Division of Solar System into two major types of planets:

1. Inner "Terrestrial" Planets: Mercury, Venus, Earth/Moon, Mars:
$\Longrightarrow$ all similar to Earth ("rocks").
$\Longrightarrow$ no moons (Earth/Moon better called "twins")
$\Longrightarrow$ Moons of
2. Outer Planets: Jupiter, Saturn, Uranus, Neptune:
$\Longrightarrow$ "gas giants"
$\Longrightarrow$ all have extensive moon systems
Although not planets (i.e., motion not around Sun), large moons of gas giants are very similar in structure to terrestrial planets.
Plan for this and next lecture:
3. Surfaces / Interiors of terrestrial planets
4. Atmospheric structure of gas giants (and terrestrial planets)

Planets: Overview
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The Inner Planets (SSE, NASA)

Lithosphere


Structure of terrestrial planets:

- Core: high-density material (Fe)
- Mantle: plastic materials, hot (e.g., Earth: molten rocks)
- Lithosphere: rigid material, e.g., Silicates

Knowledge of structure important for, e.g.,

- origin of magnetic fields (thought to be caused by molten core $\Longrightarrow$ currents $\Longrightarrow B$-field ("dynamo"). Details unknown).
- atmospheric composition (molten mantle $\Longrightarrow$ volcanism $\Longrightarrow \mathrm{CO}_{2}, \mathrm{CH}_{4}, \ldots$ )



## Mercury:

- not much larger than Moon
- densest of all terrestrial planets
- no evidence for atmosphere
- Rotation period: $59 \mathrm{~d}, 2 / 3$ of orbital period.
- surface: impact craters and tectonics
- Only information available is from Mariner 10 (three flybys, 1974/1975)
- ESA Mission Bepi Colombo, planned for ~2012
- NASA mission "Messenger"
(launched 2004 August 3, flyby 2008 and 2009, in orbit from 2011 on)


Caloris Basin ( 1300 km diameter) close to sub-solar point at perihelion
$\Longrightarrow$ hot ( $T>400^{\circ} \mathrm{C}$ on day, $T \sim-170^{\circ} \mathrm{C}$ during night) result of large impact event

Major landforms: Craters


NASA/JPL
Terraced craters, with central mountains.


Robinson, NWU / NASA
Hilly/lineated terrain antipodal to
Caloris ( 120 km across)
$\Longrightarrow$ effect of shock from Caloris impact.


S-Pole; NASA/JPL
50 km diam craters with rays (remains from impact)

Physics of impact cratering:
Kinetic energy:

$$
E=\frac{1}{2} m v^{2}=\frac{1}{2} \cdot \frac{4}{3} \pi r^{3} \rho v^{2}=\frac{\pi d^{3} \rho v^{2}}{12}
$$

Important numbers:

- Velocity of impact: several times orbital speed of planet
- Impacting body: rock or Fe, several meters to kilometers in size


## Example:

E.g., $v=10 \mathrm{~km} \mathrm{~s}^{-1}, d=25 \mathrm{~m}, \rho=7900 \mathrm{~kg} \mathrm{~m}^{-3}$
$\Longrightarrow E=3 \times 10^{15} \mathrm{~J}(\sim 1$ Megaton of TNT)
1 Megaton TNT is typical strength of US nuclear bombs [B-83 bomb],
UK's Trident bombs correspond to $\sim 0.3-100$ kilotons TNT.
French, 1998, Traces of Catastrophe, LPI Contribution 954, p. 21

## Venus:



- similar size to Earth, similar structure
- insolation $\sim 2 \times$ Earth
- very slow rotation ( 243 d , retrograde; $\Longrightarrow$ no $B$-field)
- very dense atmosphere: surface pressure $\sim 90 \times$ Earth
- atmosphere: $96.5 \% \mathrm{CO}_{2}, 3.5 \% \mathrm{~N}$ $\Longrightarrow$ strong greenhouse effect
$\Longrightarrow$ surface temperature $\sim 460^{\circ} \mathrm{C}$.
- acid rain (yes, sulphuric acid!)

NASA, Pioneer Venus
Information mainly from radar surveying from Earth and from Magellan (1990-1994), plus images from Pioneer Venus Probe (1979). Several landings (Venera, 1975/1981)

## Major landforms


$440 \times 350 \mathrm{~km}^{2}$ area in Eistla Regio, shows basic stratigraphy (sequence of geologic events): right half: old highlands, fractured structure ( $\sim 15 \%$ of surface), left part: lowlands, younger area, origin in former volcanism?
Craters (note: strong erosion $\Longrightarrow$ fewer craters overall)


Eistla Regio; heights exagerrated by factor 22.5

courtesy D.P. Mitchell
Venera 13 (3 March 1982): reanalysed image without camera distortion

Earth:

- double planet system
- Earth surface: dominated by plate tectonics, erosion
- atmosphere: $80 \% \mathrm{~N}_{2}, 20 \% \mathrm{O}_{2}$
$\Longrightarrow$ moderate greenhouse effect
$\Longrightarrow$ surface temperature $>0^{\circ} \mathrm{C}$.
- water present


## Moon:

- very similar to Mercury, overall
- Mariae (plains from massive impacts) and impact craters
- Rotation synchronous to orbit around Earth


V. L. Sharpton

Earth: Wolf Creek Crater, Australia
Currently 172 confirmed impact structures on Earth


Evidence for plate tectonics (few craters!) , volcanism,...


NASA
Evidence for life - note light pollution


Earth's Moon : surface dominated by mariae (large, dark
lava basins) and craters (only most prominent shown).

## Mars:



- smaller than Earth
- very low density ( $\langle\rho\rangle \sim 3 \mathrm{~g} \mathrm{~cm}^{-3}$ )
$\Longrightarrow$ small core, probably Fe and $\mathrm{Fe}_{x} \mathrm{~S}_{y}$,
- polar caps, seasons
- thin atmosphere, clouds, fog,...
- water sublimes $\Longrightarrow$ no liquid water today
- Volcanism (large shield volcanoes $\Longrightarrow$ no (?) plate tectonics)
- atmosphere: $95 \% \mathrm{CO}_{2}$
$\Longrightarrow$ weak greenhouse effect
- two moons (captured asteroids)

NASA, Mars Global Surveyor
Early Exploration through Mariner missions and Viking 1 and Viking 2 orbiters and landers in 1970s, recently, strong interest (NASA Mars Global Surveyor [MGS], ESA Mars Express, plus several landers). Currently best surveyed planet except for Earth.

Mars:



Rim of Valles Marineris Sedimentary rocks, steep slope caused by faulting, possible location of fault two-thirds down the slope.

NASA MGS, 6 September 2003, image: 3 km wide


Don Davis/NASA
Viking lander 2: frost (water ice) in early morning (very thin layer [ $<0.1 \mathrm{~mm}$ ])


NASA/JPL/MSSS
Mars' Polar Caps: Mainly $\mathrm{CO}_{2}$ ice ("dry ice"), grows and shrinks with seasons.


The Outer Planets (SSE, NASA)


Jupiter:

- Largest planet in solar system
- rapid rotation $\Longrightarrow$ severely flattened, banded atmosphere (Coriolis force), Great Red Spot
- strong magnetic field (strong radio emission)
- atmosphere: $75 \% \mathrm{H}, 24 \% \mathrm{He}$ (by mass), very close to solar
- differential rotation (rotation period $9 h 50 \mathrm{~m}$ on equator, 9 h 55 m on poles).
- strong magnetic field
- four major "Galilean" moons plus 59 small ones (as of Jan. 2005; all are captured asteroids)


Cassini, 2000 Dec 31

Jupiter: true color image; colors likely from trace content of organic compounds in atmosphere
false color image, red: waterclouds, dark spots: deep hot spots

Overall atmospheric structure: three layers:
Ammonia - ammonia hydrosulfide ( $\mathrm{NH}_{4} \mathrm{HS}$ ) - water ice/water (deepest)


Great Red Spot
NASA Galileo, 1996 June 26

Great Red Spot: Storm System, $\sim 2 \times$ Earth diameter, exists since more than 300 years, 8 km above and $10^{\circ}$ cooler than surrounding region (rising high pressure region), rotates counterclockwise (Coriolis force on Southern hemisphere).

Structure of atmosphere defined through hydrostatic equilibrium:
Force on area $A$ by slab of gas of area $A$ and density $\rho$ :

$$
F=m g=\rho V g=A h \rho g
$$

Such that pressure becomes

$$
P=\frac{F}{A}=\rho h g
$$

where $g$ gravitational acceleration.
For thin atmosphere ( $g$ constant): Decrease of $P$ when going upwards by $\Delta h$ :

$$
\Delta P=-\rho g \Delta h \quad \text { and for } \lim _{\Delta h \rightarrow 0}: \frac{\mathrm{d} P}{\mathrm{~d} h}=-\rho g
$$

The Outer Planets
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## Jupiter, V

For (ideal) gas: relationship between density and pressure ("equation of state") given by

$$
P=(\rho / m) k T
$$

where $T$ : Temperature ( $\mathrm{K}!$ ), $m$ : average mass per gas particle, $k$ : Boltzmann's constant $k=1.38 \times 10^{-23} \mathrm{JK}^{-1}$. Therefore:

$$
\frac{\mathrm{d} P}{\mathrm{~d} h}=-\left(\frac{m g}{k T}\right) P
$$

For isothermal atmosphere separation of variables (see handout) gives

$$
P(h)=P_{0} \exp \left(-\frac{m g}{k T} \cdot h\right)=P_{0} \exp \left(-\frac{h}{H}\right)
$$

The pressure in the atmosphere thus decreases exponentially, the characteristic height scale of the decrease is given by the scale height $H$.
On Earth, $H \sim 9 \mathrm{~km}$.

Separation of variables is a standard technique for solving boundary conditions such as the equation of hydrostatic equlibrium,

$$
\frac{\mathrm{d} P}{\mathrm{~d} h}=-\left(\frac{m g}{k T}\right) P
$$

In order to obtain $P$ as a function of height, $h$, we need to solve this differential equation with the boundary condition that for $h=0, P=P_{0}$.
First, divide by $P$ and integrate both sides of the equation with respect to height:

$$
\int_{0}^{h} \frac{1}{P} \frac{\mathrm{~d} P}{\mathrm{~d} h} \mathrm{~d} h=-\int_{0}^{h}\left(\frac{m g}{k T}\right) \mathrm{d} h
$$

we can now substitute $P(h)$ for $h$ on the left hand side. Using the chain rule gives

$$
\int_{P_{0}}^{P(h)} \frac{\mathrm{d} P^{\prime}}{P^{\prime}}=-\int_{0}^{h}\left(\frac{m g}{k T}\right) \mathrm{d} h
$$

such that
and exponentiating then gives

$$
\ln \left(\frac{P(0)}{P(h)}\right)=-\left(\frac{m g}{k T}\right) h
$$

$$
P(h)=P_{0} \mathrm{e}^{-(m g / k T) h}
$$

This method is called "separation of variables" since people often jump from the first (linear) equation to the third one in one step, by "separating the dependent from the independent variable":

$$
\frac{\mathrm{d} P}{\mathrm{~d} h}=-\left(\frac{m g}{k T}\right) P \quad \Longrightarrow \quad \frac{\mathrm{~d} P}{P}=-\left(\frac{m g}{k T}\right) \quad \Longrightarrow \quad \int_{P_{0}}^{P(h)} \frac{\mathrm{d} P^{\prime}}{P^{\prime}}=-\int_{0}^{h}\left(\frac{m g}{k T}\right) \mathrm{d} h
$$

In general, gas giants have very different properties from terrestrial planets:

- average density low, e.g.,
- Jupiter: $\langle\rho\rangle \sim 1.3 \mathrm{~g} \mathrm{~cm}^{-3}$
- Saturn: $\langle\rho\rangle \sim 0.7 \mathrm{~g} \mathrm{~cm}^{-3}$
(compare to terrestrial planets: $\langle\rho\rangle \sim 5.5 \mathrm{~g} \mathrm{~cm}^{-3}$; water has $\rho=1 \mathrm{~g} \mathrm{~cm}^{-3}$ ).
- elemental composition similar to stars (by mass):
$-75 \%$ H
$-24 \% \mathrm{He}$
- 1\% rest ("metals")
$\Longrightarrow$ expect fundamentally different internal structure!

Structure of a gas giant from equation of hydrostatic equilibrium:

$$
\frac{\mathrm{d} P}{\mathrm{~d} r}=-\rho(r) \frac{G M(r)}{r^{2}}
$$

To solve, need to know $\rho(r), M(r) \Longrightarrow$ complicated, but doable if properties of material are known.
To guesstimate the central pressure, one can show for a planet of radius $R$ :

$$
P_{\text {central }}=\frac{2 \pi}{3} G\langle\rho\rangle^{2} R^{2}
$$

(see handout for derivation).
Plug in numbers for Jupiter: $R=70000 \mathrm{~km},\langle\rho\rangle=1.3 \mathrm{~g} \mathrm{~cm}^{-3}$, get $P_{\text {central }}=1.2 \times 10^{12} \mathrm{~Pa}(10 \times$ Earth $)$.
At this pressure: existence of metallic hydrogen (i.e., electrons can move freely around).
more detailed computations: metallic hydrogen from 14000-45000 km away from center

## The Outer Planets

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Note: relative sizes of planets not to scale! Also rotational flattening not taken into account.

The following is for your education only and its knowledge will not be assessed in any way!
To obtain information on the pressure structure of any gravitationally supported static body we can again use the concept of hydrostatic equilibrium already used for estimating the structure of atmospheres,

$$
\frac{\mathrm{d} P}{\mathrm{~d} r}=-\rho(r) g(r)
$$

here, $r$ is now the radial distance from the planetary centre. In contrast to atmospheres, the acceleration $g$ depends on the position, $g=g(r)$. It is easy to show that

$$
g(r)=\frac{G M(r)}{r^{2}}
$$

where $M(r)$ is the mass of the planet contained within the radius $r$ :

$$
M(r)=\int_{0}^{r} \frac{4 \pi}{3} \rho(r) r^{2} \mathrm{~d} r
$$

(interpretation: integrate over onion shells of thickness $\mathrm{d} r$ and density $\rho(r)$; the mass in each of these shells is $(4 \pi / 3) \rho(r) \mathrm{d} r$, summing over all onion shells gives the above answer).

To solve the equation of the hydrostatic equilibrium one needs to know the equation of state. Unfortunately, this equation of state is generally much more complicated than for gases and often only roughly known. One can estimate, however, the order of magnitude for the pressure within a planet. In order to do so, we assume that the density is the same throughout the planet, and that it equals the planet's average density $\rho(r)=\langle\rho\rangle=$ const.. This is o.k. to an order of magnitude. Under this assumption,

$$
M(r)=(4 / 3) \pi r^{3}\langle\rho\rangle
$$

such that the equation of hydrostatic equilibrium reads

$$
\frac{\mathrm{d} P}{\mathrm{~d} r}=\langle\rho\rangle^{2} G(4 / 3) \pi r
$$

Differential equations looking like this are called separable. They can be solved "separation of variables", as we already did when computing the structure of an isothermal atmosphere.

First integrate both sides of the equation from $r=0$ to the surface of the planet at $r=R$ :

$$
\int_{0}^{R} \frac{\mathrm{~d} P}{\mathrm{~d} r} \mathrm{~d} r=\int_{0}^{R}\langle\rho\rangle^{2} G(4 / 3) \pi r \mathrm{~d} r
$$

To integrate the left hand side of the equation, substitute $r \longrightarrow P(r)$ where $P(r)$ is an unknown function (the pressure as a function of radius $r$ ). Luckily enough, we only need to know its values at $r=0$ and $r=R$ (the "boundary conditions"). By definition of the surface of the planet, the pressure at $r=R$ will be $P(R)=0$ to very good

## BIBLIOGRAPHY

accuracy, while the pressure at $r=0$ is the (unknown) central pressure, $P(0)=P_{\mathrm{c}}$. Therefore

$$
\int_{0}^{R} \frac{\mathrm{~d} P}{\mathrm{~d} r} \mathrm{~d} r=\int_{P_{\mathrm{c}}}^{0} \mathrm{~d} P=-P_{\mathrm{c}}
$$

The right hand side of the equation is easily found as well:

$$
\int_{0}^{R}\langle\rho\rangle^{2} G(4 / 3) \pi r \mathrm{~d} r=-\langle\rho\rangle^{2}(4 \pi / 3) G \int_{0}^{R} r \mathrm{~d} r=-\langle\rho\rangle^{2}(4 \pi / 3) G R^{2} / 2=-\frac{2 \pi}{3}\langle\rho\rangle^{2} R^{2}
$$

Putting everything together gives

$$
P_{\mathrm{c}}=\frac{2 \pi}{3}\langle\rho\rangle^{2} R^{2}
$$

As a rule of thumb, this formula gives central pressures that are correct to better than a factor of 10 compared to the detailed theory.



Montage of Jupiter and Galilean Moons: top to bottom: Io, Europa, Ganymede and Callisto.
(N.B.: All Galilean moons tidally locked to Jupiter - always same side is facing Jupiter)


Jupiter's moon lo - the vulcano moon (Diam. 1821 km [Earth moon: 1738 km])


Active vulcanoes on lo (interior heated by tidal forces from Jupiter), color due to large contents of sulphur and sulphur oxides in lava.
Height of vulcanoes: 6 km or higher

## Io - Tvashtar Catena

## I25 (26 Nov 1999)

+ C21 low-resolution color

127 (22 Feb 2000)
visible wavelength data

+ IR data of active lava flow

curtains of lava fountains [white: overexposed]
NASA Galileo, 1999 Nov 26

High temperature volcanism (2000 K; hotter than on Earth [1700K]!)


NASA Galileo / DLR, inset: $120 \times 110 \mathrm{~km}$
Ganymede - icy surface, ice hills and valleys, craters
Radius: 2634 km (~ Mercury!)


NASA Galileo / DLR, 1996 September 7

Europa - icy surface with ridges (colors: different kinds of ice)
Radius: 1565 km ( $\sim$ Earth Moon) possibility of water ocean below surface


Callisto: "pock faced", mainly impact craters. white: ice dark: ice-poor material

Radius: 2406 km (similar to Mercury!)


O


water e?



Structure of Jupiter's Galilean Moons similar to terrestrial planets (but some also have very thick ice layer on top)


## Saturn:



- similar to Jupiter, slightly smaller
- rapid rotation $\Longrightarrow$ flattened, banded atmosphere
- atmosphere: 75\% H, 24\% He (by mass), molecules etc. similar to Jupiter
- Rings!
- six major moons plus 27 small ones (as of Jan. 2005; mainly captured asteroids)

NASA Cassini, 2003 Dec.
Early Exploration 1970s through Pioneer 11 and 12, and then through the Voyager probes. Studied since 2004 July 1 by NASA/ESA Cassini-Huygens project (duration: four years)


NASA/ESA Cassini, 2005 July (polarised IR light)
Saturn: Similar atmospheric structure as Jupiter


NASA HST, 1999 October

Rings: equatorial plane, thin (few km high, 71000-140000 km from centre); gaps due to gravitational effects of outer moons (widest gap: Cassini's division); speed of rings agrees with 3rd Kepler ( $\Longrightarrow$ individual particles!)


NASA Voyager 2, 1981 August 22

Rings: equatorial plane, thin (few km high, 71000-140000 km from centre); gaps due to gravitational effects of outer moons (widest gap: Cassini's division); speed of rings agrees with 3rd Kepler ( $\Longrightarrow$ individual particles!)


Dione, Rings (edge on), and ring shadows on Saturn


NASA Voyager (montage)
Six major moons, typically $\langle\rho\rangle \sim 2 \mathrm{~g} \mathrm{~cm}^{-3}$
$\Longrightarrow$ mainly ice ( $60-70 \%$ ), with smallish rocky cores
As with Jupiter, small moons are captured asteroids.


Dione (surface detail, 23 km wide, 2005 Oct.) - note craters and fractures) Saturn's moons are icy moons, similar to Jupiter's Galilean moons


Tethys (2005 September; surface detail, ~500 km wide) Density of Tethys $\sim$ Water ice, so (if existent) its rocky core is small


NASA Voyager

27.10.2004, false colour IR/UV; NASA/ESA

Titan: dense atmosphere, $99 \%$ nitrogen, $1 \%$ methane, some hydrocarbons, thought to be similar to primordial atmosphere of Earth.

Radius: 2575 km ( $\sim$ Mercury!)
ESA probe Huygens landed on Titan on 2005 January 14

Surface of Titan (2005 January 14): methane ice rocks strewn over icy surface.

## Uranus:



- atmosphere cold ( $59 \mathrm{~K}=-214^{\circ} \mathrm{C}$ )
$\Longrightarrow$ ammonia has frozen out
- methane, hydrogen, and helium detected so far (less He than expected from Jupiter and Saturn!) $\Longrightarrow$ bluish color
- inclination of rotation axis: $98^{\circ}$ ("rolling on ecliptic plane").
- small ring system
- five major moons in equatorial plane plus 22 small ones (as of Jan. 2004; captured asteroids)

NASA Voyager 2, 1986 Jan 10
Flyby of Voyager 2 in 1986 January, since then only remote sensing via Hubble Space Telescope (HST) and ground based instruments.


HST Image (image enhanced) of Uranus ring system, plus evidence for banded atmosphere and clouds

major satellites have $\langle\rho\rangle \sim 1.3-2.7 \mathrm{~g} \mathrm{~cm}^{-3} \Longrightarrow$ rocks and ice


## Neptune:

- atmosphere similar to Uranus, but more active; bright methane clouds above general cloud layer
- ring system (5 individual rings)
- Two major moons (Triton, 2720 km diameter(!) and Nereid 355 km ), 11 captured asteroids

NASA Voyager 2

Flyby in 1989 August by Voyager 2, only HST since then (showed in 1995 that dark spot has vanished, detected new storm system)


Triton: ice cap of frozen methane (freezing point 90 K ) and frozen
nitrogen (freezing point 60 K ).
Few impact craters $\Longrightarrow$ young
surface $\Longrightarrow$ volcanism (dark spots
in picture; nitrogen geysers with
$T \sim 70 \mathrm{~K}$ )
Only three volcanically active bodies in solar
system: Earth, Io, and Triton.

## Pluto/Charon:

- discovered 1930
- double planet system (Pluto: $D=2320 \mathrm{~km}$, Charon: $D=1270 \mathrm{~km}$ ), 2 smaller moons
- planet nature debated

Kuiper belt: similar to asteroid belt, $>70000$ objects outside Neptune in 30-50 AU region; largest further members currently known: Quaoar ( $D=1200 \pm 200 \mathrm{~km}$ ), Ixion
$(D=1060 \pm 165 \mathrm{~km})$, Varuna $(D=900 \pm 140 \mathrm{~km}), 2002$
AW197 ( $D=890 \pm 120 \mathrm{~km}$ ), see
http://www.ifa.hawaii.edu/faculty/jewitt/kb.html

M. Brown et al. (Caltech)

2003 UB $_{313}$, discovered 2005: distance ~100 AU, brightness similar to Pluto
$\Longrightarrow$ has to be larger than Pluto, unless it is $100 \%$ reflective (unlikely)!

