7	-74.9	08h, 1	M31	6,10,61	
And I	NGC 292	00:52:44	-72:40:7	282.8	-44.3	163VV	MV	11,12,51	
S10 ⁻	NGC 292	00:52:44	-72:40:7	282.8	-44.3	163VV	MV	11,12,51	
IC 1613	DDO 8	01:04:54	-02:08:0	129.8	-60.6	163VV	M31/UGC	15,17	A
NGC 174	Phoxis	01:03:53	-21:53:1	28.6	-10.3	dir/08h	M31	14	
And II	NGC 598	01:33:51	-39:39:6	133.6	-71.3	Sd, rH, I	M31	17,18,51	
Phoxis	IC 1614	01:51:06	-44:26:7	272.2	-68.9	dir/08h	M31	19,20	
UGC 1027+45	EGS1027+45	04:32:01	+63:36:4	144.7	+10.5	dir	M31	23	
Leo A	DDO 69	05:23:24	-69:45:4	280.2	-32.9	163VV	MV	2,11,25,51	
Leo B	DDO 70	06:59:24	-39:44:7	386.9	+52.4	dir	MV	2,11,25,51	
And IV	NGC 206	10:02:00	-59:09:1	282.2	-33.3	163VV	M31	22,25,51	
And V	NGC 207	10:04:04	-57:19:8	281.1	-22.3	dir/08h	M31	23	
Sextans A	DDO 75	10:13:56	-41:42:5	286.4	-39.3	dir	M31	31	B
Sextans B	DDO 76	10:13:56	-41:42:5	286.4	-39.3	dir	M31	32	
Ursa Minor	DDO 155	15:09:11	+67:12:9	305.0	+44.8	08h, 1	G38	36,37,54	
And VI	NGC 2623	17:45:40	-29:03:5	0.1	-0.1	Sbc	MV	40	E
M36, M37	NGC 1057, 177	18:55:05	-30:28:7	5.6	-14.1	08h, N	MV	40	E
NGC 682	DDO 200	19:44:56	-14:48:1	25.3	-18.4	163VV	LGC	42,43,51	C
And VII	NGC 682	19:44:56	-14:48:1	25.3	-18.4	163VV	LGC	42,43,51	C
Triangulum	DDO 201	20:16:46	-11:51:0	30.0	-31.3	dir/08h	LGC	47,48	D
Triangulum	DDO 201	20:16:46	-11:51:0	30.0	-31.3	dir/08h	LGC	47,48	D
Tucana	UGCA 198	22:41:50	-41:25:2	282.8	-47.4	08h, 1	LGC	41	
IC 2573	UGCA 198	22:41:50	-41:25:2	282.8	-47.4	08h, 1	LGC	41	
Phoxis	DDO 210	22:26:27	-32:23:3	31.9	-32.0	dir/08h	LGC	2,10,41,51	

(Mataia, 1986, Tab. 1)



Block & Freedman, 2008, Fig. 40

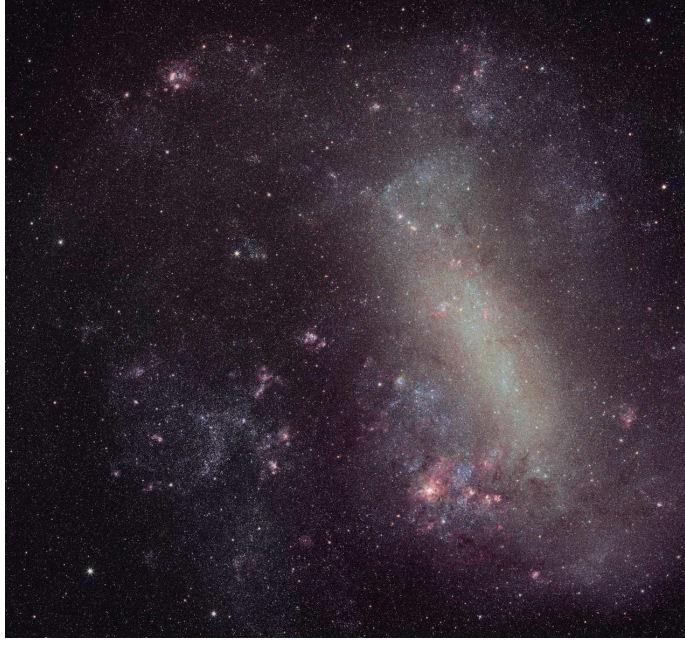
21 Foot telescope of John Herschel in Feldhausen (table mountain, close to cape town; 1825–1838)
 J. Herschel (1851): . . . there are *nebulae in abundance both regular and irregular, globular clusters in every state of condensation, and objects of a nebulous character quite peculiar, which have no analogue in any other region of the heavens. . .*



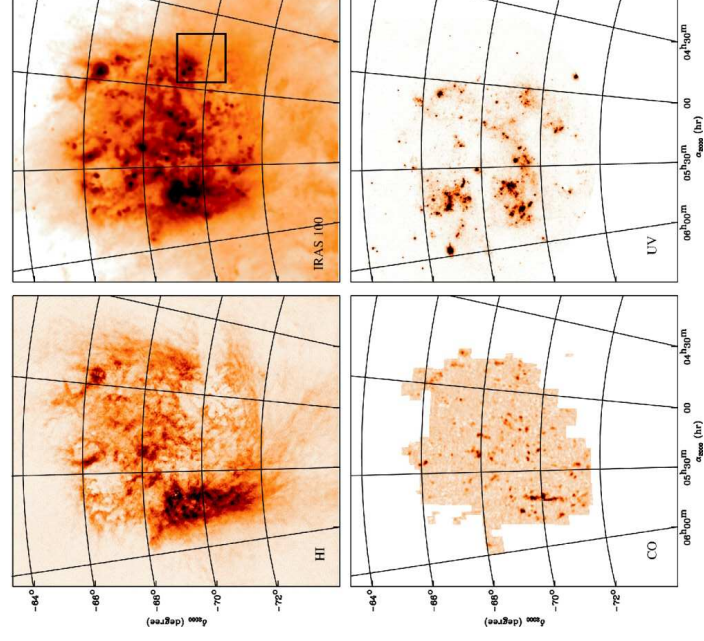
(Kim et al., 1998, Fig. 1)

Large Magellanic Cloud:

- distance: 49 kpc
- Size $15^\circ \times 13^\circ$ (~ 14 kpc)
- Prototype of Magellanic Spirals (Sm)
- Morphology: from 21 cm: flat disk, tilted by $\sim 45^\circ$ against plane of sky



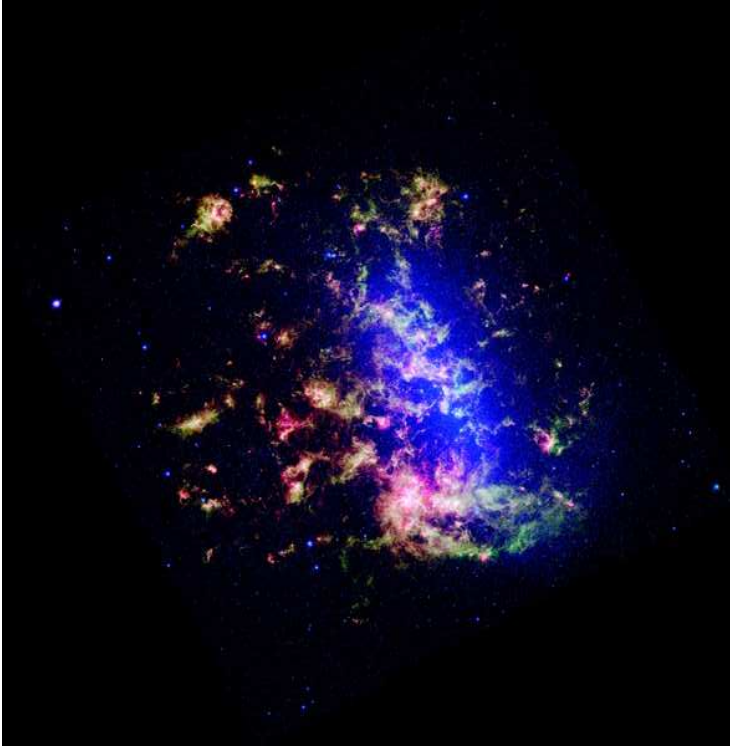
Optical: “cigar structure” of stars, many star formation regions visible through $H\alpha$ emission.



Distribution of emission in different bands:

- H I: cold gas
- IRAS: warm gas/dust
- CO: molecular clouds (star formation!)
- UV: hot stars (star formation!)

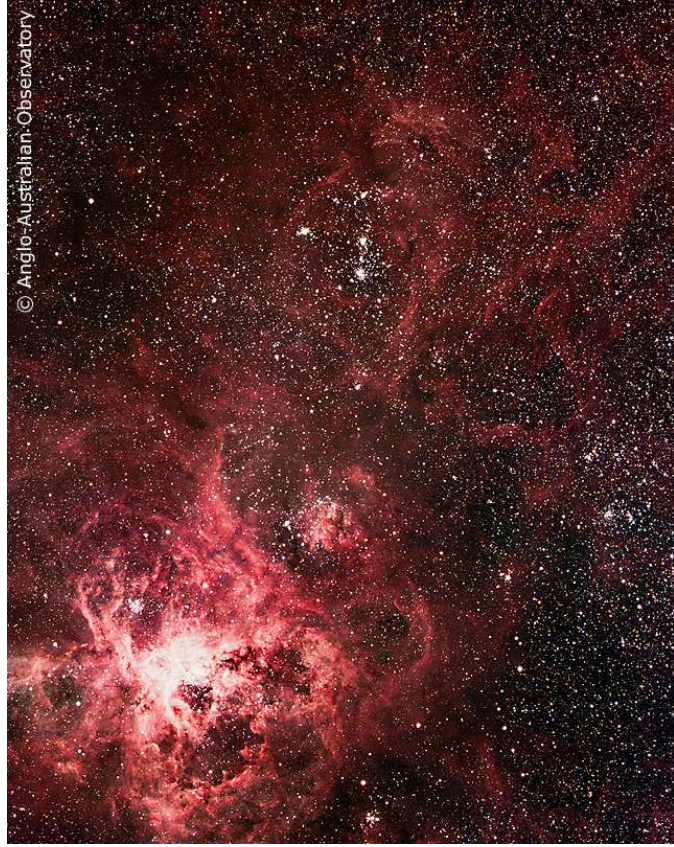
Note holes and loops: SNe and hot stars push colder ISM aside \implies hot bubbles
 Such structure is typical for irregular galaxies



SAGE (Meixner et al., 2006): Infrared mapping of the LMC with Spitzer: blue: IRAC-1 3.6 μm, green: IRAC-2 4.5 μm, red: IRAC-3 8.0 μm, purple: MIPS 16.0 μm



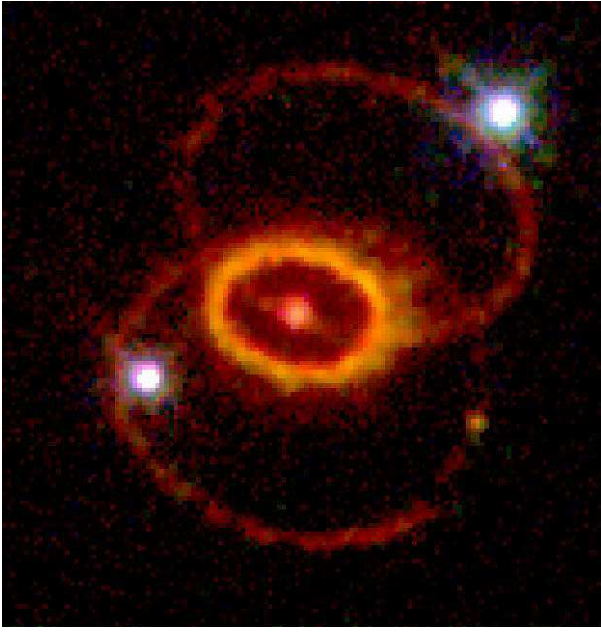
1987 February: Supernova in Large Magellanic Cloud.



© Anglo-Australian Observatory



HST/NASA/ESA/STScI



STScI PR94-22

87 d after explosion: Ring ($1.66'' \times 1.21''$) of ionized C and N around SN

⇒ Excitation of C, N in ring-like shell (ejecta from red giant phase of progenitor?); "light echo"



3-17

LMC: Distance

Light echo: direct geometrical determination of distance to LMC possible:

Time delay SN: close side of ring:

$$ct_1 = r(1 - \sin i) = 86 \pm 6 \text{ d} \tag{3.1}$$

Time delay SN: far side of ring:

$$ct_2 = r(1 + \sin i) = 413 \pm 24 \text{ d} \tag{3.2}$$

The ring radius is:

$$r = c \frac{t_1 + t_2}{2} = 250 \pm 12 \text{ lt d} \tag{3.3}$$

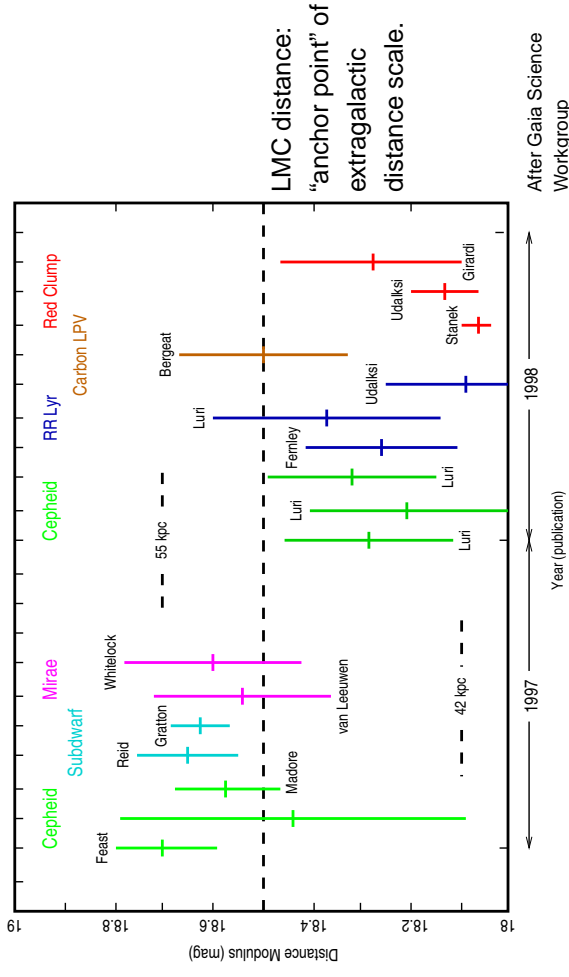
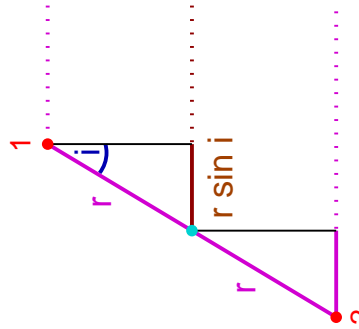
and the inclination is:

$$\sin i = \frac{t_2 - t_1}{t_1 + t_2} \implies i \sim 41^\circ \tag{3.4}$$

(From ring-geometry: $\cos i = 1''21 / 1''66 \implies i \sim 43^\circ$)

Thus from angular size of ring:

$$1''66 = \frac{r \cos i}{d} \implies d = 52 \pm 3 \text{ kpc} \tag{3.5}$$



LMC distance: "anchor point" of extragalactic distance scale.

After Gaia Science Workgroup

Strong dependence on Hipparcos calibration.

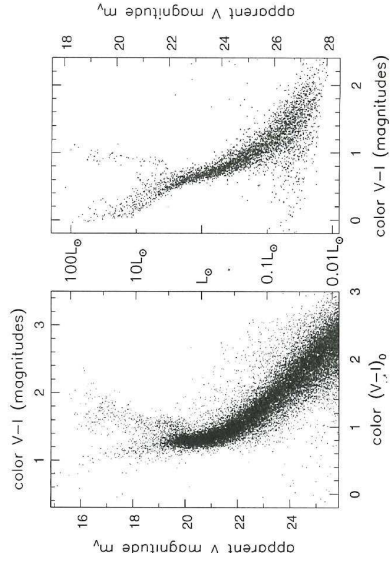
DM ranges between $18.7 \pm 0.1 \text{ mag}$ (Feast & Catchpole) and $18.57 \pm 0.11 \text{ mag}$ (Madore & Freedman)

Currently, the distance to the LMC is less well known than desirable.



3-19

LMC: Metallicity



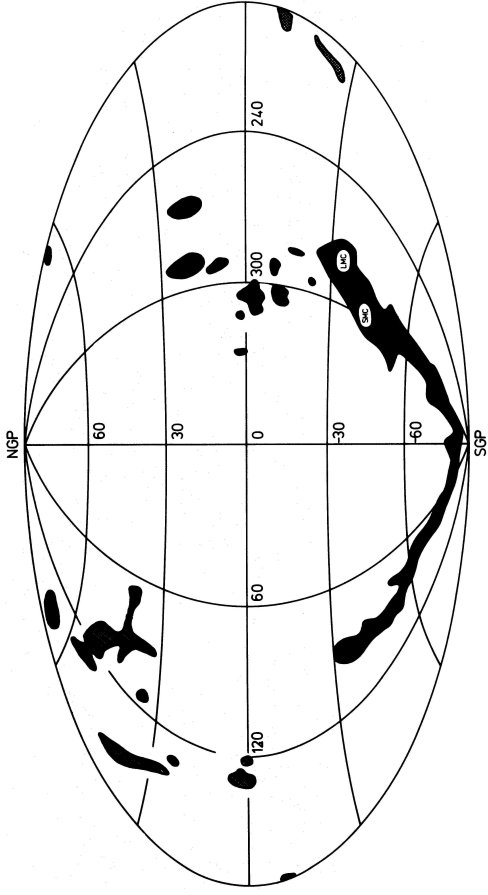
Sparke & Gallagher, Fig. 4.5

CMD of bulge stars in the MW

CMD of stars in LMC

Wide main sequence ⇒ dispersion in stellar ages

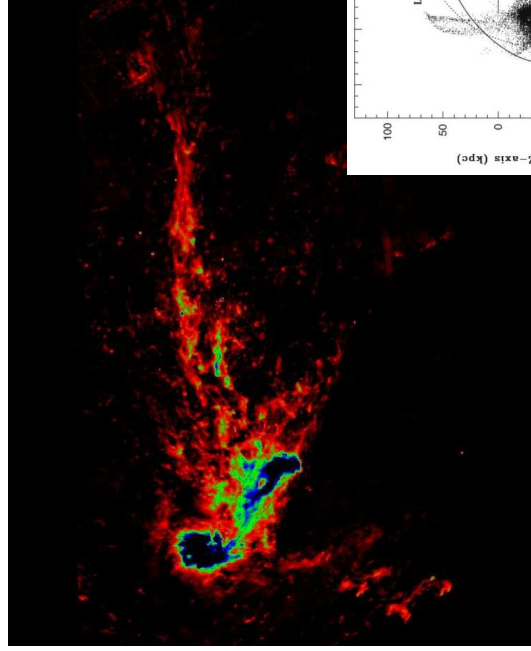
LMC: MS is bluer ⇒ LMC has lower metallicity



Mathewson et al. (1974, Fig. 1):

Magellanic Stream: number of high velocity clouds trailing Magellanic clouds

Total mass: $2 \times 10^8 M_{\odot}$.



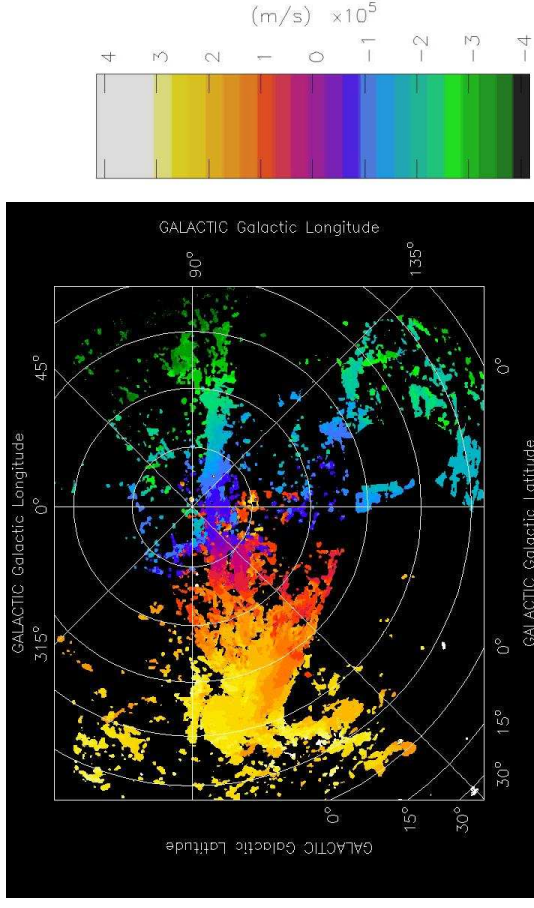
(Putman et al., 2003)

HIPASS-Survey (Putman et al., 2003): 21 cm survey spanning whole southern sky.

first real map of Magellanic Stream.

Head of stream: gas freshly removed from LMC and SMC,

tail: older material



(Putman et al., 2003)

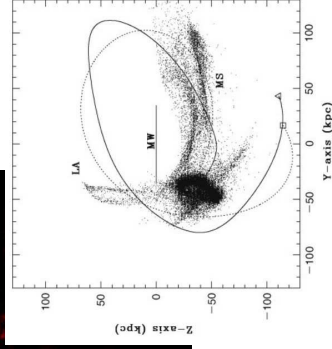
Velocity field from HIPASS-Survey

Stream has gradient of $\sim 700 \text{ km s}^{-1}$, $\sim 390 \text{ km s}^{-1}$ faster than galactic rotation

\Rightarrow noncircular orbit



R. Gendler



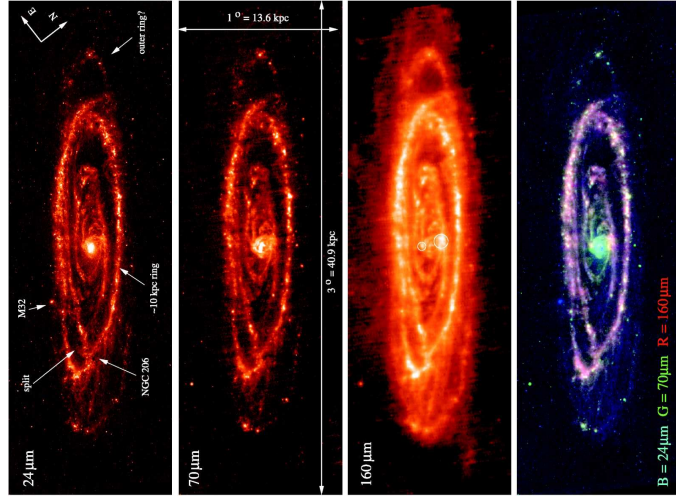
(Bekki & Chiba, 2009, Fig. 3)



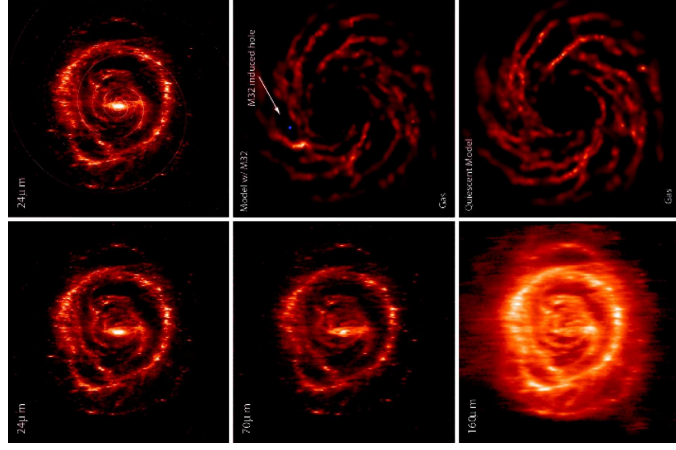
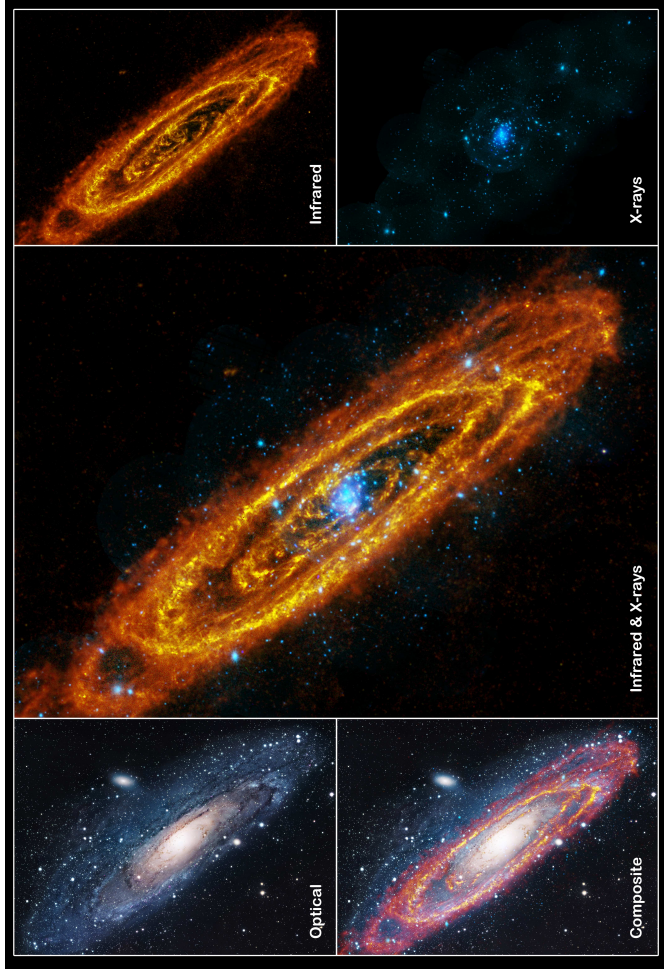
General Properties

- Andromeda galaxy:
- diameter 20 kpc, distance 675 kpc
 - ~50% more luminous than Galaxy
 - faster rotation speed (~260 km/s)
 - 300 globular clusters
 - many satellites:
 - one elliptical galaxy (M32)
 - three dwarf ellipticals
 - at least six dwarf spheroidals

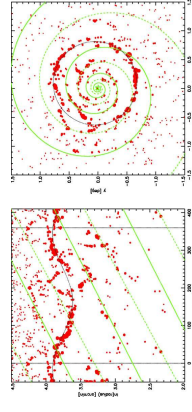
Andromeda



- Dust distribution in M31:**
- “ring of fire” at ~10 kpc
 - contains most young stars
 - also contains ionized H II regions (see last lecture)
- (Gordon et al., 2006, Fig. 1)



Deprojected images of Andromeda assuming inclination of 75°
 Note clear spiral structure, but disturbed by passage of M32 (first seen by ISO).
 Movie time: gordon_video1.mpg

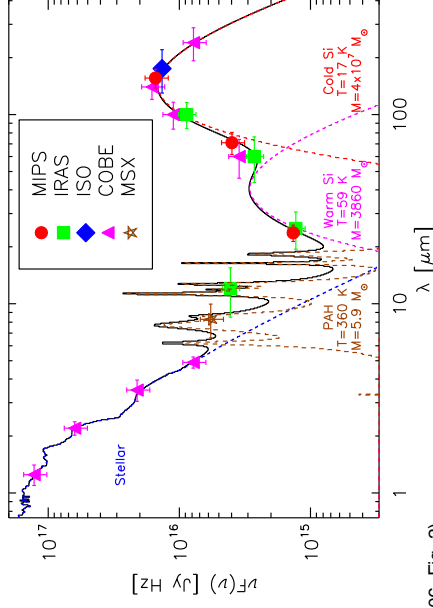


Ring is off-center, not associated directly with spiral arms (modeled by logarithmic spiral); origin not completely clear.



3-28

Dust



(Gordon et al., 2006, Fig. 2)

Total IR luminosity: $1.7 \times 10^{43} \text{ erg s}^{-1}$, corresponding to star formation rate of $0.75 M_{\odot} \text{ yr}^{-1}$.

Dust composition: silicates (warm from inner regions, cold from outer regions of Galaxy) and some polycyclic aromatic hydrocarbons (PAHs)

Andromeda

6



3-29

Milky Way and M31

M31 and Milky Way are gravitationally bound and approaching on a collision course, with collision happening in 2 billion years.

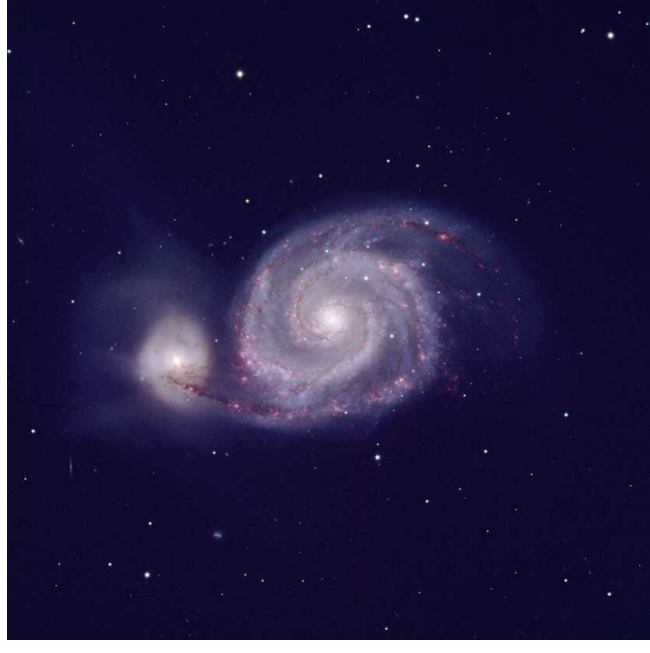
Possible scenario: formation of an elliptical galaxy over the course of about 1 billion years.

Collision studied with numerical simulations, movies show evolution calculations using 307.2 million particles (10 days on 512 processors):

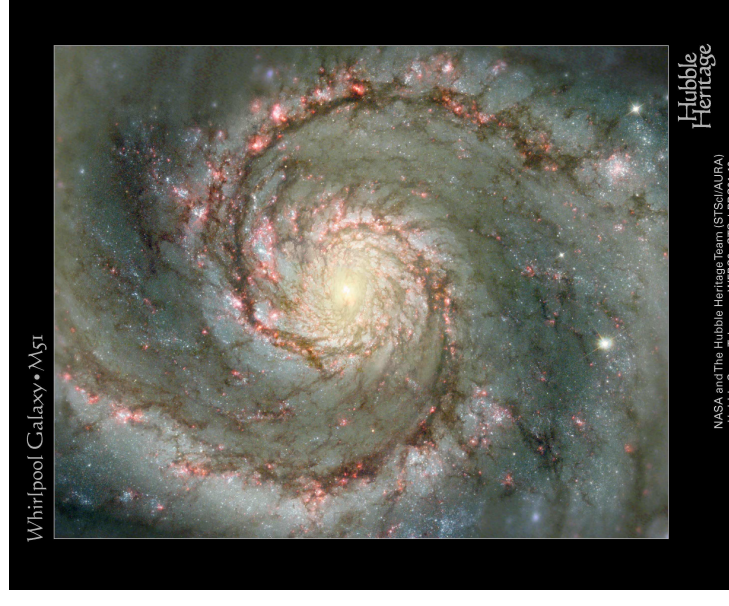
MOVIE Time: hdmwa.mov and 7_FutureSky.avi from <http://www.cita.utoronto.ca/~dubinski/nbody/>

Milky Way and M31

1



M51, NOAO, T. Rector



NASA and The Hubble Heritage Team (STScI/AURA)
Hubble Space Telescope WFC3 • STScI-PRC01-10

Hubble
Heritage



NGC 4565, McLaughlin

ESO PR Photo 02a/02 (25 January 2002)



© European Southern Observatory



The Horsehead Nebula
(VLT KUEYEN + FORS 2)

ESO PR Photo 21a/99 (20 April 1999)

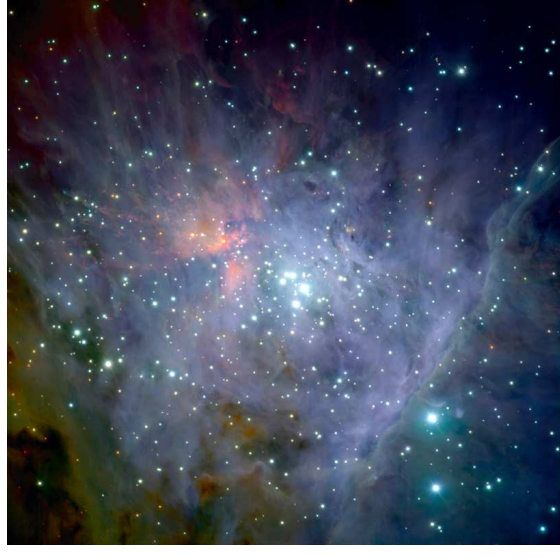


Star Forming Region RCW 108 in ARA
(MPG/ESO 2.2-m + WFI)

© European Southern Observatory

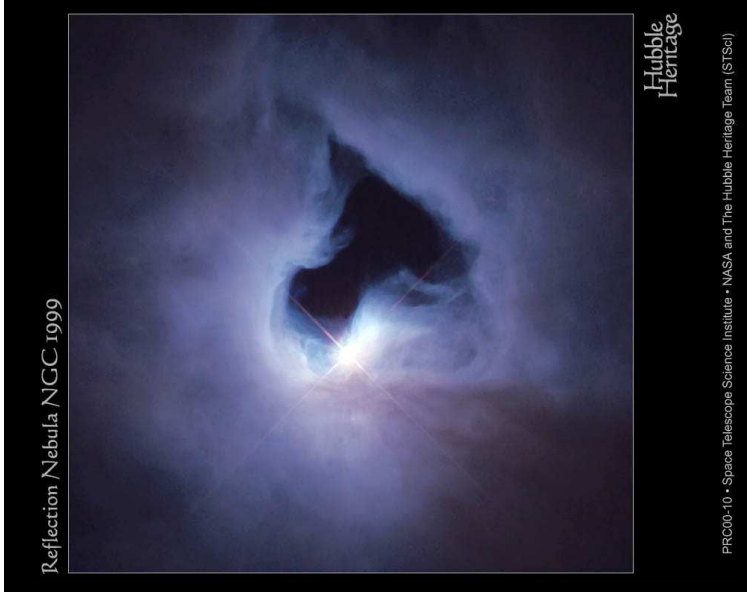


ESO PR Photo 08a/01 (15 January 2001)



The Orion Nebula and Trapezium Cluster
(VLT ANTU + ISAAC)

© European Southern Observatory



Molecules: History

- Secchi, 1878: First notice of molecular features in stellar spectra (class III and IV; no explanation)
Today known as TiO, C₂, and CN bands
- 1930s: Molecular lines in spectra of planetary atmospheres and comets as well as low temperature stars
- 1941: Interstellar absorption lines due to CN, CH, and CH⁺ in optical spectrum of ζ Oph
- Weinreb et al, 1963: Radio absorption lines at λ = 18 cm from OH towards SNR Cas A (not associated with Cas A, but with foreground clouds). masers (=non-LTE!)
- Cheung et al., 1968: First multi-atom molecules: NH₃ and H₂O (λ = 1.35 cm).
- Snyder et al., 1969: Formaldehyde (H₂CO).
- Today: more than 120 different molecules known

Molecules and Dust



Milky Way: ISM

The ISM of the Milky Way consists of the following phases

Name	Type	<i>n</i> cm ⁻³	T K	Filling Factor Vol-%	Mass % ISM	Comments
HIM	H II	10 ⁻² -10 ⁻⁴	10 ⁶ -10 ⁸	20-60	<1	SNR, wind, shocks
WIM	H II	10 ⁻¹ -10 ⁻⁴	10 ⁴	1-10	<1	photoionized by O/B-stars
WNM	H I	1-10	10 ⁴	20-30	20-50	21cm clouds, shells
CNM	H I	10-10 ²	100	10-20	20-50	HI envelopes, shells
MC	H I	10 ² -10 ⁴	10	1	40-50	IR, dust

HIM: Hot Ionized Medium, WIM: Warm Ionized Medium, WNM: Warm Neutral Medium, CNM: Cool Neutral Medium, MC: Molecular Clouds

courtesy J. Bally

Molecules and Dust



Molecular Hydrogen

Because of high abundances: most molecular gas is H₂.

For review of properties of H₂, see Shull & Beckwith, 1982, Ann. Rev. Astron. Astrophys. 20, 163

H₂ is homonuclear

⇒ no permanent dipole moment

⇒ no rotational dipole transitions.

Only transitions observable are vibrational or electronic.

Vibrational: λ ~ 6 μm, in the infrared.

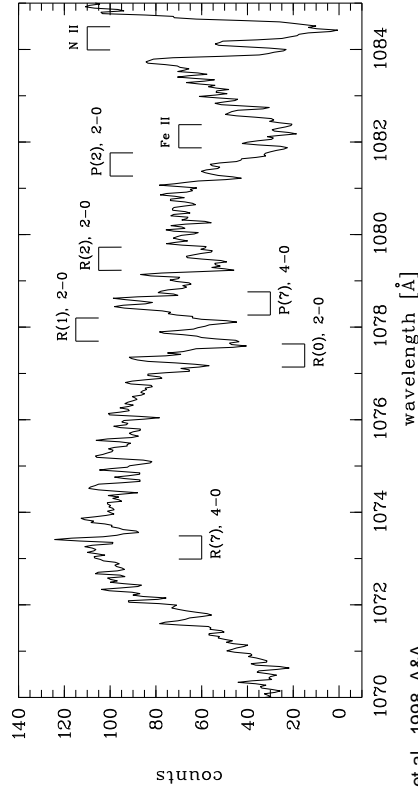
Problem: Dust extinction in IR severe

Once H is molecular, it is very difficult to see.

Alternative: Observation of electronic transitions of H₂ in absorption against hot UV-Stars ("Werner-bands").

Note that excitation of transitions requires lots of energy which cannot be produced otherwise.

Molecules and Dust

**Molecular Hydrogen**

Richter et al., 1998, A&A

ORFEUS: Discovery of H₂ bands in absorption in direction towards SMC

⇒ H₂ also present in diffuse ISM, not only in clouds
(agrees with Copernicus measurements in milky way; Spitzer, 1974)

Molecules and Dust

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**Molecular Hydrogen**

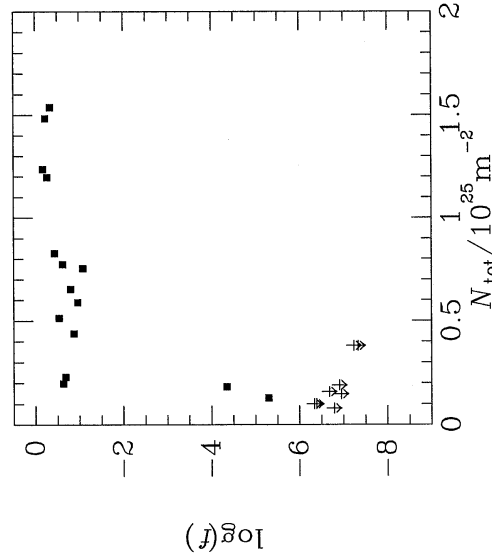
Calculate total Hydrogen-density obtained from

$$N(\text{H}_{\text{tot}}) = N(\text{HI}) + 2N(\text{H}_2) \quad (3.6)$$

and molecular fraction

$$f_{\text{H}_2} = \frac{2N(\text{H}_2)}{N(\text{H}_{\text{tot}})} \quad (3.7)$$

For $N(\text{H}_{\text{tot}}) < 2 \times 10^{18} \text{ cm}^{-2}$, i.e., low columns, H is atomic, above that molecular ⇒ More molecules in denser parts of ISM.



Binney&Merrifield, Fig. 8.5

Molecules and Dust

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**Carbon Monoxide**

Better than observing H₂ directly is to deduce its presence *indirectly* using other molecules with rotational positions ⇒ use heteronuclear molecules, e.g., CO, CS, HCN.

Candidate Number 1: CO, rotational transitions at 1.3 mm ($J = 2 \rightarrow J = 1$) and 2.6 mm ($J = 1 \rightarrow J = 0$).

Notation: CO(2-1) and CO(1-0)

CO is less abundant than H₂ (see later), but Einstein A-coefficients of lines very large; $\tau = 1$ reached at CO-column $\sim 6 \times 10^{15} \text{ cm}^{-2}$, corresponding to $N_{\text{H}} \sim 8 \times 10^{19} \text{ cm}^{-2}$

⇒ Cannot use “standard” CO to look into thick clouds.

⇒ Use some tricks: Isotope effects!

Molecules and Dust

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**CO: Isotope Effects**

CO occurs in several forms:

- $^{12}\text{C}^{16}\text{O}$ (= ^{12}CO)
- $^{13}\text{C}^{16}\text{O}$ (= ^{13}CO)
- $^{12}\text{C}^{18}\text{O}$ (= C^{18}O)

because of slightly different reduced masses, wavelength of transitions slightly different ⇒ can separate emission lines from these species.

Relative abundances:

$^{12}\text{CO} : ^{13}\text{CO} : \text{C}^{18}\text{O} = 500 : 65 : 1$

By using ^{13}CO or C^{18}O , can look deeper in molecular cloud.

Molecules and Dust

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Column from Lines

To measure mass from emission line, determine number of emitting atoms, N .
 Observed intensity not trivially $\propto N$ because of self-absorption.

Excess in line:

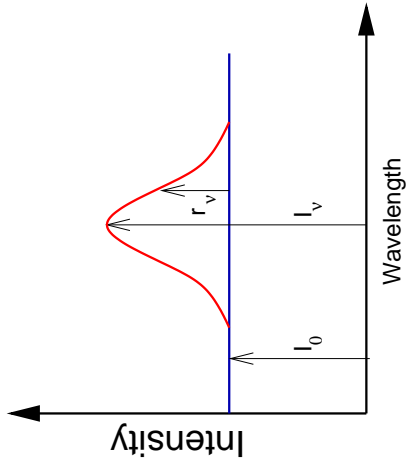
$$r_\nu = \frac{I_\nu - I_0}{I_0} = \frac{S_\nu - I_0}{S_\nu} \left(1 - \exp\left(-\frac{\tau_\nu}{\mu}\right) \right) \quad (3.8)$$

where τ : optical depth, I_0 : background intensity, $\mu = \cos\theta$

Inserting τ in terms of transition probability f_{nm} and expanding the exponential gives for the equivalent width

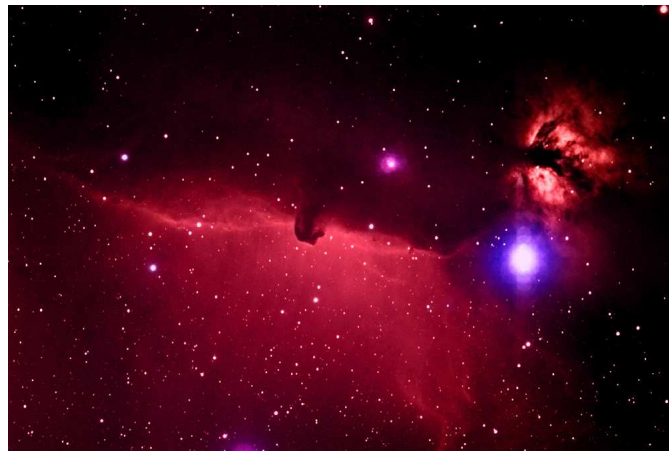
$$W_\nu = \int r_\nu d\nu \sim \frac{\pi e^2}{3mc} r_0 f_{nm} \frac{N_n}{\mu} \quad (3.9)$$

where $r_0 = (S_\nu - I_0)/S_\nu$.

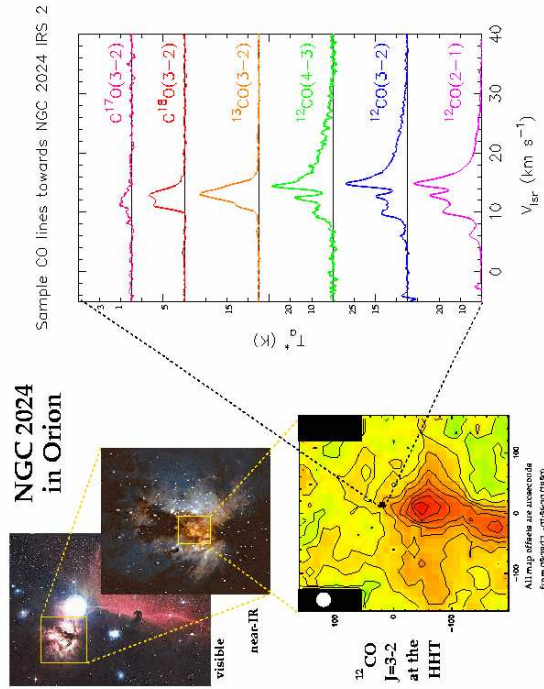


after Cowley, Fig. 14.5

Molecules and Dust



courtesy Matthew T. Russell

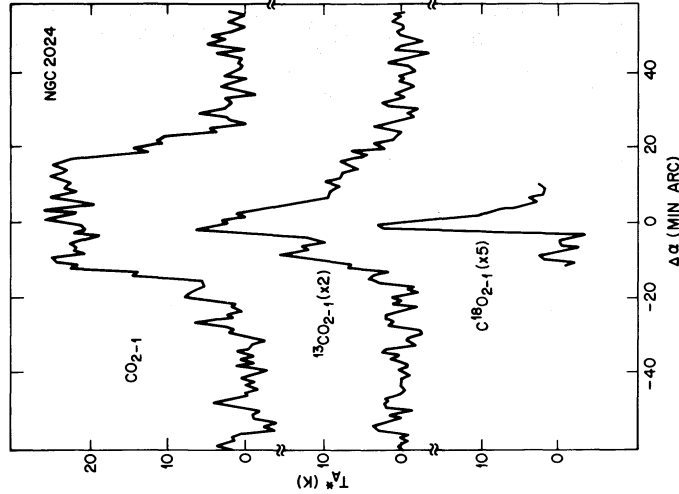


Sample CO lines towards NGC 2024 IRS 2

NGC 2024 in Orion

(courtesy Craig Kulesa)

As a case study: use NGC 2024 (flame nebula, bright star is Alnitak [ζ Ori]).



Right-ascension strip maps over NGC 2024: peak intensities ^{12}CO , ^{13}CO , and C^{18}O scale as 5:2:1
 \Rightarrow cloud is optically thick (lines should scale as the abundances, and they don't).
 Last step to obtain N_{CO} : use Boltzmann if (and only if) LTE is appropriate...

(Phillips et al., 1979, Fig. 3b). Intensity given as antenna temperature, $I = 2kT_{\text{A}}^2/c^2$.



From CO to H

Once $N(\text{CO})$ has been determined: Infer H_2 column using some “standard” ratio. Typical assumptions:

$$\frac{N(^{13}\text{CO})}{N(\text{H}_2)} \sim 0.5 \dots 2.0 \times 10^{-6} \quad (3.10)$$

Ratio determined from UV-data on hydrogen and CO measurements at cloud edges (low τ).

Caveats:

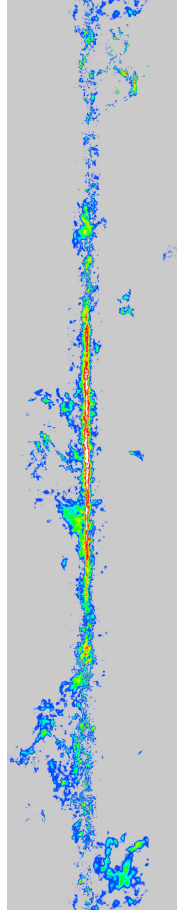
- CO usually *not* in LTE for higher J
- $n(\text{H}_2)/n(^{12}\text{C}), n(^{12}\text{C})/n(^{13}\text{C})$ affected by astration (passage of ISM through stars), $\implies n(^{12}\text{C})/n(^{13}\text{C}) = 20$ at GC, 90 at large Galactic radii,
- Clumpy clouds? Shadowing? (finite beamsize of telescope...),
- Isotope ratios very different between different cloud complexes
- ...

H_2 mass only determinable to factor of a few!

Molecules and Dust



Molecular Clouds



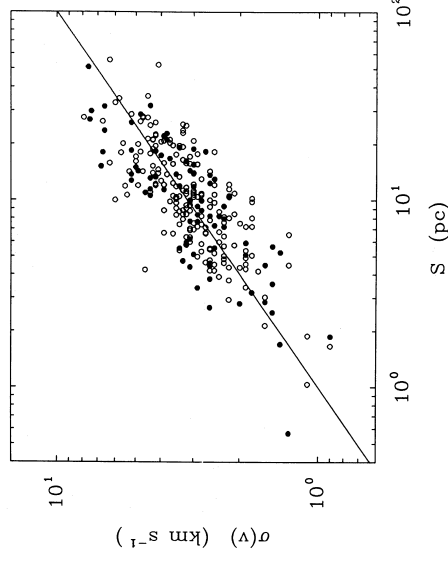
Dame et al., CfA; Columbia 1.2m telescope

CO distribution in galactic coordinates: concentration of clouds on plane; high speed at center not yet understood.

Molecules and Dust



Molecular Clouds



Solomon et al. (1987): 2.6 mm ^{12}CO survey of > 200 molecular clouds within solar circle.

Relationship between velocity dispersion, σ_v , (from line width) and cloud size, S :

$$\sigma_v = (1 \pm 0.1) \text{ km s}^{-1} \left(\frac{S}{\text{pc}} \right)^{0.5} \quad (3.11)$$

(Solomon et al., 1987, Fig. 1)

Molecules and Dust



Molecular Clouds

Median linewidth in Solomon survey:

$$\sigma_v \sim 3 \text{ km s}^{-1} \quad (3.12)$$

Compare to sound-speed, assuming $kT \sim 30 \text{ K}$

$$c_s \sim \sqrt{\frac{kT}{m_p}} \sim 0.5 \text{ km s}^{-1} \sqrt{\frac{T}{30 \text{ K}}} \quad (3.13)$$

σ_v dominated by turbulent velocity within clouds, not by sound speed...

Turbulent pressure $P \sim nm\sigma_v^2$, with $n \gtrsim 10^2 \text{ cm}^{-3}$, much higher than confining pressure in intra-cloud medium (there: $n \sim 1 \text{ cm}^{-3}, c_s \sim 10 \text{ km s}^{-1}$) \implies clouds confined by gravity!

Use virial theorem to obtain mass:

$$M \sim \text{const.} \frac{\sigma_v^2 S}{G} \quad (3.14)$$

where const. ~ 8.7 , depending on geometry.

Molecules and Dust



Molecular Clouds

Mass spectrum of molecular clouds is roughly

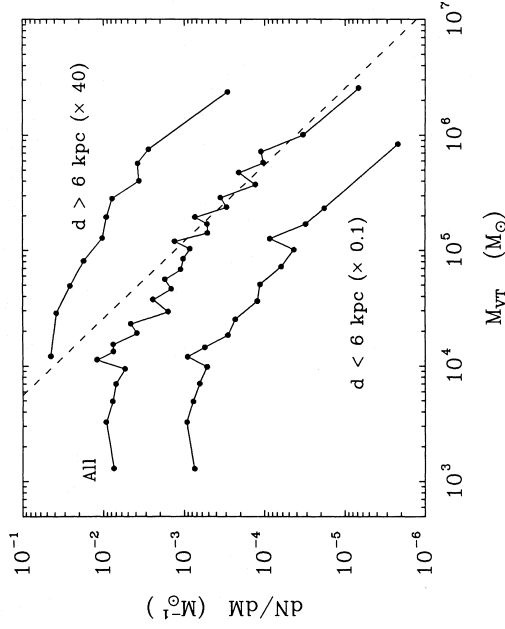
$$\frac{dN}{dM} \propto M^{-1.7} \quad (3.15)$$

for $2000 M_{\odot} < M < 40000 M_{\odot}$.

At low masses selection effect (biasing).

Integrating over mass distribution shows

Most of the Galaxy's molecular gas is in the most massive clouds



(Solomon & Rivolo, 1989, Fig. 1)

Molecules and Dust

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Molecule Formation

Formation of molecules in dense media (e.g., Earth's atmosphere) is no problem. This is very different from the rest of the universe!

Assume two-body collision of two (neutral) atoms: typical interaction timescale 10^{-13} s (1 vibration timescale).

To form molecule, need to get rid of excess energy!

Problem: Typical time for radiative relaxation given by A -coefficient ($\sim 10^8 \text{ s}^{-1}$)

\implies Typical collisional time-scale too low

\implies cannot form molecules!

On Earth, excess energy carried away by triple-collisions, these are too rare in the ISM...

Further complication: UV-dissociation of molecules.

Molecules and Dust

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Molecule Formation

Solution: "nonstandard chemistry", i.e., Atom-ion reactions and dust as catalyst Atom-ion reactions are, e.g.,



These reactions are very effective since the ion polarizes the molecule.

Langevin theory:

Assume charge q_1 approaches molecule; represent induced dipole-moment by charge q_2 separated by distance p . Then

$$q_2 p = \alpha E \quad (3.17)$$

where E electric field, α polarizability. Since $E = q_1/r^2$, this means

$$p = \frac{\alpha q_1}{q_2 r^2} \quad (3.18)$$

and the attractive force is

$$F_r = -\frac{2q_1 q_2 p}{r^3} = -\frac{2q_1^2 \alpha}{r^5} \quad (3.19)$$

Molecules and Dust

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Molecule Formation

Thus the potential energy is

$$V(r) = \int_r^\infty F_r dr = \frac{q_1^2 \alpha}{2r^4} \quad (3.20)$$

Motion in such a potential allows spiral-in (F can not always be balanced by centrifugal force).

This happens for impact parameters $b < b_0$ where

$$b_0 = q_1 \left(\frac{4\alpha}{\mu v^2} \right)^{1/4} \quad (3.21)$$

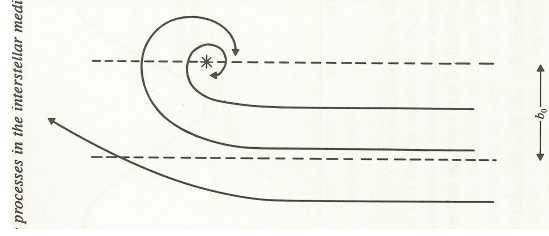
where μ is the reduced mass.

\implies Langevin cross section

$$Q = \pi b_0^2 \propto \frac{1}{v_{\infty}} \quad (3.22)$$

Since the collision frequency $\propto (Qv)$, collision frequency is independent of energy

Not really true in full theory, but dependence small for regime of astrophysical interest.

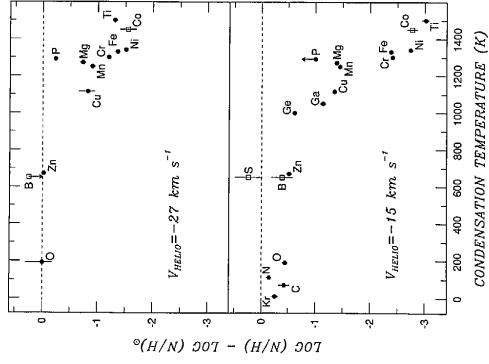


Molecules and Dust

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Dust



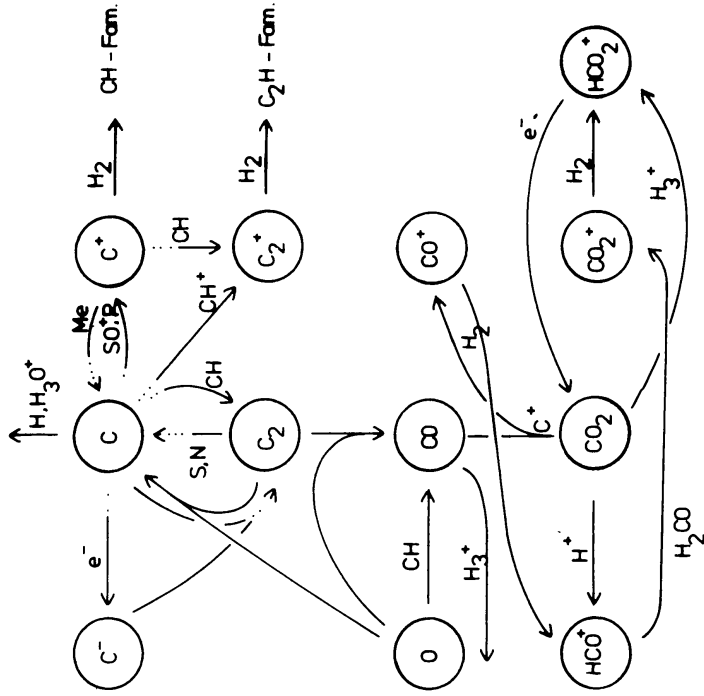
Evidence for existence of solid state material in universe comes mainly from two observations:

1. Depletion of elements in ISM gas phase wrt. solar abundances
2. Reddening of stars

Abundances in direction to ζ Oph (Federman et al., 1993)

Typical theory of molecular formation: reaction networks with ~ 1000 and more different reactions.

Henning, 1981



Hydrogen Molecule

One unavoidable fact: we cannot produce H_2 in gas phase \implies this must occur on surface of dust grains.

Why?

Two-body recombination is not possible because H_2 has no dipole moment \implies radiative relaxation would go via quadrupole terms, which is **very slow**.

Therefore: the general picture is:

adsorption of H on grain surface (e.g., ice, silicate) \implies proton will thermally "hop" over surface (tunnel through lattice structure,...) \implies Two H-atoms meet \implies formation of H_2

Detailed theory requires knowledge about grains.

Extinction

Extinction = dimming of starlight by dust
How is this measured?

Assume two stars, 1,2, at distances d_1, d_2 , with same physical spectral shape, $F(\lambda)$. Medium to star 2 has optical depth $\tau(\lambda)$. Observed spectral fluxes are

$$F_1(\lambda) = \frac{F(\lambda)}{d_1^2} \quad \text{and} \quad F_2(\lambda) = \frac{F(\lambda)}{d_2^2} e^{-\tau(\lambda)} \quad (3.23)$$

Compare fluxes at wavelength λ_1 :

$$\frac{F_1(\lambda_1)}{F_2(\lambda_1)} = \frac{F(\lambda_1)/d_1^2}{F(\lambda_2)/d_2^2} e^{\tau(\lambda_1)} = \frac{d_2^2}{d_1^2} e^{\tau(\lambda_1)} \quad (3.24)$$

Same at λ_2 :

$$\frac{F_1(\lambda_2)}{F_2(\lambda_2)} = \frac{d_2^2}{d_1^2} e^{\tau(\lambda_2)} \quad (3.25)$$

Therefore

$$\frac{F_1(\lambda_1)/F_1(\lambda_2)}{F_2(\lambda_1)/F_2(\lambda_2)} = e^{\tau(\lambda_1) - \tau(\lambda_2)} \quad (3.26)$$

**Extinction**

Take the logarithm of both sides and multiply with -2.5 :

$$-2.5 \log \left(\frac{F_1(\lambda_1)}{F_1(\lambda_2)} \right) - \left(-2.5 \log \left(\frac{F_2(\lambda_1)}{F_2(\lambda_2)} \right) \right) = \text{const.} \cdot (\tau(\lambda_1) - \tau(\lambda_2)) \quad (3.27)$$

Now remember the definition of the magnitude

$$m(\lambda_1) - m(\lambda_2) = -2.5 \log \frac{F(\lambda_1)}{F(\lambda_2)} \quad (3.28)$$

Therefore Eq. (3.27) reads

$$(m_1(\lambda_1) - m_1(\lambda_2)) - (m_2(\lambda_1) - m_2(\lambda_2)) = \text{const.} \cdot (\tau_1 - \tau_2) \quad (3.29)$$

In astronomy, a color is defined as a difference of magnitudes, e.g. for the B- and V-filters:

$$B - V = m(B) - m(V) \quad (3.30)$$

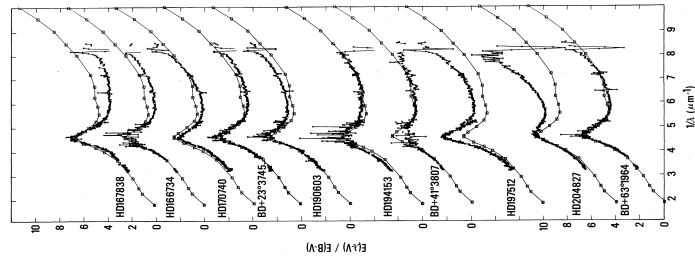
Thus, Eq. (3.29) is difference between colors, or color excess

$$E_{\lambda_1-\lambda_2} := (m_1(\lambda_1) - m_1(\lambda_2)) - (m_2(\lambda_1) - m_2(\lambda_2)) \quad (3.31)$$

Note that because of Eq. (3.29)

$$E_{\lambda_1-\lambda_2} \propto \tau_1 - \tau_2 \quad (3.32)$$

Molecules and Dust



Generally, we use normalized color excess,

$$\frac{E(\lambda - V)}{E(B - V)} = \frac{\tau(\lambda) - \tau(V)}{\tau(B) - \tau(V)} \quad (3.33)$$

$$\propto \frac{\tau(\lambda) - \tau(V)}{\tau(B) - \tau(V)} \quad (3.34)$$

$$\propto \tau(\lambda) \quad (3.35)$$

$$\propto \sigma_{\text{sca}}(\lambda) \quad (3.36)$$

Stellar spectra in the UV (Witt et al., 1984): Overall the extinction is very similar, there is a prominent feature at $1/\lambda \sim 4.6$ ($\lambda = 2170\text{\AA}$), the strength of the feature varies, but its position is very stable.

**Extinction**

Observationally important is relationship between reddening $E(B - V)$ and extinction in V-band.

Extinction defined via

$$A_V = V - V_0 \quad (3.37)$$

Now, normalized extinction was

$$\frac{E(\lambda - V)}{E(B - V)} = \frac{(m_\lambda - m_V) - (m_\lambda - m_V)_0}{E(B - V)} \quad (3.38)$$

$$= \frac{m_\lambda - m_{\lambda,0} - (m_V - m_{V,0})}{E(B - V)} \quad (3.39)$$

$$= \frac{A_\lambda - A_V}{E(B - V)} \quad (3.40)$$

But for $\lambda \rightarrow \infty$:

$$\frac{E(\lambda - V)}{E(B - V)} \rightarrow \text{const.} =: R \quad (3.41)$$

where $R \sim 3.1 \pm 0.1$.

$\Rightarrow A_V$ known if $E(B - V)$ known!

Note also that $A_V/E(B - V) \propto \tau$ since $\tau = n\sigma_{\text{sca}}r$

\Rightarrow can measure distance! Generally, $A_V \sim 1 \dots 2 \text{ mag pc}^{-1}$.

Molecules and Dust

**Extinction**

The normalized reddening observed is roughly $\propto 1/\lambda$.

Explanation: scattering of radiation on grains.

The overall theory is very complicated, so only show the rough idea here...
In scattering, intensity is

$$I = I_0 \exp(-n\pi a^2 Q l) \quad (3.42)$$

where the quality factor Q has two components:

$$Q = Q_{\text{abs}} + Q_{\text{sca}} \quad (3.43)$$

Q_{abs} : absorption,

Q_{sca} : scattering.

(see next slide)

Note that Q is proportional to the optical depth...

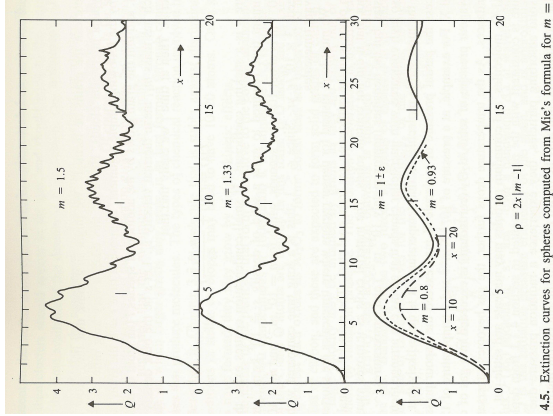
Define the Albedo of particles

$$\gamma = \frac{Q_{\text{sca}}}{Q_{\text{abs}} + Q_{\text{sca}}} \quad (3.44)$$

(note that in principle there is also an angular dependence)

Molecules and Dust

Extinction



4.5. Extinction curves for spheres computed from Mie's formula for $m = 1.5$, 1.33 , and $1.2 + i\epsilon$.

Detailed theory: Mie scattering; gives $Q \propto 1/\lambda$ for small diameters $a \implies$ as observed!

Q_{sea} as a function of $x = 2\pi a/\lambda$ for several dielectric constants m (Dyson & Williams, Fig. 4.5; $m = 1.33$ is water/ice)

Extinction

For detailed theory also need size distribution of grains.

Common assumption:

$$n(a) = Aa^{-3.5} \quad (3.45)$$

("MRN distribution"; Mathis, Rumpel, Nordsieck; $0.005 \mu\text{m} < a < 0.25 \mu\text{m}$) determined from fitting extinction curves.

Overall $1/\lambda$ -behavior is understood as being due to Mie scattering

2200 Å feature:

- **graphite** grains? Optical constants change dramatically around 2200 Å for small graphite grains.
- **Silicate** grains?
- **Polycyclic aromatic hydrocarbons (PAHs)**?

Dust Models

Major dust models:

- MRN model
- Core-mantle models
- post-IRAS models

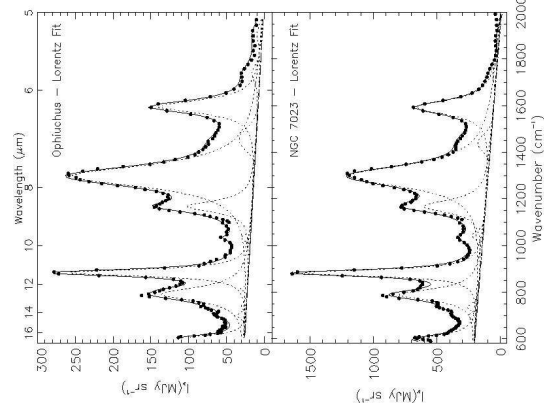


Models must take constraints on dust models into account:

- extinction curve (IR to UV)
- abundance deficiency of ISM gas phase
- (narrow) spectral features

See Witt, IAU Symp. 197, for a discussion of results.

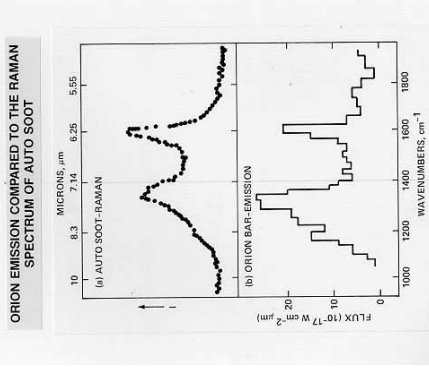
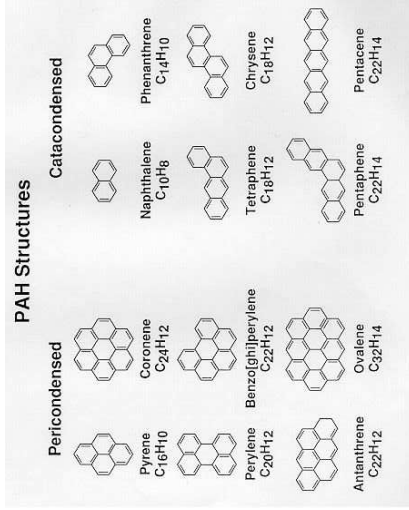
UIBs



Unidentified emission structures seen at 3.3, 6.2, 7.7, 8.6, 11.3 μm seen in H II regions, YSOs, diffuse ISM, and even AGN: "unidentified infrared bands"

(Boulanger et al., 1998)

PAHs

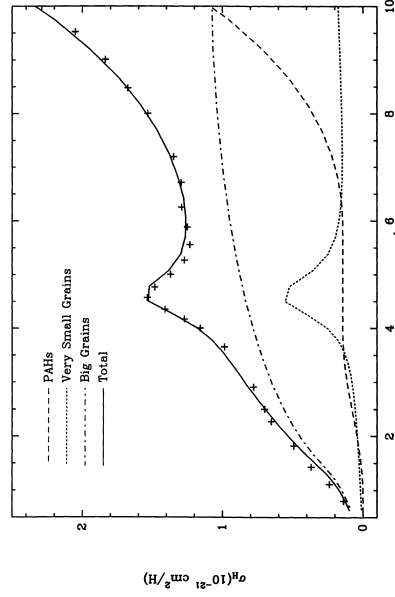


UIB emission is probably due to polycyclic aromatic hydrocarbons (PAHs), complex large carbonaceous molecules (UIB: related to C-C, C-H modes)

Molecules and Dust

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PAHs



Inclusion of PAHs in dust models can also account for extinction curve, need three distinct populations:

- big grains (15 nm to 110 nm),
- very small grains (1.2 nm to 15 nm)
- **PAHs** (<1.2 nm)

Also predicts UIB emission!

Désert, Boulanger, Puget (1990)

A problem with the Désert et al. model is the small size of large grains, which is inconsistent with X-ray halos... Possible solution: fluffy grains (Fogel & Leung, 1998)

Molecules and Dust

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Dust Formation

Where does dust come from?

Three potential sources:

1. Condensation out of the ISM
2. Condensation in cool stellar outflows
3. Condensation in protostars

and 1) only possible in very dense molecular clouds: formation of clusters of 10...20 atoms as "condensation nuclei"; accretion of further molecules via collisions.

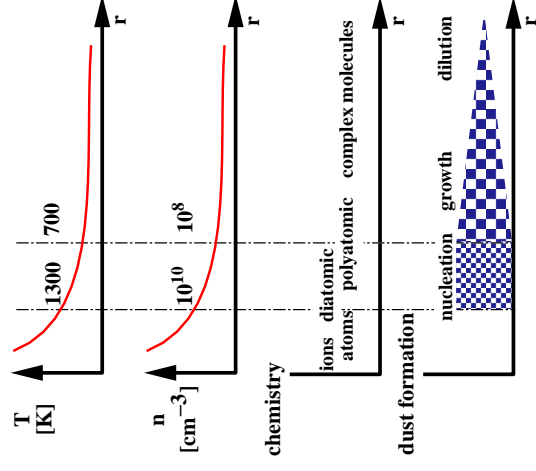
Due to small densities dust formation timescale very long (10^8 years), thus rather impossible.

Dust is mainly generated in stars and then ejected into the ISM.

Molecules and Dust

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Dust Formation



Dust formation in stars

Stellar atmospheres have much higher density than GMCs (solar photosphere: 10^{17} cm^{-3} , late type giants: $\sim 10^{15} \text{ cm}^{-3}$, compared to 10^6 cm^{-3} in GMCs)

⇒ much higher condensation probability.

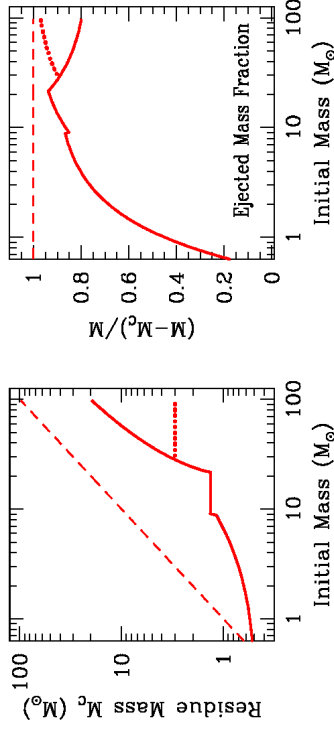
General process:

1. formation of molecules
2. accretion of more material, formation of clusters
3. formation of macroscopic particles

(Sedlmayr & Krüger, 1997)

Molecules and Dust

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**Closed Box Model**

(Prantzos, 2008, Fig. 2)

Galactic metallicity evolution is influenced by:

- stellar mass ejection rates

Chemical Evolution

**Closed Box Model**

Galactic metallicity evolution is influenced by:

- stellar evolution (see previous slides)
- inflow from outside galaxy
- ejection from galaxy
- mixing of elements within galaxy (influences populations).

Will look here at a simple model: one-zone, instantaneous recycling:

- gas well mixed
- stars return fusion products immediately
- no gas escapes/added (closed-box model)

Chemical Evolution

**Closed Box Model**

Let

- $M_g(t)$: Mass of gas in galaxy at time t
- $M_s(t)$: Mass in low-mass stars and compact objects (i.e., mass locked in stellar objects throughout lifetime of Galaxy)
- $M_h(t)$: Mass of metals ($Z > 2$) in galactic gas.

Then the Metal abundance is

$$Z(t) = \frac{M_h(t)}{M_g(t)} \quad (3.46)$$

Stellar lifetimes:

- $Z = Z_\odot, M = M_\odot \implies \tau \sim 11.4 \text{ Gyr}$,
- $Z = Z_\odot, M = 0.8 M_\odot \implies \tau \sim 23 \text{ Gyr}$,
- $Z = 0.05 Z_\odot, M = 0.8 M_\odot \implies \tau \sim 13.8 \text{ Gyr}$

Stars with $M = 0.8 M_\odot$: lowest mass stars that have ever died (=heaviest stars surviving in oldest globular clusters).

Chemical Evolution

**Closed Box Model**

Assume formation of massive stars which produce metals. Let

- ΔM_s : mass in remnants
- $p \cdot \Delta M_s$: mass returned to ISM (p : yield, depends on initial mass function and evolution)
- $Z \cdot \Delta M_s$: metals locked in remnants

\implies change in mass of metals due to formation of stars given by

$$\Delta M_h = p \cdot \Delta M_s - Z \cdot \Delta M_s = (p - Z) \Delta M_s \quad (3.47)$$

(assuming instantaneous recycling)

\implies metallicity increases by

$$\Delta Z = \Delta \left(\frac{M_h}{M_g} \right) = \frac{p \cdot \Delta M_s - Z (\Delta M_s + \Delta M_g)}{M_g} \quad (3.48)$$

where $-Z \cdot \Delta M_g$ term due to exchange of mass with other regions.

Note that in the closed box case (no gas enters/leaves the system):

$$\Delta M_s = -\Delta M_g \quad (3.49)$$

Chemical Evolution



Closed Box Model

Define as primary elements those elements for which the formation is independent of Z (i.e., p independent of Z).

For these elements and a closed box ($\Delta M_s = -\Delta M_g$):

$$\Delta Z = \frac{p \cdot \Delta M_s - Z(\Delta M_s + \Delta M_g)}{M_g} = -p \frac{\Delta M_g}{M_g} \implies \frac{dZ}{dt} = -\frac{p}{M_g} \frac{dM_g}{dt} \quad (3.50)$$

such that

$$\int_0^t \frac{dZ}{dt} dt = -p \int_{M(t=0)}^{M(t)} \frac{dM_g}{M_g} = -p \ln \frac{M_g(t)}{M_g(t=0)} \quad (3.51)$$

and finally

$$Z(t) = Z(t=0) + \ln \frac{M_g(t)}{M_g(t=0)} \quad (3.52)$$

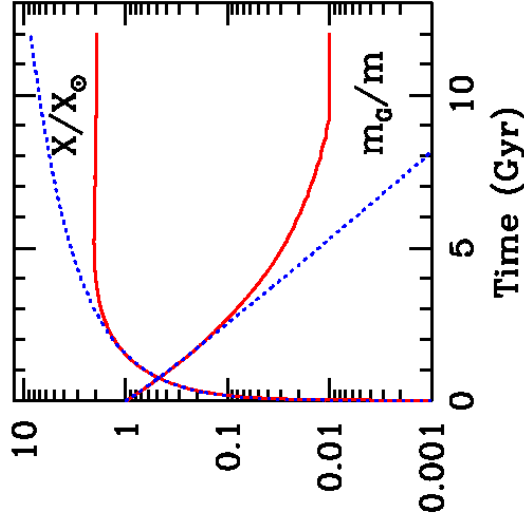
Note that $M_g(t) < M_g(t=0)$, and therefore $\ln M_g(t)/M_g(t=0) > 0$, such that

- $Z(t)$ increases with time, and
- $Z(t)$ is higher in regions with less gas.

Chemical Evolution



Closed Box Model



Evolution of abundance, X , and gas fraction, m_g , with time.

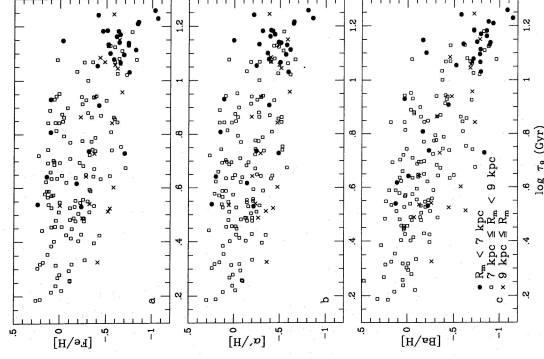
Calculations for closed box model in Instantaneous Recycling Approximation (IRA) and Non-IRA (stellar evolution)

(Prantzos, 2008, Fig. 12)

Chemical Evolution



Closed Box Model



Younger stars in solar vicinity tend to be richer in metals.

Notation used:

$$[\text{Fe}/\text{H}] = \log_{10} \frac{A_{\text{Fe}}/A_{\text{H}}}{A_{\text{Fe},\odot}/A_{\text{H},\odot}} \quad (3.53)$$

where

- A_i : abundance by number of element i , and
 - $A_{i,\odot}$: solar abundance by number of element i .
- α : α -process elements (esp. Mg, Si, Ca, Ti)

Edvardsson et al. (1993, Fig. 14)

Chemical Evolution



Closed Box Model

We had

$$Z(t) = Z(t=0) + \ln \frac{M_g(t=0)}{M_g(t)} \quad (3.52)$$

But the mass in low-mass stars formed before time t is

$$M_s(t) = M_g(t=0) - M_g(t) \quad (3.54)$$

But these stars have lower metallicity. Therefore the mass in low metallicity stars is

$$M_s(Z < Z(t)) = M_g(t=0) \left(1 - \exp \left\{ -\frac{Z(t) - Z(t=0)}{p} \right\} \right) \quad (3.55)$$

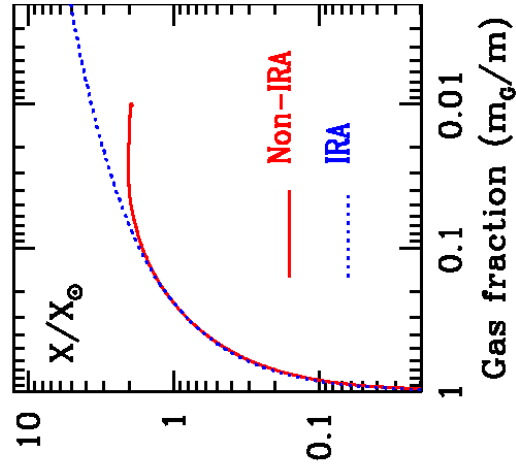
Where the gas density is high vs. number of stars, the average metallicity must be low.

This effect is seen, e.g., in Large Magellanic Cloud or as metal abundance gradient in spirals.

Chemical Evolution



Closed Box Model



Abundance as function of gas fraction in the closed box model in Instantaneous Recycling Approximation (IRA) and Non-IRA (stellar evolution).

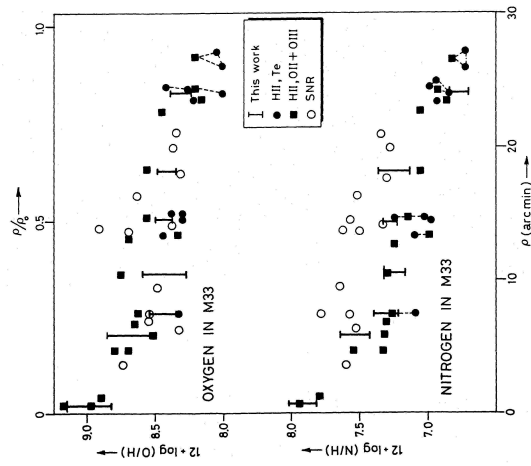
(Prantzos, 2008, Fig. 12)

Chemical Evolution

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Closed Box Model



Spiral galaxies generally show abundance gradients away from their core, as predicted by closed box models.

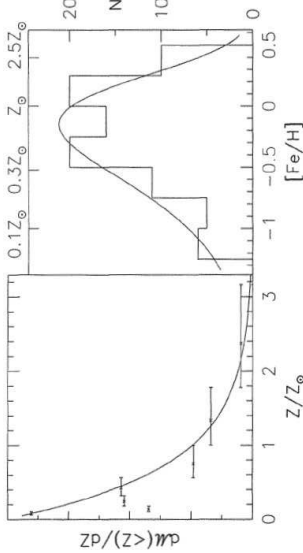
(Vilchev et al., 1988, Fig. 9)

Chemical Evolution

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Closed Box Model



The metallicity in low-mass stars was

$$M_s(<Z) = M_{g,0} \left(1 - e^{-\frac{Z(t)-Z_0}{p}} \right) \quad (3.55)$$

and once all gas is gone, the mass of stars with metallicity in $[Z, Z + \Delta Z]$:

$$\frac{dM_s(<Z)}{dZ} \Delta Z \propto \exp \left(-\frac{Z(t) - Z(t=0)}{p} \right) \Delta Z \quad (3.56)$$

This reproduces well the metallicity distribution found in the galactic bulge (see figure), and one finds $p \sim 0.7 Z_\odot$.

Bulge seems to have managed to convert all of its gas into stars!

Chemical Evolution

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Problems of Closed Box



Dwarf spheroidal galaxy Leo I (next to Regulus)

1. loss of metals? \implies galaxies have low mass, thus escape velocity is low (2nd explanation is preferred)

For other regions, closed box is clearly wrong

Dwarf spheroidal galaxies: very little gas, but metallicity still low.

Two explanations:

1. Possibly low formation of massive stars (=different Initial Mass Function) \implies little formation of metals?

Chemical Evolution

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Solar Neighborhood

Surface density $\Sigma = \int_{-\infty}^{+\infty} n dl$ of stuff in solar neighborhood:

- stellar density: $\Sigma = 30\text{--}40 M_{\odot} \text{pc}^{-2}$ ($30 M_{\odot} \text{pc}^{-2}$ in stars, $8 M_{\odot} \text{pc}^{-2}$ in stellar residues)
- gas density: $\Sigma = 13 M_{\odot} \text{pc}^{-2}$

so total surface density is $50 M_{\odot} \text{pc}^{-2}$.

n : mass density ($M_{\odot} \text{pc}^{-3}$)

In neighborhood, abundance is $0.7Z_{\odot}$ (i.e., Sun is enriched!). Therefore

$$Z(\text{now}) = 0.7Z_{\odot} = p \ln(50/13) \implies p \sim 0.5Z_{\odot} \quad (3.57)$$

this is slightly lower than bulge ($p \sim 0.7Z_{\odot}$), but could be explained if disk is less efficient in retaining gas (galactic fountain!).

However, further problem: predicted fraction of metal poor stars

$$\frac{M_s(Z < 0.25Z_{\odot})}{M_s(Z < 0.7Z_{\odot})} = \frac{1 - \exp(-Z_{\odot}/4p)}{1 - \exp(-0.7Z_{\odot}/p)} \sim 0.52 \quad (3.58)$$

so 50% of all stars in vicinity should have low abundances.

Reality: <20% of all stars have $Z < 0.25Z_{\odot}$: G-dwarf problem

Possible solution: local region was enriched by Supernovae to $Z(0) \sim 0.15Z_{\odot}$.

Chemical Evolution

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