



### Question 1: *Synchrotron Self-Absorption*

For an electron gas, the energy density is  $u = nkT/(\gamma_{\text{SH}} - 1)$  where  $\gamma_{\text{SH}}$  is the ratio of specific heats, which is 4/3 for a relativistic gas and 5/3 for a non-relativistic gas.

- a) Convince yourself that it makes sense to associate a temperature  $T_e$  with electrons of particle energy  $\gamma m_e c^2$  by setting

$$\gamma m_e c^2 = 3kT_e \quad (\text{w1.1})$$

- b) In the Rayleigh-Jeans-limit, the flux of a source with angular size  $\Omega$  is

$$S_\nu = \frac{2kT}{\lambda^2} \Omega \quad (\text{w1.2})$$

Taking the above into account, show that for optically thick synchrotron radiation

$$S_\nu \propto \nu^{5/2} B^{-1/2} \quad (\text{w1.3})$$

Note:  $\gamma \sim (\nu/\nu_L)^{1/2}$  and  $\nu_L = eB/m_e c$