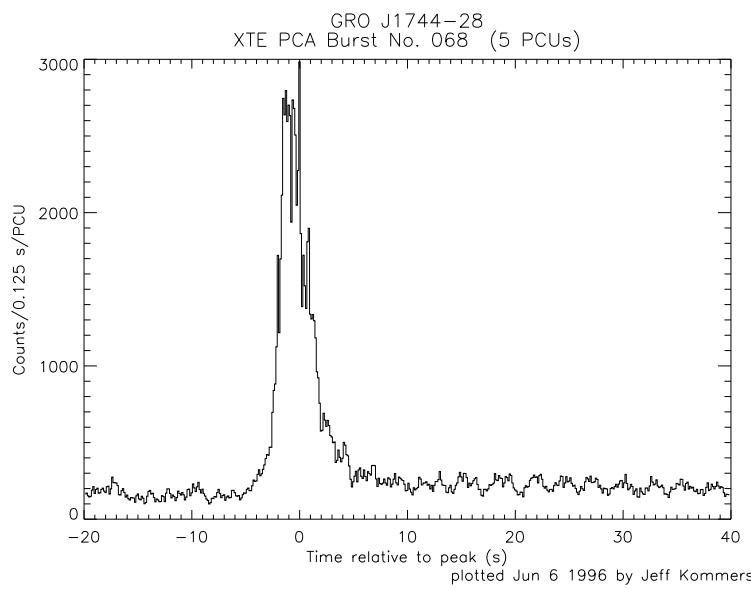


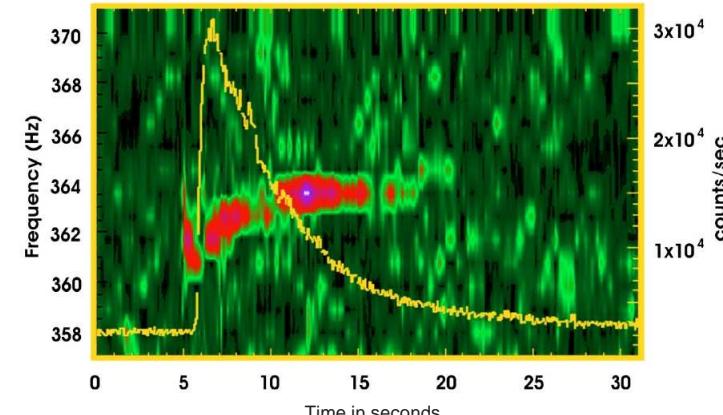
(Joss & Rappaport, 1984, Fig. 18)

Bursting of the "Rapid Burster" MXB1730–335: Type I and Type II bursts.

Type II bursts: magnetospheric gate model: B -field blocks accretion until $P_{\text{gas}} > P_{\text{mag}} \Rightarrow \text{BOOM}$.

(Bursting Pulsar; Kommers, 1996, priv. comm.)

Before 1995 December 2: X-ray bursts and pulsations cannot occur in the same object.

Then: GRO J1744–28 the bursting pulsar. Pulsations with 2 Hz and type II bursts. *Burst rate*: $\sim 20 \text{ h}^{-1}$, then decreasing to 1 h^{-1} . Orbit ~ 2 d. Source temporarily brightest X-ray source in the sky (several Crab).**Burst oscillations**

(after Galloway et al., 2006, Fig. 3; colors: power spectrum)

Burst oscillation: strong, coherent oscillation in decay of burst with long term stability. Asymptotic frequency \sim agrees with pulsar rotational frequency**Bursting Pulsar****Timing**To describe the variability of an evenly spaced time series $x_k = x(t_k = k\Delta t)$ we use the Discrete Fourier Transform $X_j = X(f_j = j/N\Delta t)$

$$X_j = \sum_{k=0}^{N-1} x_k \exp(2\pi i j k / N) \quad , \text{ for } j = 1 \dots N/2 \quad (6.11)$$

Remember: $\exp(i\phi) = \cos \phi + i \sin \phi$ The amount of variability at a frequency f_j is then characterized by the Power Spectral Density,

$$\text{PSD}_j = A X_j^* X_j \quad (6.12)$$

where A is a normalization constant.

To reduce scatter, one often averages the power spectra of several data segments.

The PSD describes the contribution of a given frequency to the total variance of the lightcurve (power).

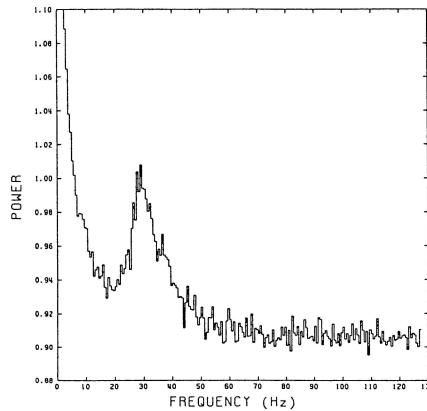
One often uses the Miyamoto normalization where

$$A_{\text{Miyamoto}} \iff (\text{rms}/\langle \text{rate} \rangle)^2 \text{ Hz}^{-1} \quad (6.13)$$



6-46

EXOSAT: The QPO Era, I



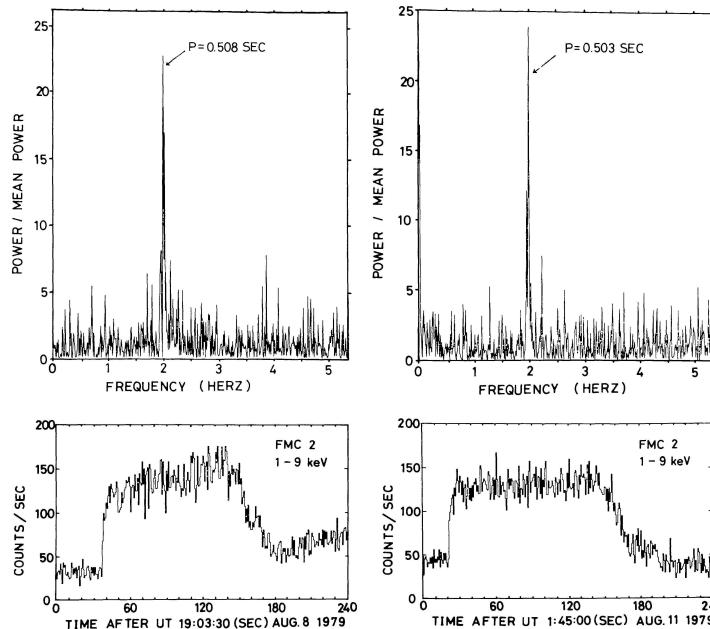
1985, IAUC 4043:
“EXOSAT observations of the bright galactic-bulge source GX 5–1 made during 1984 Sept. 18.46–18.83 UT with a time resolution of 0.25 ms show the presence of quasiperiodic oscillations of the 1–10 keV flux with a typical period between 25 and 50 ms [20–40 Hz].”

“Since this is the discovery of a new phenomenon, we urge observers to search for similar X-ray behavior in other sources ...”

van der Klis, Jansen, van Paradijs, Lewin, van den Heuvel, Trümper, Szałjno

LMXB Timing Properties

2

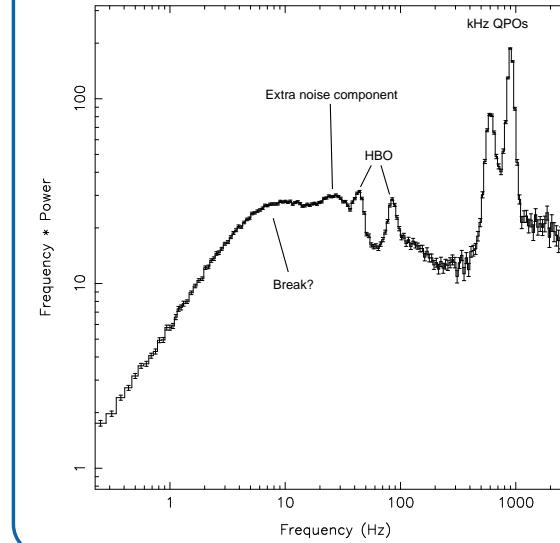


(QPOs during type II bursts of the rapid burster; Lewin, van Paradijs & van der Klis, 1988, Fig. 1.3)



6-48

RXTE: The Kilohertz QPO Era, I



“The kHz QPO are the most important scientific result to date of RXTE”.

(<http://heasarc.gsfc.nasa.gov/docs/xte/Greatest.html>)

RXTE PCA: 2–25 keV, $A_{\text{eff}} = 5000 \text{ cm}^2$, $\Delta t = 1 \mu\text{s}$

Sco X-1; van der Klis et al., 1996, IAUC 6319, Wijnands & van der Klis (1999)

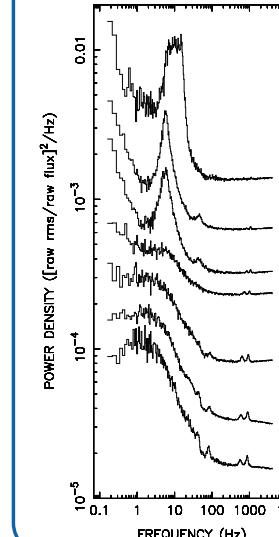
LMXB Timing Properties

4



6-49

RXTE: The Kilohertz QPO Era, II



- always have 3 characteristic frequencies:
 - “Low Frequency QPOs” (ν_{LF}): 0.1–100 Hz, many types
 - “kHz Twin Peaks” (ν_1, ν_2): 200–1400 Hz
- “real” kHz QPOs only for neutron star binaries, mostly persistent LMXBs, $\gtrsim 20$ kHz QPO sources are known, mostly showing double peaks

The kHz QPO strength is flux dependent.
(Wijnands & van der Klis, 1999)

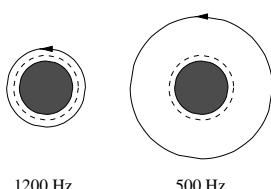
LMXB Timing Properties

5



6-50

Origin of QPOs



kHz QPOs occur on timescales close to the innermost stable circular orbit:

The Keplerian orbit frequency: is

$$\nu_{\text{orb}} = \left(\frac{GM}{4\pi^2 R_{\text{orb}}^3} \right)^{1/2} \approx 1200 \text{ Hz} \left(\frac{R_{\text{orb}}}{15 \text{ km}} \right)^{-3/2} m_{1.4}^{1/2} \quad (6.14)$$

The edge of the accretion disk is at the innermost stable circular orbit (ISCO), Schwarzschild geometry:

$$R_{\text{ISCO}} = \frac{6GM}{c^2} \sim 12.5 M_{1.4} \text{ km} \quad (6.15)$$

and therefore the maximum stable frequency in an accretion disk is

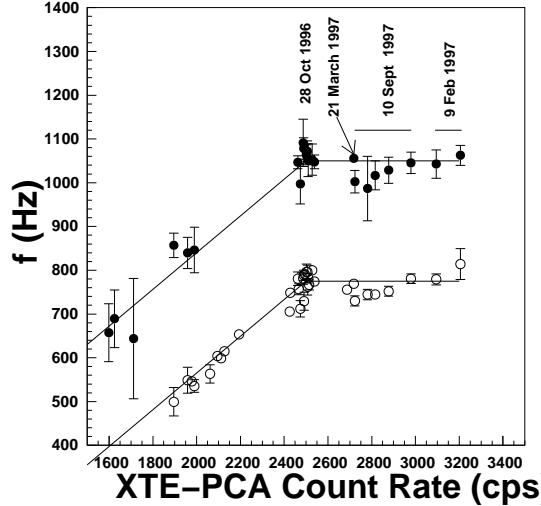
$$\nu_{\text{ISCO}} \sim \frac{1580 \text{ Hz}}{M_{1.4}} \quad (6.16)$$

Corrections due to the spin of the central object can amount to several 10%



6-51

Origin of QPOs



The frequencies of kHz QPOs usually increase with X-ray flux ("parallel-lines phenomenon"), and can saturate at a maximum frequency.
⇒ Models need to explain ν_{LF} , ν_1 , and ν_2 .

(4U 1820–30; Zhang et al., 1998)



6-52

Beat Frequency Model, I

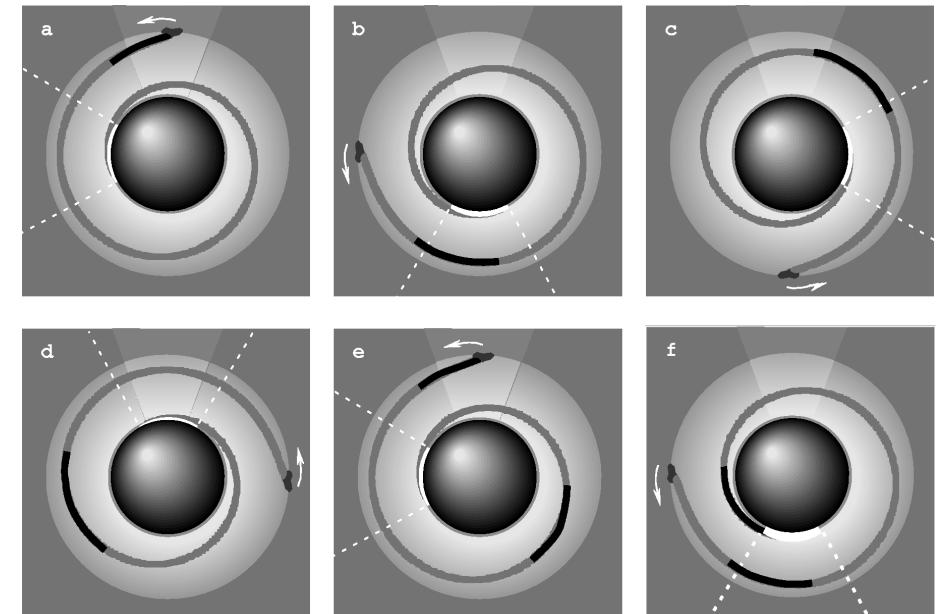
"beat": resonance between some preferred Keplerian orbit & spin frequency

Magnetospheric BFM:

- preferred radius = Alfvén radius
 - orbiting clump ($\nu_{\text{Alfvén}}$) modulated by B -field (ν_{spin})
- ⇒ can explain LF QPOs, 5–50 Hz

Sonic Point BFM:

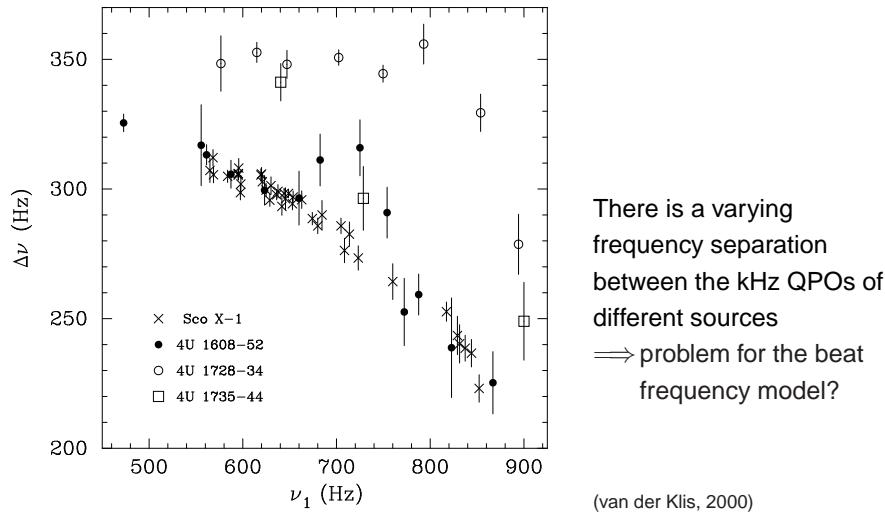
- preferred radius = where radial inflow velocity becomes supersonic, near ISCO
- orbiting clump ($\nu_{\text{sonic}} > \nu_{\text{spin}}$) causes bright footpoint near surface, **footpoint: upper kHz QPO, $\nu_2 = \nu_{\text{sonic}}$**
- clumps are irradiated with ν_{spin}
⇒ footpoint emission is modulated with beat between ν_{sonic} and ν_{spin} , **footpoint modulation: lower kHz QPO, $\nu_1 = \nu_{\text{beat}}$**



(Miller, Lamb & Psaltis, 1998)



6-54

Beat Frequency Model, III

Models for QPOs

3

6-56

Beat Frequency Model, V

Properties & problems of the sonic point beat frequency model:

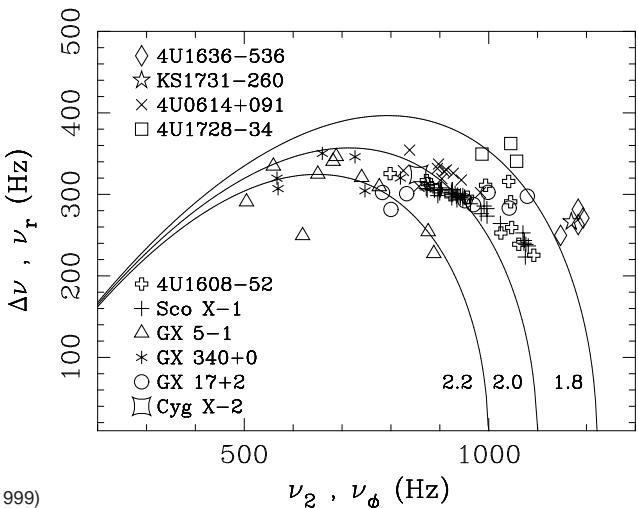
- needs surface
⇒ not valid for BHC sources
- Keplerian motion inside $r_{\text{Alfén}}$
- r_{sonic} depends on \dot{M}
⇒ varying ν_2 can be explained
- $\Delta\nu = \nu_2 - \nu_1$, constant, can be $< \nu_{\text{spin}}$
⇒ varying $\Delta\nu$ cannot easily be explained
- predicts additional frequencies (differing from precession model)

Models for QPOs

5



6-55

Beat Frequency Model, IV

Models for QPOs

4



6-57

Relativistic Precession Model, I

General Relativity: free-particle orbits show characteristic frequencies

Idea of the model:

- disk is disrupted near ISCO, forming blobs
- blob orbits are inclined and eccentric

Characteristic frequencies:

- orbit frequency: upper kHz QPO, ν_2
- periastron precession: lower kHz QPO, ν_1
- relativistic frame dragging → “wobble of the orbital plane”: nodal precession (Lense-Thirring)

$$\nu_{\text{LF}} = 2 \times \nu_{\text{nod}}$$

$$\nu_{\text{nod}} = 8\pi^2 I \nu_2^2 \nu_{\text{spin}} / c^2 M, \quad \text{where } I: \text{moment of inertia}$$

see, e.g., Stella & Vietri (1998)

Models for QPOs

6



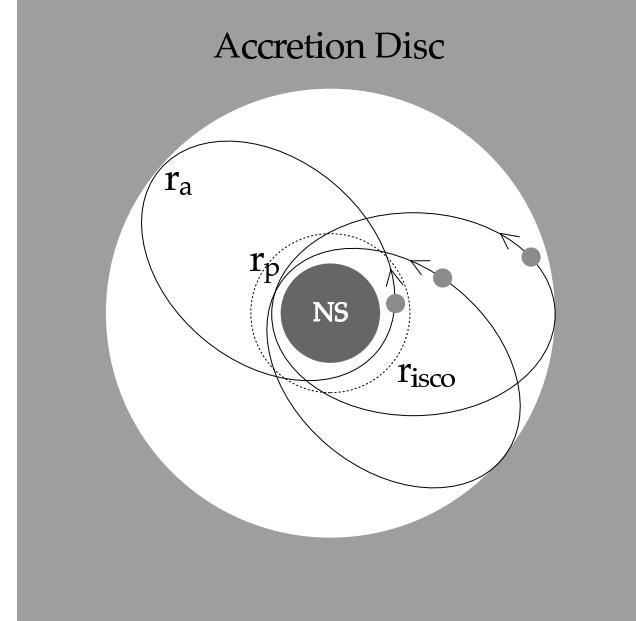
Model Summary

Promises:

- constrain M and R (via kHz QPOs)
⇒ constrain Equation of State for neutron stars
- constrain spin
("holy grail", LMXB/ms radio pulsar evolution?!)
- constrain B-field (via LF QPOs)
- observe GR effects

Difficulties:

- observations (varying $\Delta\nu_{\text{kHz}}$, ν -correlations)
triggered evolution of many different models (> 12)
- no individual model does address all issues
(i.e. generation of flux modulation, ...)
- models predict different ν_{spin} and M , e.g.,
BFM: $\nu_{\text{spin}} = 250\text{--}350 \text{ Hz}$
RPM: $\nu_{\text{spin}} = 300\text{--}900 \text{ Hz}$
- what about "surface models"? ⇐⇒ big question: do BHCs show the same behavior as neutron star XRBs?



(Marković & Lamb, 1998, see also Marković & Lamb, 2000, astro-ph/0009169)



6–59

Relativistic Precession Model, III

Properties & problems of the RPM:

- does not need surface
⇒ also valid for BHC sources
- can explain $\Delta\nu$ (more or less)
- how to disrupt the disk?
how to create compact clumps?
how to maintain tilted orbits?
- how to create the flux modulations?
- other frequencies could be more important

9

6–60

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