

Multi- $\lambda$  Paris Summer School 2009

Images from Interferometry

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Fourier transforms are at the heart of interferometry

Jean Baptiste Joseph Fourier buried 3.5 km from where we are now

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A gaussian transforms to a gaussian

A delta-function transforms to a constant

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A disc transforms to a Bessel function

Sharp edges result in many high spatial frequencies

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|                            |                                                   |
|----------------------------|---------------------------------------------------|
| FT relationships           | $f(x) \rightleftharpoons F(s)$                    |
| scaling                    | $f(\alpha x) = \alpha^{-1} F(s/\alpha)$           |
| shifting                   | $f(x - x_0) = F(s) e^{i2\pi x_0 s}$               |
| convolution/multiplication | $g(x) = f(x) \otimes h(x); \quad G(s) = F(s)H(s)$ |

Thompson, Moran & Swenson (2001)

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Image

Real

Imaginary

FT

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Image

Real

Imaginary

FT

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Real

Imaginary

multiply

Real

Imaginary

Applied Sampling Mask

FT

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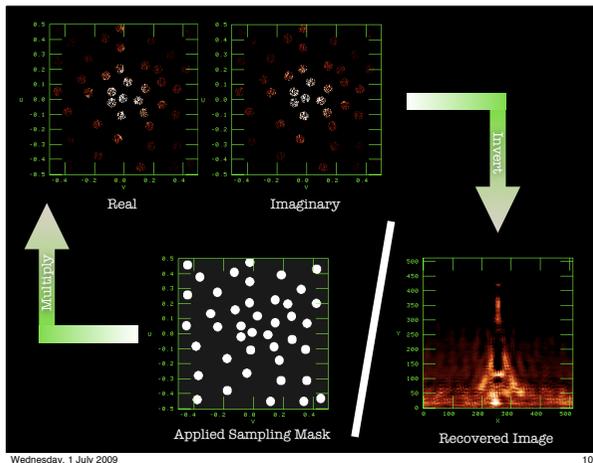
Real

Imaginary

Applied Sampling Mask

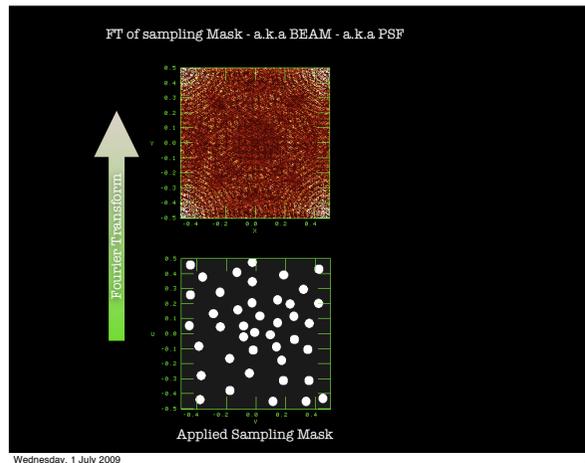
multiply

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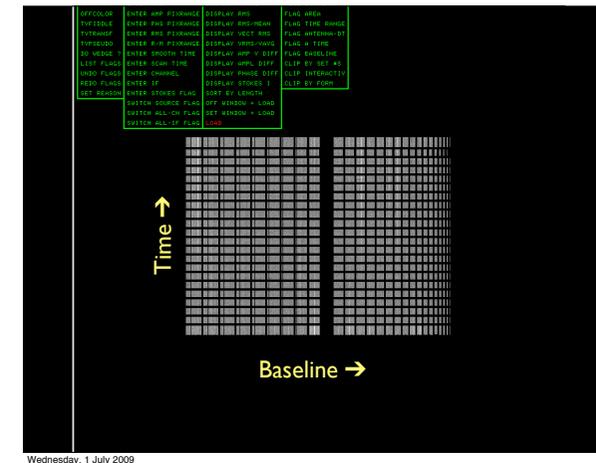
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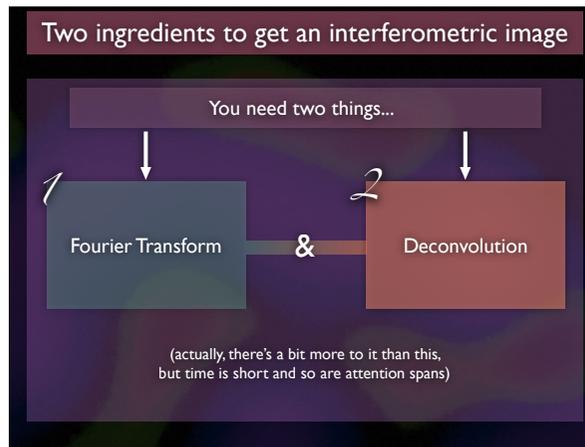
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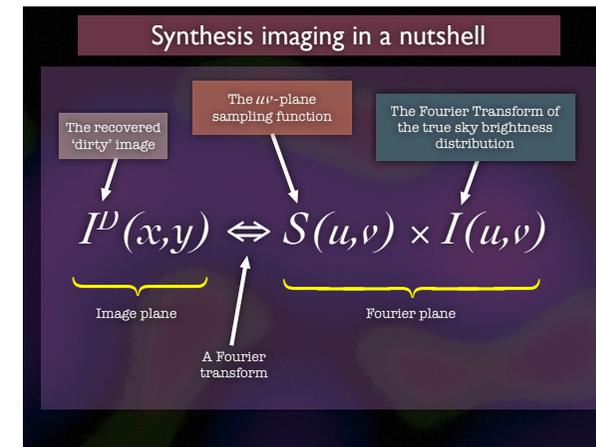


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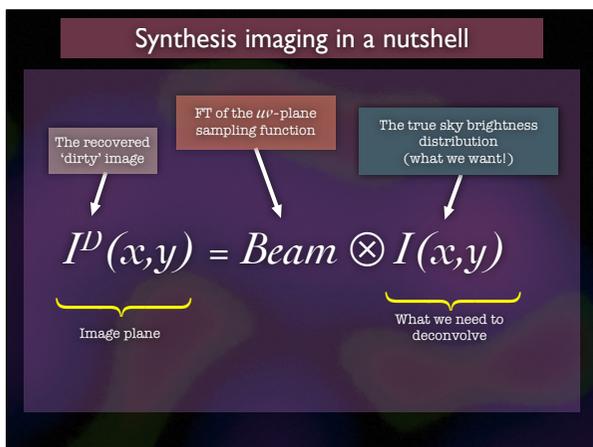


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|                                        |                                                                                      |
|----------------------------------------|--------------------------------------------------------------------------------------|
| <b>Beam</b>                            | what the image you want is convolved with, i.e. the <b>PSF</b>                       |
| <b>UV-plane (coverage)</b>             | How you have sampled the FT of what you want to observe                              |
| <b>Baseline</b>                        | <b>Single antenna pair</b> (at one instant, corresponds to one sampling of UV-plane) |
| <b>Flux calibrator (or primary)</b>    | Object of <b>known structure</b> , so we know what its amplitude & phase should be   |
| <b>Phase calibrator (or secondary)</b> | A nearby, <b>point source</b>                                                        |

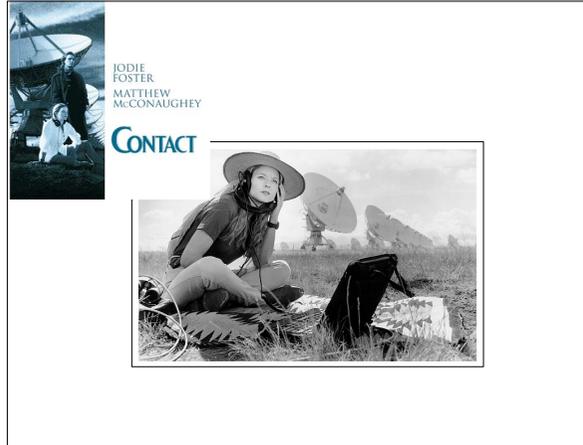
Parlez-vous interferometry?

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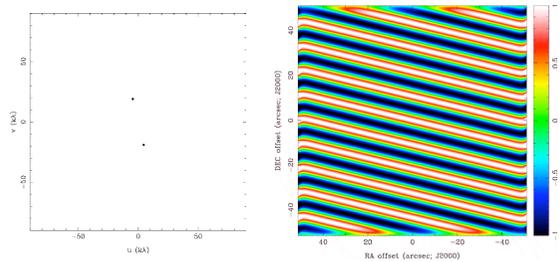
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The separation of the VLA antennas is altered every ~4 months.  
 Most extended: A Most compact: D

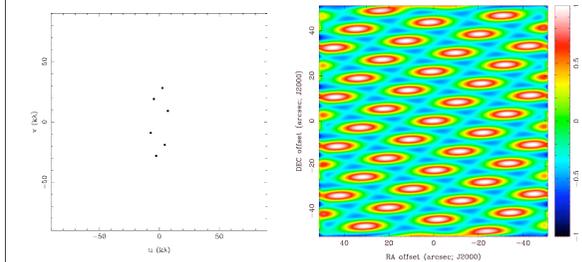
### Dirty Beam Shape and N Antennas

2 Antennas



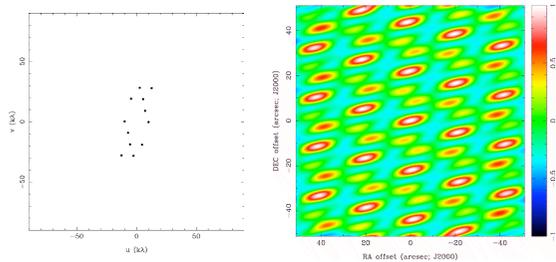
### Dirty Beam Shape and N Antennas

3 Antennas



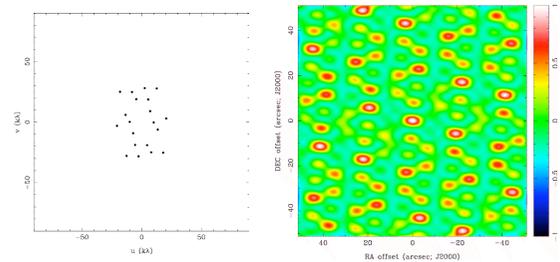
### Dirty Beam Shape and N Antennas

4 Antennas



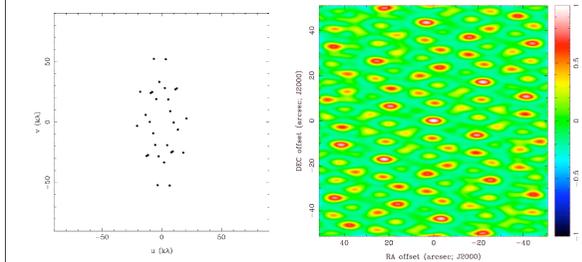
### Dirty Beam Shape and N Antennas

5 Antennas



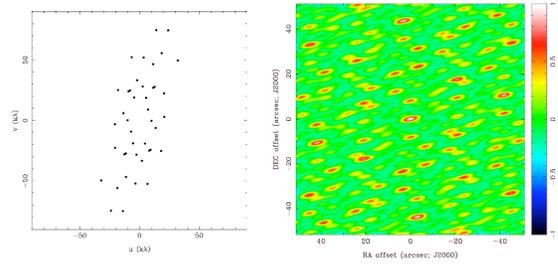
### Dirty Beam Shape and N Antennas

6 Antennas



# Dirty Beam Shape and N Antennas

7 Antennas

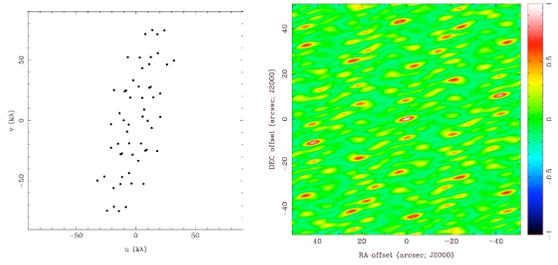


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# Dirty Beam Shape and N Antennas

8 Antennas

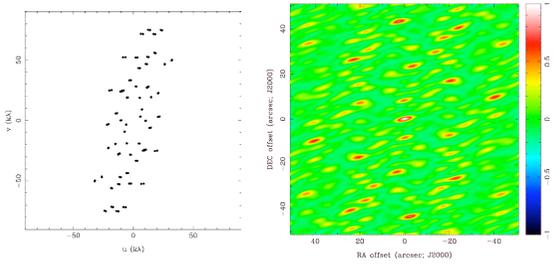


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# Dirty Beam Shape and Super Synthesis

8 Antennas x 2 samples

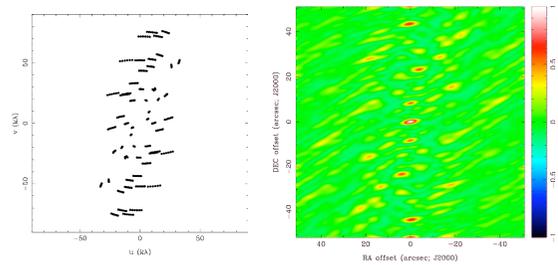


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# Dirty Beam Shape and Super Synthesis

8 Antennas x 6 samples

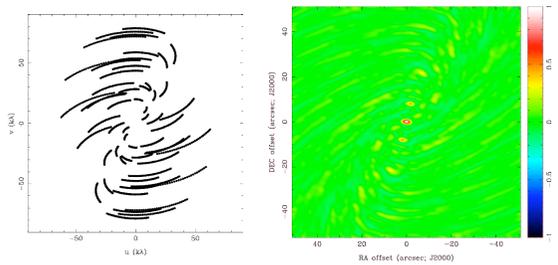


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# Dirty Beam Shape and Super Synthesis

8 Antennas x 30 samples

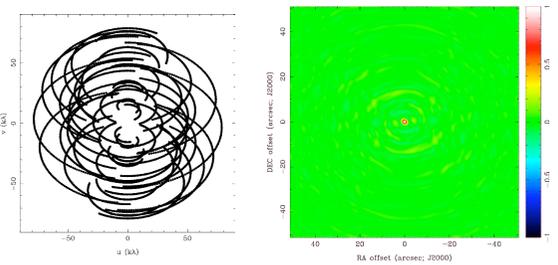


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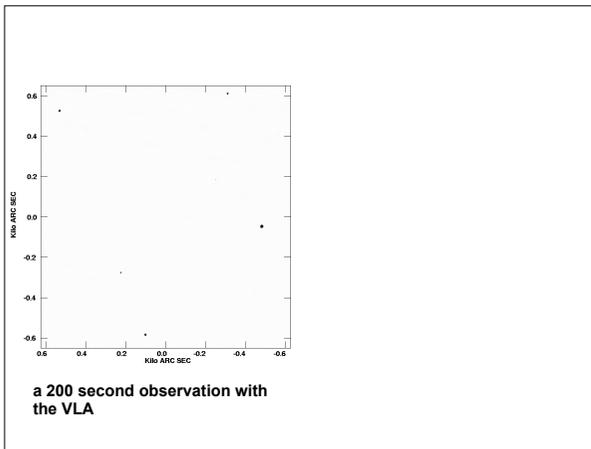
# Dirty Beam Shape and Super Synthesis

8 Antennas x 107 samples



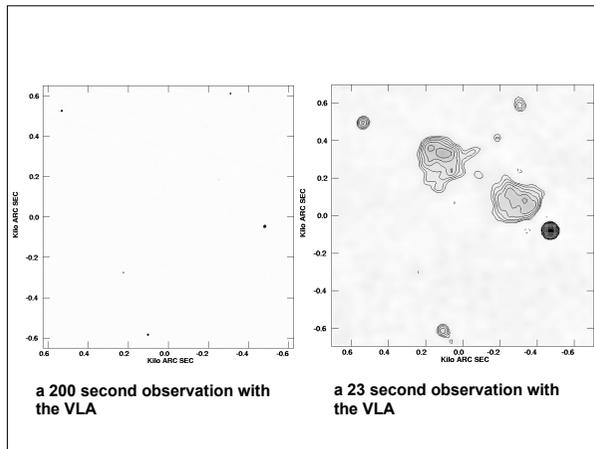
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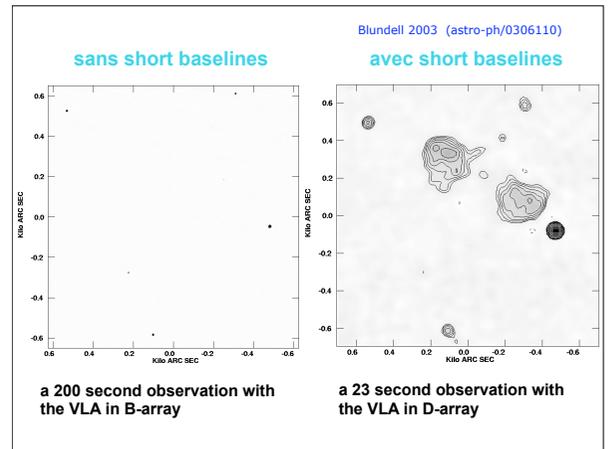
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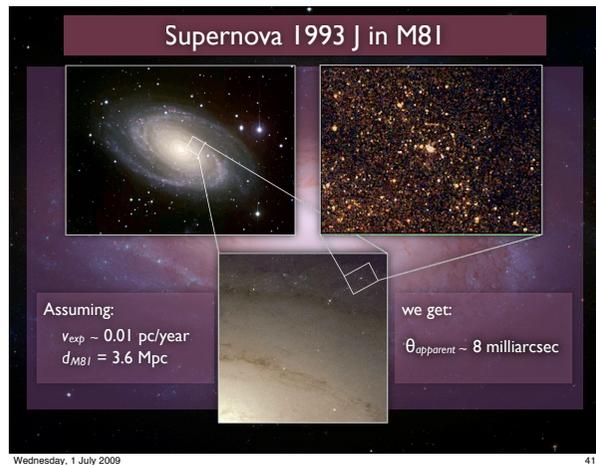
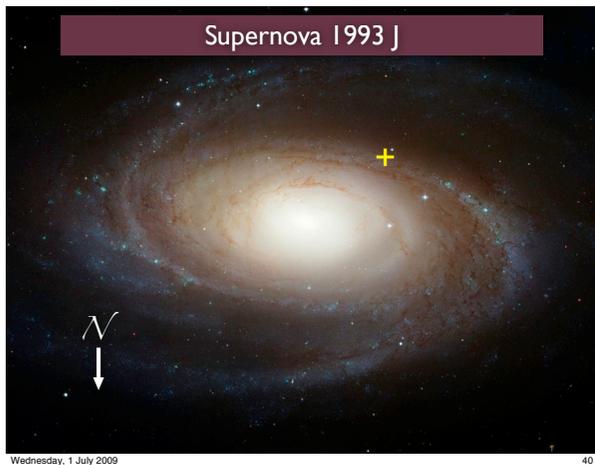
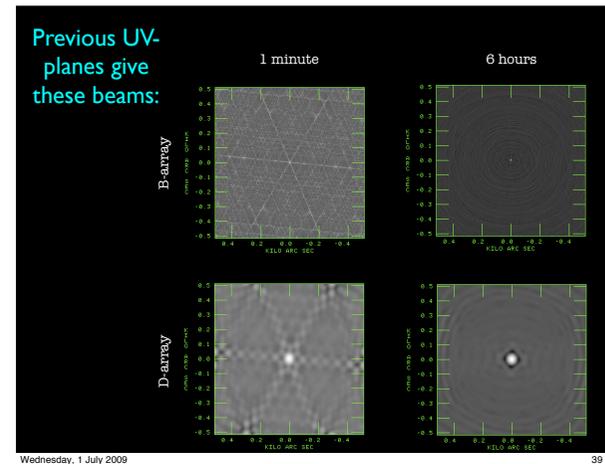
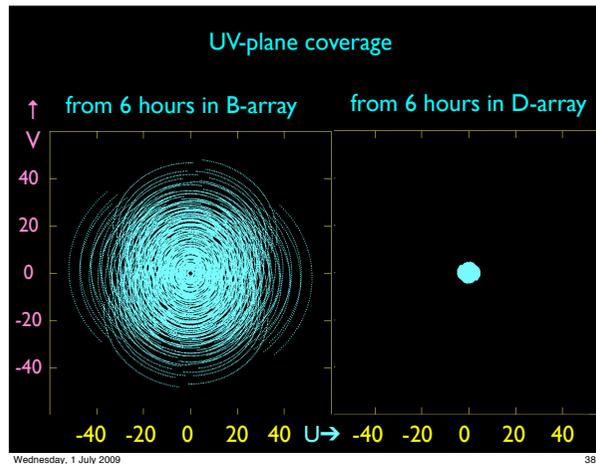
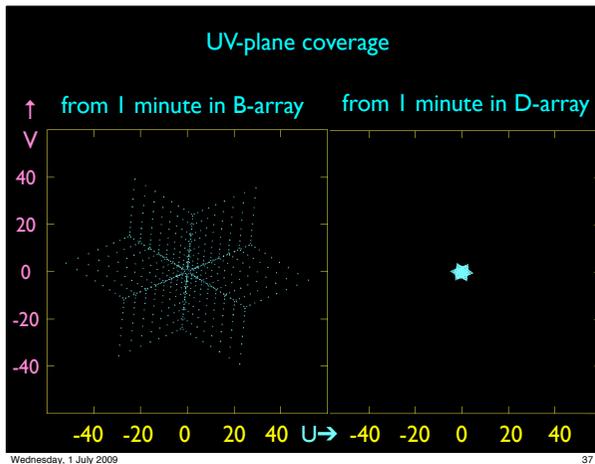
sans short baselines

avec short baselines

a 200 second observation with the VLA in B-array

a 23 second observation with the VLA in D-array

Blundell 2003 (astro-ph/0306110)



### VLBI observations of SNI993J

Shell-like radio structure resolved 239 days after outburst

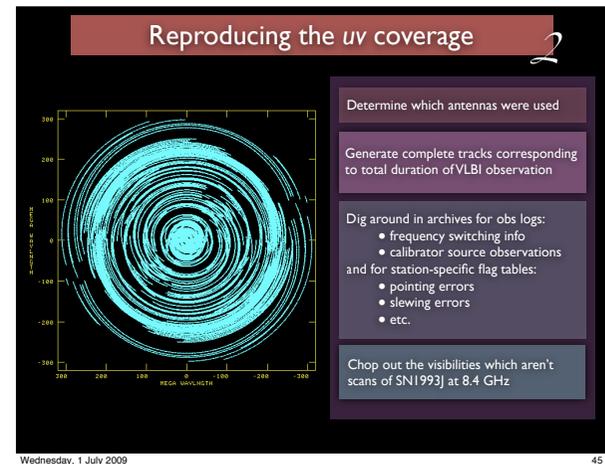
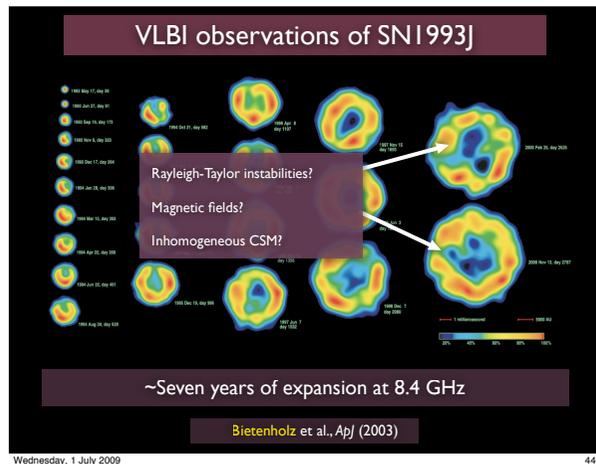
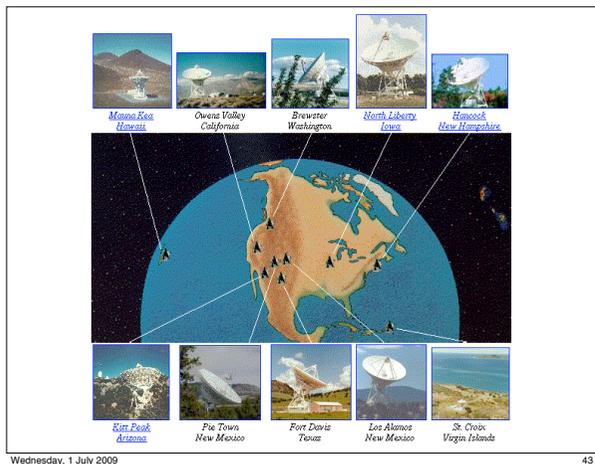
VLBI follow-up monitoring program:  
 over ~9 years and 3 frequencies

Accurate determination of explosion centre  
 Proper motion limits  
 Radio light curves and spectra  
 Measurement of expansion speed and deceleration  
 ...etc.

Extensive sequence of images of the expanding shell...

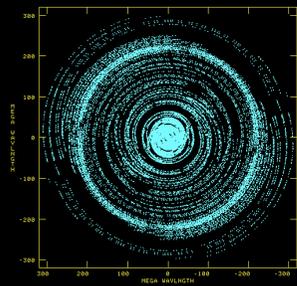
Marcaide et al., *Nature* (1995); Bietenholz et al., *ApJ* (2001; 2003); Bartel et al., *ApJ* (2002)

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## Reproducing the uv coverage

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Determine which antennas were used

Generate complete tracks corresponding to total duration of VLBI observation

Dig around in archives for obs logs:

- frequency switching info
- calibrator source observations

and for station-specific flag tables:

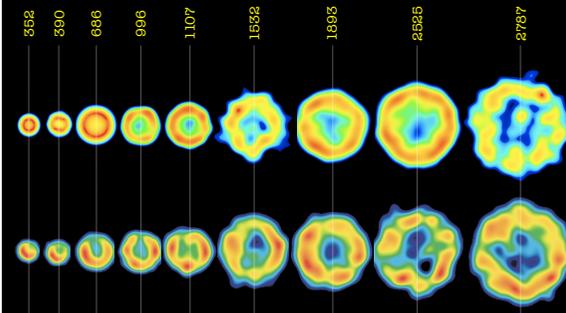
- pointing errors
- slewing errors
- etc.

Chop out the visibilities which aren't scans of SNI1993] at 8.4 GHz

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## Simulated VLBI images



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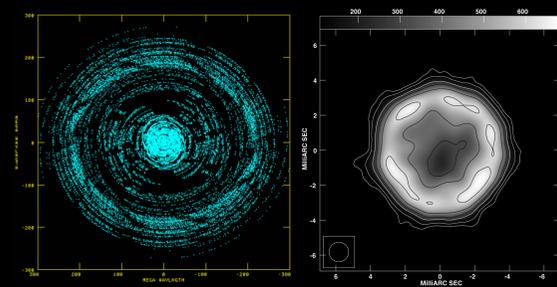
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## A few more illustrative simulations

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## Structural evolution via flagging

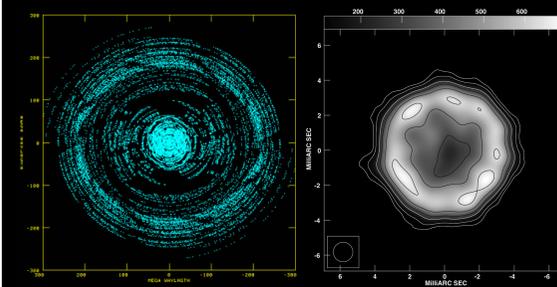


Day 2525: uv coverage and simulated image...

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## Structural evolution via flagging

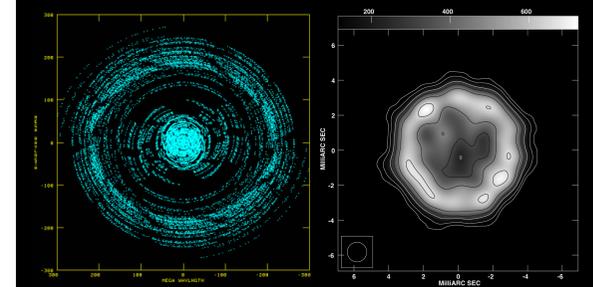


...35 degree elevation flag on Mauna Kea station...

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## Structural evolution via flagging

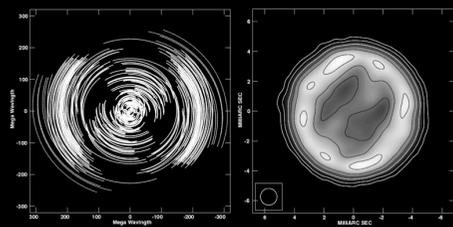


...complete removal of St. Croix station

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## Apparent rotation



Hour angle range: 00:00 - 06:00

Day 2787: six-hour continuous track;  
full figures & detailed examples in **Heywood et al 2009**

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Incomplete sampling of the Fourier plane can impart false, complex structure to a morphologically simple source

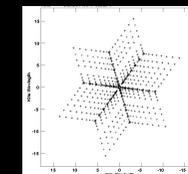
These effects are certainly partially, and potentially fully responsible for the evolving complex structure in SNI1993]

If SNI1993] has genuine clumpy structure, and it is *not* a smooth sphere (it probably isn't), the VLBI observations cannot tell the difference between these two cases

Mitigation: simulations in parallel with observations  
Full description in **Heywood et al (2009)**

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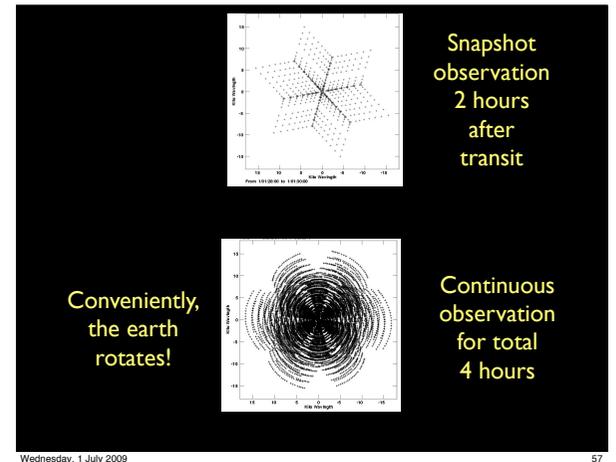
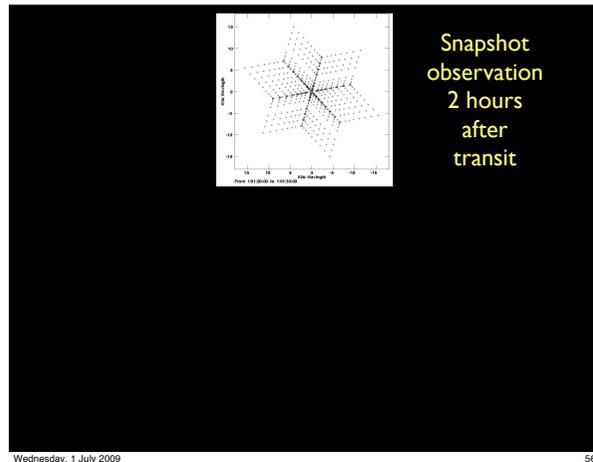
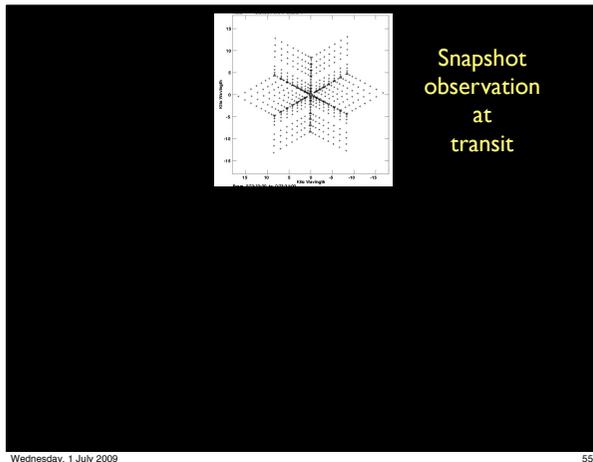
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Snapshot  
observation  
2 hours  
before  
transit

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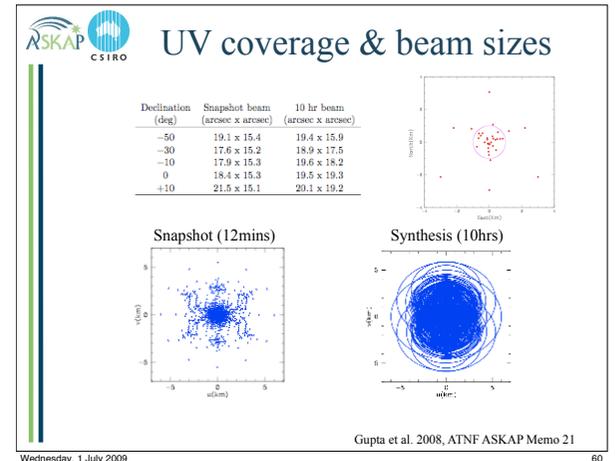
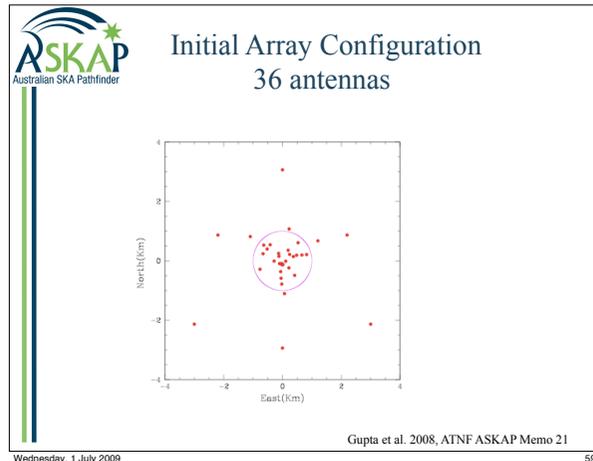
ASKAP CSIRO

Slides courtesy Ilana Feain

|                     |                                      |
|---------------------|--------------------------------------|
| Number of dishes    | 36                                   |
| Dish diameter       | 12 m                                 |
| Collecting Area     | 4070 m <sup>2</sup>                  |
| Max baseline        | 6km                                  |
| Resolution          | ~10"                                 |
| Observing frequency | 700 – 1800 MHz                       |
| Field of View       | 30 deg <sup>2</sup> (v. independent) |
| Processed Bandwidth | 300 MHz                              |
| Channels            | 16 384                               |
| System Temperature  | 35-50K                               |

+ Infrastructure for new SKA-ready observatory Murchison Radio Observatory (MRO)

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ALMA

- Atacama Large Millimetre/submillimetre Array
- Aperture synthesis array optimised for millimetre and sub-millimetre wavelengths
- High, dry site, Chajnantor Plateau, Chile (5000m)
- North America (NRAO) + Europe (ESO) + Japan (NAOJ) + Chile
- Fifty 12-m dishes, baselines from 15 m to 14 km
  - few arcsec to 5 milli-arcsec resolution
- ALMA Compact Array 12x7-m dishes, + total power
  - providing sensitivity to larger structures
- 8-GHz bandwidth, 1 mJy in 1 second at 350 GHz!
  - spectral resolution down to tens m/s

ALMA MERLIN

A.M.S. Richards EVLA May 2009 p Printed: 22/06/09

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ALMA ESO

Key performance numbers

- Baseline range 15m – 14.5 km + ACA + single dish
- Primary beam / arcsec  $\approx 17 (\lambda/\text{mm})$  [12m dish]
- Resolution/ arcsec  $\approx 0.2 (\lambda/\text{mm}) / (\text{max baseline}/\text{km})$ 
  - 0.04 arcsec at 100 GHz, 14.5 km baseline
  - 0.005 arcsec at 900 GHz, 14.5 km baseline
- Wide bandwidth (8 GHz/polarization), low noise temperatures, good site and antennas, ...  $\rightarrow$  excellent continuum sensitivity and wide spectral coverage
- Full polarization

Robert Laing European ALMA Instrument Scientist Heidelberg, June 10th 2009

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ALMA ESO

Protoplanetary discs with ALMA

Orion Trapezium HST+ALMA

Birth of planets

- $M_{\text{planet}} / M_{\text{star}} = 1.0 M_{\text{Jup}} / 5 M_{\text{sun}}$
- Orbital radius: 5AU at 50pc distance
- Disk mass = circumstellar disk around the Butterfly Star in Taurus

ALMA 850 GHz

5AU Wolf

Robert Laing European ALMA Instrument Scientist Heidelberg, June 10th 2009

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## Simulation of compact configuration and ACA

Robert Laing  
European ALMA Instrument Scientist  
Heidelberg, June 10th 2009

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## Continuous reconfiguration

Robert Laing  
European ALMA Instrument Scientist  
Heidelberg, June 10th 2009

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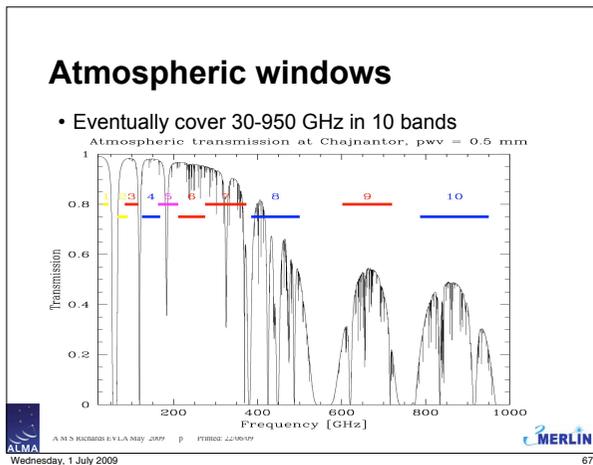
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## Prototype interferometer

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European ALMA Instrument Scientist  
Heidelberg, June 10th 2009

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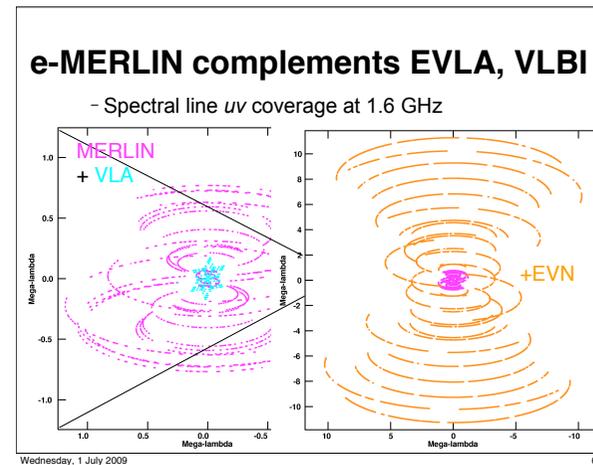
## e-MERLIN capabilities

- Resolution matches HST/JWST/ALMA
  - Sub-mas ICRF astrometry, in-beam calibration
  - Full polarization
- 6 mJy 3-s sensitivity in 12 hr at 4-8 GHz (2-GHz bw)
  - 40-mas resolution, up to 8-arcmin field of view
- ~15 mJy continuum sensitivity at other frequencies
- Spectral line sensitivity 7-20 mJy in 0.1 km/s
- Early science later this year, full operations 2010
  - Open access via UK PATT peer review
  - Joint observations with EVN/ Global VLBI
- <http://www.merlin.ac.uk>

A.M.S. Richards EVLA May 2009 p. Printed: 22/06/09

ALMA MERLIN

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## e-MERLIN

ALMA

MERLIN

EUROPEAN VLBI NETWORK

RadioNet

Northwest

JMU UNIVERSITY OF CAMBRIDGE

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## What is eMERLIN?

- MERLIN operating since 1992
- 6 dedicated antennas + Lovell
- Baselines 10-217 km
- 2 GHz opt fibre b/w
- WIDAR correlator
- Lovell upgrade
  - 10-30x sensitivity
  - 3 E-systems + Ca 32 m
    - On-axis Rx carousel
    - L-band lenses to make them fit
- Mk2, De prime focus carousels
- New receivers, hard/software

Jodrell Bank Lovell

Jodrell Bank Mk2

Pickering

Darroch

Cambridge

Duffell

Knockin

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## e-MERLIN capabilities

- Sub-mas ICRF astrometry (in-beam calibration)
- Full polarization
- Resolution matches HST/JWST, ALMA
- VO access to customised archive products
- RadioNet, NRAO software collaborations

|                 | L-band                                  | C-band                                  | K-band                                  |
|-----------------|-----------------------------------------|-----------------------------------------|-----------------------------------------|
| GHz/cm          | 1.3-1.725 / 23-17.4                     | 4.2-7.8 / 7.1-3.8                       | 21.5-24.5 / 1.4-1.2                     |
| Ang. resol'n    | 220 - 110 mas                           | 70 - 30 mas                             | 13 - 8 mas                              |
| FoV             | 13 - 30 arcmin                          | 4 - 7 arcmin                            | 2 arcmin                                |
| Continuum       | sensitivity / beam<br>(max Dn /subband) | sensitivity / beam<br>(max Dn /subband) | sensitivity / beam<br>(max Dn /subband) |
| 3s 12 hr / 4 hr | 14 nJy / 25 nJy                         | 6 nJy / 10 nJy                          | 15 nJy / 26 nJy                         |

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## Spectral capabilities

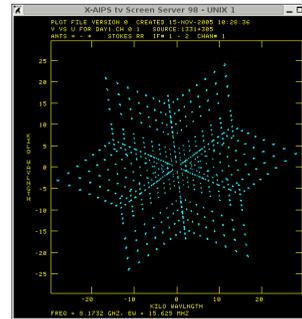
- Spectral resolution  $\Delta\nu \approx 2 \text{ Hz}$  ( $l/d \approx 7 \times 10^8$  @ 21cm)
- No more jumping about to cover high velocity sources!
- Transfer calibration between lines and continuum
- Almost always a good, close calibrator
  - Achieve optimal sensitivity even if line too weak to self-cal
- Easy to match spectral configs with EVLA or VLBI

| Spectral       | L-band                             | C-band                             | K-band                             |
|----------------|------------------------------------|------------------------------------|------------------------------------|
| 3s 12 hr / 4 h | sensitivity /beam<br>(per channel) | sensitivity /beam<br>(per channel) | sensitivity /beam<br>(per channel) |
| Lines:         |                                    |                                    |                                    |
| 0.05 km/s      | 23 mJy / 40 mJy                    | 10 mJy / 17 mJy                    | 32 mJy / 55 mJy                    |
| 3 km/s         | 2.9 mJy / 5 mJy                    | 1.3 mJy / 2.2 mJy                  | 4 mJy / 7 mJy                      |
| Continuum      | (max Dn /subband)                  | (max Dn /subband)                  | (max Dn /subband)                  |
| 12 subbands    | 17 nJy / 30 nJy                    | 8 nJy / 14 nJy                     | 17 nJy / 30 nJy                    |

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## Looking at UV-data: U versus V

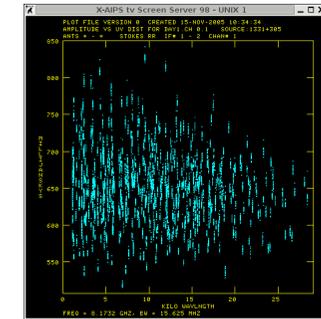


task 'UVPLT'; bparm 6,7

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## Looking at UV-data: Amplitude versus baseline length

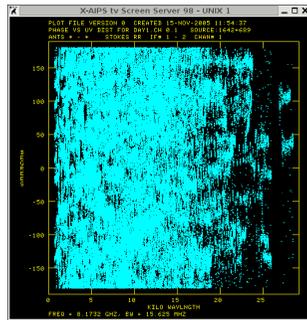


task 'UVPLT'; bparm 0,0

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## Looking at UV-data: Phase versus baseline length



task 'UVPLT'; bparm 0,2

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## Pixel size and image size

- Pixel size
  - should satisfy sampling theorem for longest baselines,  $\Delta x < 1/2 u_{\max}$ ,  $\Delta y < 1/2 v_{\max}$
  - In practice, use 3-5 pixels across dirty beam
- Image size
  - Image size 2 x primary beam
  - Sometimes larger

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## Deconvolution via CLEAN

- Identify strongest feature in dirty image
- Add a fraction  $g$  (loop gain) of this point source to the "clean components" list
- Subtract *this fraction multiplied by the beam* from the dirty image
- Repeat...
- Finally, convolve clean component list with clean beam and add back to (cleaned) dirty image to give restored image

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## Remarkably important tip regarding CLEAN

- Well worth taking the time to centre the brightest point on the dirty image on the centre of a pixel.

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$$V_{ij}(t) = g_i(t)g_j^*(t)V^{\text{true}}(t) + \epsilon_{ij}(t)$$

Complex gain of antenna  $i$  (points to  $g_i(t)$ )  
 Additive noise (points to  $\epsilon_{ij}(t)$ )  
 True visibility (but use model) (points to  $V^{\text{true}}(t)$ )  
 Visibility measured between antennas  $i$  and  $j$  (points to  $V_{ij}(t)$ )

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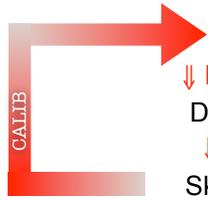
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## Self-calibration

- a priori calibration not perfect
  - calibration solutions from a different time, different direction from target
- Self-cal aims to find antenna-based errors ( $N$  complex gains) while making use of model of your target.  $N(N-1)/2$  visibilities.
- Absolute positional information is preserved IF model has correct initial position
- Dangerous if target is complex, and/or signal-to-noise is low
- Iterative technique: start with conservative model, improve...

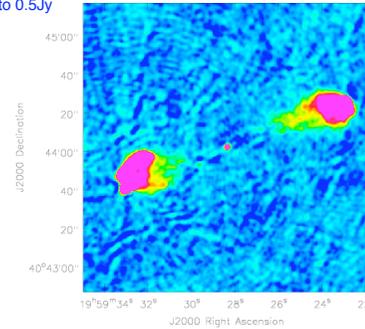
Wednesday, 1 July 2009

81

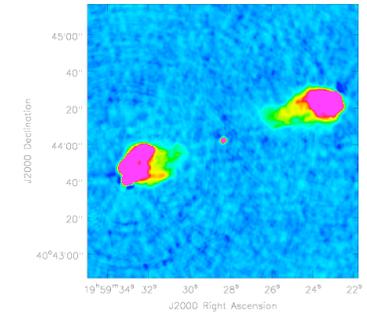


Calibrated Visibilities  
 ↓ Fourier Transform [IMAGR]  
 Dirty Beam and Dirty Image  
 ↓ Deconvolution [IMAGR]  
 Sky Model, “restored” Image

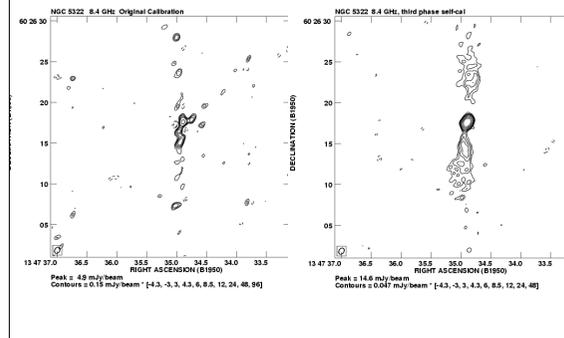
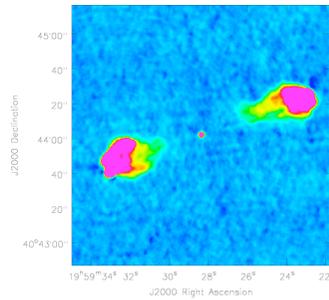
Phase calibration using nearby source observed every 20 minutes  
 Peak ~ 22Jy  
 Display shows -0.05Jy to 0.5Jy



Phase self-cal  
 every 10 seconds



Then after 1 amp+ phase self-cal



## Rules of thumb for self-cal

- Start with phase self-cal. (Meaning no amplitude self-cal)
- Short solution interval (~30 seconds)
- As final(ish) step: amplitude+phase self-cal (~20 minutes)
- Only include baselines in model if their flux is included

## When self-calibration is risky / impossible

When your target source is too weak and feeble to self-calibrate, then need to use phase-referencing technique (extreme form of which is fast-switching).