

Clusters of Galaxies: defined as an excess of galaxies with respect to their surroundings.

quantitative definition:

Abell: "Cluster" = more than 50 galaxies in brightness range  $m_3 < m < m_3 + 2$  within 1.5 Mpc of cluster center ( $m_3$ : magnitude of 3rd brightest galaxy).

Catalogue:  $\sim$  4000 Clusters (including southern extension of catalogue, "Abell-Clusters", e.g., A1656=Coma)

**Zwicky:** "Cluster"= density of 50 galaxies weaker than  $m_1$  + 3 is more than twice of local galaxy density outside of cluster.

Catalogue: 9730 Clusters



Introduction

### Clusters

#### General properties of clusters:

- largest gravitationally bound objects in the universe
- clusters with up to 10000 galaxies known
- $\bullet$  total masses up to 10<sup>15</sup>  $M_{\odot}$
- linear diameter 305...12000 kpc
- small space density
- for "well defined" clusters, galaxy density  $\propto r^{-\alpha}$ , where  $\alpha \sim 0.9 \dots 1.6$ .







# Mass Luminosity Relation

Easiest method for mass determination: mass-luminosity relation.

Assumption:  $M/L \sim \text{const.}$ 

For elliptical galaxies:  $M/L \sim$  30, for spirals  $M/L \sim$  4 (i.e., always > 1).

 $\implies$  Measure L for each galaxy, determine M, and add all galaxies.

#### Problems:

- Is M/L really constant?
- faint galaxies are ignored.



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### Virial Theorem

Preferred way: Virial theorem

In equilibrium: V + 2T = 0

where

$$V = -\frac{\alpha G M^2}{R}$$

where M total mass, and  $\alpha$  depends on density distribution ( $\alpha = 3/5$  for uniform density).

The kinetic energy is

$$T = \frac{1}{2} \sum M_i v_i^2$$

Gives equation that can be solved for M.

Problems:

- Measurement of velocities and radii (we only see projected components)
- Virial theorem assumes equilibrium



Mass determination



# History

- 1965: M87 is first extragalactic source detected in X-rays
- 1969: Perseus clusters detected
- 1973–1975: UHURU detects emission from lots of clusters
- 1979: HEAO-1: Spectra: optically thin radiation
- 1984: Einstein: imaging and high resolution spectra
- 1990: ROSAT: Emission from essentially all clusters
- 1990: ASCA: high resolution spectra
- 2000: XMM/Chandra: high resolution spectra, imaging,...



7–10

## Coma in X-rays, I



ROSAT All Sky Survey image of the Coma cluster







### 7–12 RXJ1347–1145: The Brightest Cluster



Note decrease of the X-ray emissivity with distance from center of cluster.







First seen with Einstein: Cluster gas emits K $\alpha$  lines from highly ionized Mg, Si, S, Fe, etc.

X-ray emission seen from same area as optical cluster.



### X-ray Emission

- $\bullet$  X-ray Luminosity  $\sim 10^{42} \dots 10^{45}\, erg/s$
- Thermal bremsstrahlung dominant for continuum,

$$\epsilon \propto n_{\rm e} n_{\rm p} T^{-1/2} \exp\left(-E/kT\right)$$
 (7.1)

- $\bullet \Longrightarrow$  emissivity is density tracer
- $\bullet$  Temperature of the gas  $\sim 10^7 \dots 10^8 \, K$
- $\bullet$  density  $n_{
  m e} \lesssim 10^{-3}\,{
  m cm^{-3}}$
- ullet enriched in metals, e.g., Fe  $\sim$  30% solar

What powers the X-rays?





Temperature structure of Centaurus cluster as observed with *Chandra* (red: cold, blue: hot)



## Deprojection, II

Let's first assume that the X-ray emitting gas is in hydrostatic equilibrium and obeys the equation of state of an ideal gas:

$$\frac{\mathrm{d}P}{\mathrm{d}r} = -
ho \frac{\mathrm{d}\Phi}{\mathrm{d}r}$$
 and  $P = \frac{
ho kT}{\mu m_{\mathrm{p}}}$  (7.2)

in addition assume that the gravitational potential is of the form

$$\Phi = \frac{9\sigma^2}{4\pi G r_c^2} (1 + r/r_c)^{-3/2}$$
(7.3)

( $\sigma$ : galaxy velocity dispersion). ("King Profile")

Measure the temperature profile, T(r), from the local X-ray emissivity assuming  $\rho(r)$ , and solve system of equations. Iterate until convergence reached.

*Result:* T,  $\rho$ , P, and  $\Phi$  determined selfconsistently.

For clusters,  $\Phi$  is decoupled from  $\rho \Longrightarrow$  Missing mass determines gravitational potential.



### Cooling Flows

Most clusters show central peak in density structure.

evidence for a cooling flow

Why? Gas density at center is high

- $\implies \epsilon \propto n^2$
- $\implies$  gas has energy loss due to radiation
- $\Longrightarrow$  gas cools faster
- $\implies$  Pressure drops
- $\implies$  Gas gets compressed by gravity well
- $\implies$  density and therefore  $\epsilon$  increases
- $\implies$  Run away process

At the end gas is so cold that stars can form and it becomes invisible

 $\implies$  Inward motion of gas  $\implies$  Cooling flow



**Cooling Flows** 

### Cooling Flows

Estimate for mass deposition rate from X-ray luminosity:

$$L_{\rm cool} = \frac{5}{2} \frac{\dot{M}}{\mu m_{\rm p}} kT$$
(7.4)

Typical accretion rates: 200–300 $M_{\odot}$ /yr for Perseus, 20–100  $M_{\odot}$ /yr for Centaurus, 5  $M_{\odot}$ /yr for the Virgo cluster.

The accumulated mass over the time t the cooling flow works is

$$M_{\text{total}} = 10^{12} \left( \frac{\dot{M}}{100 \, M_{\odot} \text{yr}^{-1}} \right) \left( \frac{t}{10^{10} \, \text{yr}} \right) \, M_{\odot}$$

 $\implies$  continued formation of a galaxy?

